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Exploring cosmic origins with CORE: Effects of observer peculiar motion

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Abstract. We discuss the effects on the cosmic microwave background (CMB), cosmic infrared background (CIB), and thermal Sunyaev-Zeldovich effect due to the peculiar motion of an observer with respect to the CMB rest frame, which induces boosting effects. After a brief review of the current observational and theoretical status, we investigate the scientific perspectives opened by future CMB space missions, focussing on the Cosmic Origins Explorer (CORE) proposal. The improvements in sensitivity offered by a mission like CORE, together with its high resolution over a wide frequency range, will provide a more accurate estimate of the CMB dipole. The extension of boosting effects to polarization and cross-correlations will enable a more robust determination of purely velocity-driven effects that are not degenerate with the intrinsic CMB dipole, allowing us to achieve an overall signal-to-noise ratio of 13; this improves on the *Planck* detection and essentially equals that of an ideal cosmic-variance-limited experiment up to a multipole $\ell \simeq 2000$. Precise inter-frequency calibration will offer the opportunity to constrain or even detect CMB spectral distortions, particularly from the cosmological reionization epoch, because of the frequency dependence of the dipole spectrum, without resorting to precise absolute calibration. The expected improvement with respect to COBE-FIRAS in the recovery of distortion parameters (which could in principle be a factor of several hundred for an ideal experiment with the CORE configuration) ranges from a factor of several up to about 50, depending on the quality of foreground removal and relative calibration. Even in the case of $\simeq 1\%$ accuracy in both foreground removal and relative calibration at an angular scale of 1° , we find that dipole analyses for a mission like CORE will be able to improve the recovery of the CIB spectrum amplitude by a factor $\simeq 17$ in comparison with current results based on COBE-FIRAS. In addition to the scientific potential of a mission like CORE for these analyses, synergies with other planned and ongoing projects are also discussed.

Keywords: CMBR experiments, CMBR theory, high redshift galaxies, reionization

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1 Introduction

The peculiar motion of an observer with respect to the cosmic microwave background (CMB) rest frame gives rise to boosting effects (the largest of which is the CMB dipole, i.e., the multipole $\ell = 1$ anisotropy in the Solar System barycentre frame), which can be explored by future CMB missions. In this paper, we focus on peculiar velocity effects and their relevance to the Cosmic Origins Explorer (CORE) experiment. CORE is a satellite proposal dedicated to microwave polarization and submitted to the European Space Agency (ESA) in October 2016 in response to a call for future medium-sized space mission proposals for the M5 launch opportunity of ESA’s Cosmic Vision programme.

This work is part of the *Exploring Cosmic Origins* (ECO) collection of articles, aimed at describing different scientific objectives achievable with the data expected from a mission like CORE. We refer the reader to the CORE proposal [1] and to other dedicated ECO papers for more details, in particular the mission requirements and design paper [2] and the instrument paper [3], which provide a comprehensive discussion of the key parameters of CORE adopted in this work. We also refer the reader to the paper on extragalactic sources [4] for an investigation of their contribution to the cosmic infrared background (CIB), which is one of the key topics addressed in the present paper, as well as the papers on B -mode component separation [5] for a stronger focus on polarization, and mitigation of systematic effects [6] for further discussion of potential residuals included in some analyses presented in this work. Throughout this paper we use the CORE specifications summarised in table 1.

The analysis of cosmic dipoles is of fundamental relevance in cosmology, being related to the isotropy and homogeneity of the Universe at the largest scales. In principle, the observed dipole is a combination of various contributions, including observer motion with respect to the CMB rest frame, the intrinsic primordial (Sachs-Wolfe) dipole and the Integrated Sachs-Wolfe dipole as well as dipoles from astrophysical (extragalactic and Galactic) sources. The interpretation that the CMB dipole is mostly (if not fully) of kinematic origin has strong support from independent studies of the galaxy and cluster distribution, in particular via the measurements of the so-called *clustering dipole*. According to the linear theory of cosmological perturbations, the peculiar velocity of an observer (as imprinted in the CMB dipole) should be related to the observer’s peculiar gravitational acceleration via $\vec{v}_{\text{lin}} = \beta_{\text{rd}} \vec{g}_{\text{lin}}$, where $\beta_{\text{rd}} \simeq \Omega_m^{0.55} / b_g$ is also known as the redshift-space distortion parameter (b_g and Ω_m being, respectively, the bias of the particular galaxy sample and the matter density parameter at the present time). The peculiar velocity and acceleration of, for instance, the Local Group treated as one system, i.e., as measured from its barycentre, should thus be aligned and have a specific relation between amplitudes. The former fact has been confirmed from analyses of many surveys over the last three decades, such as IRAS [7, 8], 2MASS [9, 10], or galaxy cluster samples [11, 12]. As far as the amplitudes are concerned, the comparison has been used to place constraints on the β_{rd} parameter [10, 11, 13–15], totally independent of those from redshift-space distortions observed in spectroscopic surveys. In this context, confirming the kinematic origin of the CMB dipole, through a comparison accounting for our Galaxy’s motion in the Local Group and the Sun’s motion in the Galaxy (see e.g., refs. [16, 17]), would provide support for the standard cosmological model, while finding any significant deviations from this assumption could open up the possibility for other interpretations (see e.g., refs. [18–21]).

Cosmic dipole investigations of more general type have been carried out in several frequency domains [22], where the main signal comes from various types of astrophysical sources differently weighted in different shells in redshift. An example are dipole studies in

Channel [GHz]	Beam [arcmin]	N_{det}	ΔT [$\mu\text{K}\cdot\text{arcmin}$]	ΔP [$\mu\text{K}\cdot\text{arcmin}$]	ΔI [$\mu\text{K}_{\text{RJ}}\cdot\text{arcmin}$]	ΔI [$\text{kJy sr}^{-1}\cdot\text{arcmin}$]	$\Delta y \times 10^6$ [$y_{\text{SZ}}\cdot\text{arcmin}$]
60	17.87	48	7.5	10.6	6.81	0.75	-1.5
70	15.39	48	7.1	10	6.23	0.94	-1.5
80	13.52	48	6.8	9.6	5.76	1.13	-1.5
90	12.08	78	5.1	7.3	4.19	1.04	-1.2
100	10.92	78	5.0	7.1	3.90	1.2	-1.2
115	9.56	76	5.0	7.0	3.58	1.45	-1.3
130	8.51	124	3.9	5.5	2.55	1.32	-1.2
145	7.68	144	3.6	5.1	2.16	1.39	-1.3
160	7.01	144	3.7	5.2	1.98	1.55	-1.6
175	6.45	160	3.6	5.1	1.72	1.62	-2.1
195	5.84	192	3.5	4.9	1.41	1.65	-3.8
220	5.23	192	3.8	5.4	1.24	1.85	...
255	4.57	128	5.6	7.9	1.30	2.59	3.5
295	3.99	128	7.4	10.5	1.12	3.01	2.2
340	3.49	128	11.1	15.7	1.01	3.57	2.0
390	3.06	96	22.0	31.1	1.08	5.05	2.8
450	2.65	96	45.9	64.9	1.04	6.48	4.3
520	2.29	96	116.6	164.8	1.03	8.56	8.3
600	1.98	96	358.3	506.7	1.03	11.4	20.0
Array		2100	1.2	1.7			0.41

Table 1. *Proposed CORE-M5 frequency channels.* The sensitivity is estimated assuming $\Delta\nu/\nu = 30\%$ bandwidth, 60 % optical efficiency, total noise of twice the expected photon noise from the sky and the optics of the instrument being at 40 K. The second column gives the FWHM resolution of the beam. This configuration has 2100 detectors, about 45 % of which are located in CMB channels between 130 and 220 GHz. Those six CMB channels yield an aggregated CMB sensitivity of $2\,\mu\text{K}\cdot\text{arcmin}$ ($1.7\,\mu\text{K}\cdot\text{arcmin}$ for the full array).

the radio domain, pioneered by ref. [23] and recently revisited by ref. [24] performing a re-analysis of the NRAO VLA Sky Survey (NVSS) and the Westerbork Northern Sky Survey, as well as by refs. [25, 26] using NVSS data alone. Prospects to accurately measure the cosmic radio dipole with the Square Kilometre Array have been studied by ref. [27]. Perspectives on future surveys jointly covering microwave/millimeter and far-infrared wavelengths aimed at comparing CMB and CIB dipoles have been presented in ref. [28]. The next decades will see a continuous improvement of cosmological surveys in all bands. For the CMB, space observations represent the best, if not unique, way to precisely measure this large-scale signal. It is then important to consider the expectations from (and the potential issues for) future CMB surveys beyond the already impressive results produced by *Planck*.

In addition to the dipole due to the combination of observer velocity and Sachs-Wolfe and intrinsic (see ref. [29] for a recent study) effects, a moving observer will see velocity imprints on the CMB due to Doppler and aberration effects [30, 31], which manifest themselves in correlations between the power at subsequent multipoles of both temperature and polarization anisotropies. Precise measurements of such correlations [32, 33] provide important consistency checks of fundamental principles in cosmology, as well as an alternative and general way to probe observer peculiar velocities [21, 34]. This type of analysis can in principle be extended to thermal Sunyaev-Zeldovich (tSZ) [35] and CIB signals. We will discuss how

these investigations could be improved when applied to data expected from a next generation of CMB missions, exploiting experimental specifications in the range of those foreseen for LiteBIRD [36] and CORE.

Since the results from COBE [37], no substantial improvements have been achieved in the observations of the CMB spectrum at $\nu \gtrsim 30$ GHz.¹ Absolute spectral measurements rely on ultra-precise absolute calibration. FIRAS [41] achieved an absolute calibration precision of 0.57 mK, with a typical inter-frequency calibration accuracy of 0.1 mK in one decade of frequencies around 300 GHz. The amplitude and shape of the CIB spectrum, measured by FIRAS [42], is still not well known. Anisotropy missions, like CORE, are not designed to have an independent absolute calibration, but nevertheless can investigate the CMB and CIB spectra by looking at the frequency spectral behaviour of the dipole amplitude [43–46]. Unavoidable spectral distortions are predicted as the result of energy injections in the radiation field occurring at different cosmic times, related to the origin of cosmic structures and to their evolution, or to the different evolution of the temperatures of matter and radiation (for a recent overview of spectral distortions within standard Λ CDM, see ref. [47]). For quantitative forecasts we will focus on well-defined types of signal, namely Bose-Einstein (BE) and Comptonization distortions [48, 49]; however, one should also be open to the possible presence of unconventional heating sources, responsible in principle for imprints larger than (and spectral shapes different from) those mentioned above, and having parameters that could be constrained through analysis of the CMB spectrum. Deciphering such signals will be a challenge, but holds the potential for important new discoveries and for constraining unexplored processes that cannot be probed by other means. At the same time, a better determination of the CIB intensity greatly contributes to our understanding of the dust-obscured star-formation phase of galaxy evolution.

The rest of this paper is organised as follows. In section 2 we quantify the accuracy of a mission like CORE for recovering the dipole direction and amplitude separately at a given frequency, focussing on a representative set of CORE channels. Accurate relative calibration and foreground mitigation are crucial for analysing CMB anisotropy maps. In section 3 we describe a parametric approach to modelling the pollution of theoretical maps with potential residuals. The analysis in section 2 is then extended in section 4 to include a certain level of residuals. The study throughout these sections is carried out in pixel domain.

In section 5 we describe the imprints at $\ell > 1$ due to Doppler and aberration effects, which can be measured in harmonic space. Precise forecasts based on CORE specifications are presented and compared with those expected from LiteBIRD. The intrinsic signature of a boost in Sunyaev-Zeldovich and CIB maps from CORE is also discussed in this section.

In section 6 we study CMB spectral distortions and the CIB spectrum through the analysis of the frequency dependence of the dipole distortion; we introduce a method to extend predictions to higher multipoles, coupling higher-order effects and geometrical aspects. The theoretical signals are compared with sensitivity at different frequencies, in terms of angular power spectrum, for a mission like CORE. In section 7 we exploit the available frequency coverage through simulations to forecast CORE’s sensitivity to the spectral distortion parameters and the CIB spectrum amplitude, considering the ideal case of perfect relative calibration and foreground subtraction; however, we also parametrically quantify the impact of potential residuals, in order to define the requirements for substantially improve the results beyond those from FIRAS.

¹For recent observations at long wavelengths, see the results from the ARCADE-2 balloon [38, 39] and from the TRIS experiment [40].

In section 8 we summarise and discuss the main results. The basic concepts and formalisms are introduced in the corresponding sections, while additional information and technical details are provided in several dedicated appendices for sake of completeness.

2 The CMB dipole: forecasts for CORE in the ideal case

A relative velocity, $\beta \equiv v/c$, between an observer and the CMB rest frame induces a dipole (i.e., $\ell = 1$ anisotropy) in the temperature of the CMB sky through the Doppler effect. Such a dipole is likely dominated by the velocity of the Solar System, $\vec{\beta}_S$, with respect to the CMB (Solar dipole), with a seasonal modulation due to the velocity of the Earth/satellite, $\vec{\beta}_o$, with respect to the Sun (orbital dipole). In this work we neglect the orbital dipole (which may indeed be used for calibration), thus hereafter we will denote with $\vec{\beta}$ the relative velocity of the Solar dipole.

In this section we forecast the ability to recover the dipole parameters (amplitude and direction) by performing a Markov chain Monte Carlo (MCMC) analysis in the ideal case (i.e., without calibration errors or sky residuals). Results including systematics are given in section 4. We test the amplitude of the parameter errors against the chosen sampling resolution and we probe the impact of both instrumental noise and masking of the sky. We consider the “*Planck* common mask 76” (in temperature), which is publicly available from the Planck Legacy Archive (PLA)² [50], and keeps 76 % of the sky, avoiding the Galactic plane and regions at higher Galactic latitudes contaminated by Galactic or extragalactic sources. We exploit here an extension of this mask that excludes all the pixels at $|b| \leq 30^\circ$.³

Additionally, we explore the dipole reconstruction ability for different frequency channels, specifically 60, 100, 145, and 220 GHz. We finally investigate the impact of spectral distortions (see sections 6 and 7), treating the specific case of a BE spectrum (with chemical potential $\mu_0 = 1.4 \times 10^{-5}$, which is several times smaller than FIRAS upper limits).

We write the dipole in the form:

$$d(\hat{n}) = A \hat{n} \cdot \hat{n}_0 + T_0, \quad (2.1)$$

where \hat{n} and \hat{n}_0 are the unit vectors defined respectively by the Galactic longitudes and latitudes (l, b) and (l_0, b_0) . In figure 1 we show the dipole map we have used in our simulations, generated assuming the best-fit values of the measurements of the dipole amplitude, $A = (3.3645 \pm 0.0002)$ mK, and direction, $l_0 = 264.00^\circ \pm 0.03^\circ$ and $b_0 = 48.24^\circ \pm 0.02^\circ$, found in the *Planck* (combined result from the High Frequency Instrument, HFI, and Low Frequency Instrument, LFI) 2015 release [51–53]. Assuming the dipole to be due to velocity effects only, its amplitude corresponds to $\beta \equiv |\vec{\beta}| \equiv v/c = A/T_0 = 1.2345 \times 10^{-3}$, with $T_0 = 2.72548 \pm 0.00057$ K being the present-day temperature of the CMB [54]. In figure 2 we show the instrumental noise map and the *Planck* Galactic mask employed in the simulations. The noise map corresponds to 7.5 $\mu\text{K}\cdot\text{arcmin}^2$, as expected for the 60-GHz band.

We calculate the likelihoods for the parameters A , l_0 , b_0 and T_0 using the publicly available **COSMOMC** generic sampler package [55–57]. While the monopole T_0 is not an observable of interest in this context, we include it as a free parameter, to verify any degeneracy with the other parameters and for internal consistency checks.

²<http://pla.esac.esa.int/pla/>.

³When we degrade the *Planck* common mask 76 to lower resolutions we apply a threshold of 0.5 for accepting or excluding pixels, so that the exact sky coverage not excluded by each mask (76–78 %) slightly increases at decreasing N_{side} . In the case of the extended masks, typical sky coverage values are 47–48 %.

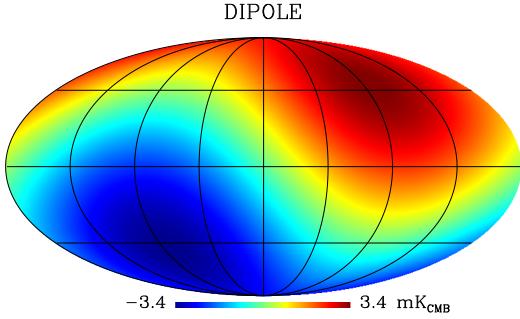


Figure 1. Map of the CMB dipole used in the simulations, corresponding to an amplitude $A = 3.3645 \text{ mK}$ and a dipole direction defined by the Galactic coordinates $b_0 = 48.24^\circ$ and $l_0 = 264.00^\circ$. The map is in Galactic coordinates and at a resolution of $\simeq 3.4 \text{ arcmin}$, corresponding to HEALPix $N_{\text{side}} = 1024$.

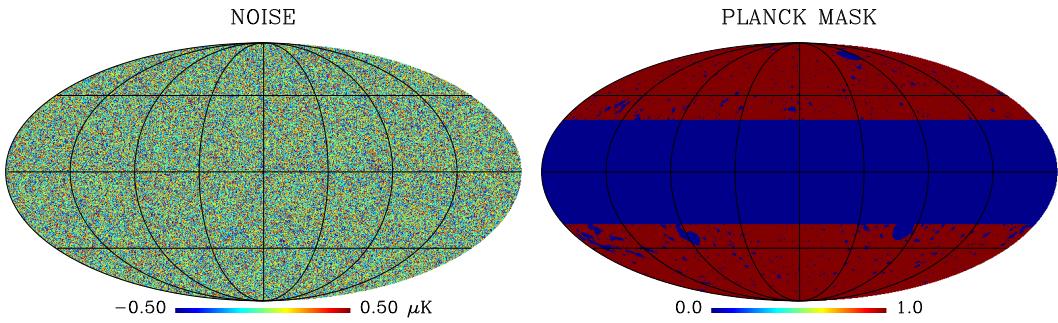


Figure 2. Instrumental noise map and *Planck* Galactic mask (extended to cut out $\pm 30^\circ$ of the Galactic plane) employed in the simulations. The noise map corresponds to $7.5 \mu\text{K}\cdot\text{arcmin}$, as expected for the 60-GHz band. The Map is in Galactic coordinates and at resolution of $\simeq 3.4 \text{ arcmin}$, corresponding to HEALPix $N_{\text{side}} = 1024$.

To probe the dependence of the parameter error estimates on the sampling resolution, we investigate the dipole reconstruction at HEALPix [58] $N_{\text{side}} = 128, 256, 512$, and 1024 , eventually including the noise and the Galactic mask. The reference frequency channel for this analysis is the 60-GHz band. The corresponding likelihoods are collected in appendix A (see figure 15) for the same representative values of N_{side} (see also table 12 for the corresponding 68% confidence levels).

In figure 4 we plot the 1σ uncertainties on the parameter estimates as functions of the HEALPix N_{side} value. We find that the pixelization error due to the finite resolution is dominant over the instrumental noise at any N_{side} . This means that we are essentially limited by the sampling resolution. As expected, the impact of noise is negligible, although the effect of reducing the effective sky fraction is relevant. In fact, the presence of the Galactic mask results in larger errors (for all parameters) and introduces a small correlation between the parameters A and b_0 , as clearly shown in these plots.

The likelihood results for some of the different frequencies under analysis are collected in figures 16 of appendix A (see also table 13 for the 68% confidence levels at the four considered frequencies). Here we keep the resolution fixed at HEALPix $N_{\text{side}} = 1024$ and consider both noise level and choice of Galactic mask. We find that the dipole parameter estimates do not

significantly change among the frequency channels, which is clearly due to the sub-dominant effect of the noise.

As a last test of the ideal case, we compare the dipole parameter reconstruction between the cases of a pure blackbody (BB) spectrum and a BE-distorted spectrum. The comparison of the likelihoods is presented in figure 17 of appendix A (see also table 14 for the corresponding 68% confidence levels). This analysis shows that the parameter errors are not affected by the spectral distortion and that the direction of the dipole is successfully recovered. The difference found in the amplitude value is consistent with the theoretical difference of about 76 nK.

3 Parametric model for potential foreground and calibration residuals in total intensity

In the previous section we showed that in the ideal case of pure noise, i.e., assuming perfect foreground subtraction and calibration (and the absence of systematic effects) in the sky region being analysed, pixel-sampling limitation dominates over noise limitation.

Clearly, specific component-separation and calibration methods (and implementations) introduce specific types of residuals. Rather than trying to accurately characterise them (particularly in the view of great efforts carried out in the last decade for specific experiments and the progress that is expected over the coming years), we implemented a simple toy model to parametrically estimate the potential impact of imperfect foreground subtraction and calibration in total intensity (i.e., in temperature). This includes using some of the *Planck* results and products made publicly available through the PLA.

The PLA provides maps in total intensity (or temperature) at high resolution ($N_{\text{side}} = 2048$) of global foregrounds at each *Planck* frequency (here we use those maps based on the **COMMANDER** method).⁴ It provides also suitable estimates of the zodiacal light emission (ZLE) maps (in temperature) from *Planck*-HFI. Our aim is to produce templates of potential foreground residuals that are simply scalable in amplitude according to a tunable parameter. In order to estimate such emission at CORE frequencies, without relying on particular sky models, we simply interpolate linearly (in logarithmic scale, i.e., in $\log(\nu)$ - $\log(T)$) pixel by pixel the foreground maps and the ZLE maps, and linearly extrapolate the ZLE maps at $\nu < 100$ GHz. We then create a template of signal sky amplitude at each CORE frequency, adding the absolute values in each pixel of these foreground and ZLE maps⁵ and of the CMB anisotropy map available at the same resolution in the PLA (we specifically use that based on **COMMANDER**). Since for this analysis we are not interested in separating CMB and astrophysical emission at $\ell \geq 3$, we then generate templates from these maps, extracting the a_{lm} modes for $\ell \leq 2$ only. These templates are then degraded to the desired resolution. Finally, we generate maps of Gaussian random fields at each CORE frequency, with rms amplitude given by these templates, $T_{\text{amp,for}}$, multiplied by a tunable parameter, E_{for} , which globally characterizes the potential amplitude of foreground residuals after component separation.

⁴Adopting this choice or one of the other foreground-separation methods is not relevant for the present purpose.

⁵Since we are not interested here in the separation of the diffuse Galactic emission and ZLE, this assumption is in principle slightly conservative. In practice, separation methods will at least distinguish between these diffuse components, which are typically treated with different approaches, e.g., analysing multi-frequency maps in the case of Galactic emission, and different surveys (or more generally, data taken at different times) for the ZLE.

Clearly, the choice of reasonable values of E_{for} depends on the resolution being considered (or on the adopted pixel size), with the same value of E_{for} but at smaller pixel size implying less contamination at a given angular scale.

Planck maps reveal, at least in temperature, a greater complexity in the sky than obtained by previous experiments. The large number of frequencies of CORE is in fact designed to accurately model foreground emission components with a precision much better than *Planck*'s. Also, at least in total intensity, ancillary information will come in the future from a number of other surveys, ranging from radio to infrared frequencies.

The target for CORE in the separation of diffuse polarised foreground emission corresponds to $E_{\text{for}} \simeq 0.01$, i.e., to $\simeq 1\%$ precision at the map level for angular scales larger than about 1° (i.e., up to multipoles $\ell \lesssim 200$), where the main information on primordial B -modes is contained, while at larger multipoles the main limitation comes from lensing subtraction and characterization and secondarily through control of extragalactic source contributions. We note also that comparing CMB anisotropy maps available from the PLA at $N_{\text{side}} = 2048$ derived with four different component-separation methods and degraded to various resolutions, shows that the rms of the six difference maps does not scale strongly with the adopted pixel size, at least if we exclude regions close to the Galactic plane. For example, outside the *Planck* common mask 76, if we pass from $N_{\text{side}} = 2048$ to $N_{\text{side}} = 256$ or 64, i.e., increasing the pixel linear size by a factor of 8 or 32 (with the exception of the comparison of SEVEM versus SMICA), the rms values of the cross-comparisons range from about $8\text{--}9\,\mu\text{K}$ to about $3\text{--}5\,\mu\text{K}$, i.e., a decreases by a factor of only about 2.5. This suggests that, at least for temperature analyses, the angular scale adopted to set E_{for} is not so critical.

Data calibration represents one of the most delicate aspects of CMB experiments. The quality of CMB anisotropy maps does not rely on absolute calibration of the signal (as it would, for example, in experiments dedicated to absolute measurements of the CMB temperature, i.e., in the direct determination of the CMB spectrum). However, the achievement of very high accuracy in the relative calibration of the maps (sometimes referred to as absolute calibration of the anisotropy maps), as well as the inter-frequency calibration of the maps taken in different bands, is crucial for enabling the scientific goals of CMB projects. Although this calibration step could in principle benefit from the availability of precise instrumental reference calibrators (implemented for example in FIRAS [59] and foreseen in PIXIE [60], or — but with much less accurate requirements — in *Planck*-LFI [61]), this is not necessary for anisotropy experiments, as shown for example by WMAP and *Planck*-HFI. This represents a huge simplification in the design of anisotropy experiments with respect to absolute temperature ones. *Planck* demonstrated the possibility to achieve relatively calibration of anisotropy data at a level of accuracy of about 0.1% up to about 300 GHz, while recent analyses of planet flux density measurements and modelling [62] indicate the possibility to achieve a calibration accuracy of $\simeq 1\%$ even above 300 GHz, with only moderate improvements over what is currently realised.

The goal of CORE is to achieve a calibration accuracy level around 0.01%, while the requirement of 0.1% is clearly feasible on the basis of current experiments, with some possible relaxation at high frequencies. Methods for improving calibration are fundamental in astrophysical and cosmological surveys, and clearly critical in CMB experiments. In principle, improvements in various directions can be pursued: from a better characterization of all instrument components to cross-correlation between different CMB surveys; from the implementation of external precise artificial calibration sources to the search for a better characterization (and increasing number) of astronomical calibration sources; and, in general, with the improvement of data analysis methods.

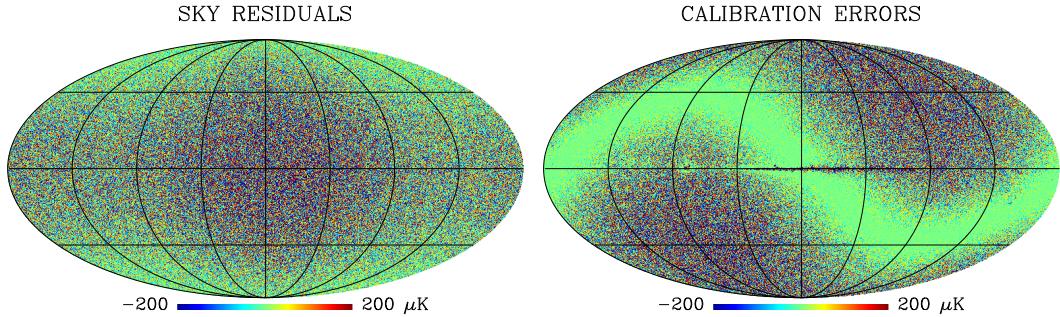


Figure 3. Sky residual and calibration error maps (in Galactic coordinates) in the 60-GHz band employed in the simulations. Their amplitudes correspond to the pessimistic case, $E_{\text{for}} = 0.64$ and $E_{\text{cal}} = 0.064$, for maps at resolution HEALPix $N_{\text{side}} = 1024$.

To parametrically model potential residuals due to imperfect calibration we follow an approach similar to that described above for foreground contamination. We note that calibration uncertainty implies an error proportional to the global effective (anisotropy in our case) signal. We therefore produce templates as described above, but do so by adding the foreground, ZLE, and CMB anisotropy maps, keeping their signs and maintaining all the a_{lm} modes contained in the maps. The absolute values of these templates are then multiplied by a tunable parameter, E_{cal} (possibly dependent on frequency), which globally characterizes the amplitude of potential residuals arising from imperfect calibration. These are then used to define the pixel-by-pixel rms amplitudes, which are adopted to construct maps, $T_{\text{res,cal}}$, of Gaussian random fields at each CORE frequency.

In fact, we might also expect calibration errors to affect the level of foreground residuals. Hence, as a final step, we include in the model a certain coupling between the two types of residuals. At each frequency, we multiply the above simulated maps of foreground residuals by $(1 + T_{\text{res,cal}}/T_{\text{amp,for}})$.

4 The CMB dipole: forecasts for CORE including potential residuals

We now extend the analysis presented in section 2 by including two sources of systematic effects, namely calibration errors and sky foreground residuals. We consider two pairs of calibration uncertainty and sky residuals (parameterised by $E_{\text{for}} = 0.04$ and $E_{\text{cal}} = 0.004$, and by $E_{\text{for}} = 0.64$ and $E_{\text{cal}} = 0.064$) at $N_{\text{side}} = 1024$ in order to explore different resolutions through pixel degradation. Rescaled to $N_{\text{side}} = 64$, the two cases correspond to a set-up respectively better and worse by a factor of 4 with respect to the case $E_{\text{cal}} = 10^{-3}$ and $E_{\text{for}} = 10^{-2}$.

In figure 3 we display the maps used in the simulations (for the 60-GHz band). The amplitudes correspond to the worse expected case; the most optimistic case is not shown, since the amplitude is just rescaled by a factor 16. The corresponding likelihood plots and 68% confidence levels are collected in appendix A.

We find that the impact of systematic effects on the parameter errors is negligible. In fact, as shown in figure 4, calibration errors and sky residuals do not noticeably worsen the 1σ uncertainty at any sampling resolution. Furthermore, the frequency analysis confirms that the impact of systematic effects is not relevant in any of the bands under consideration (from 60 to 220 GHz).

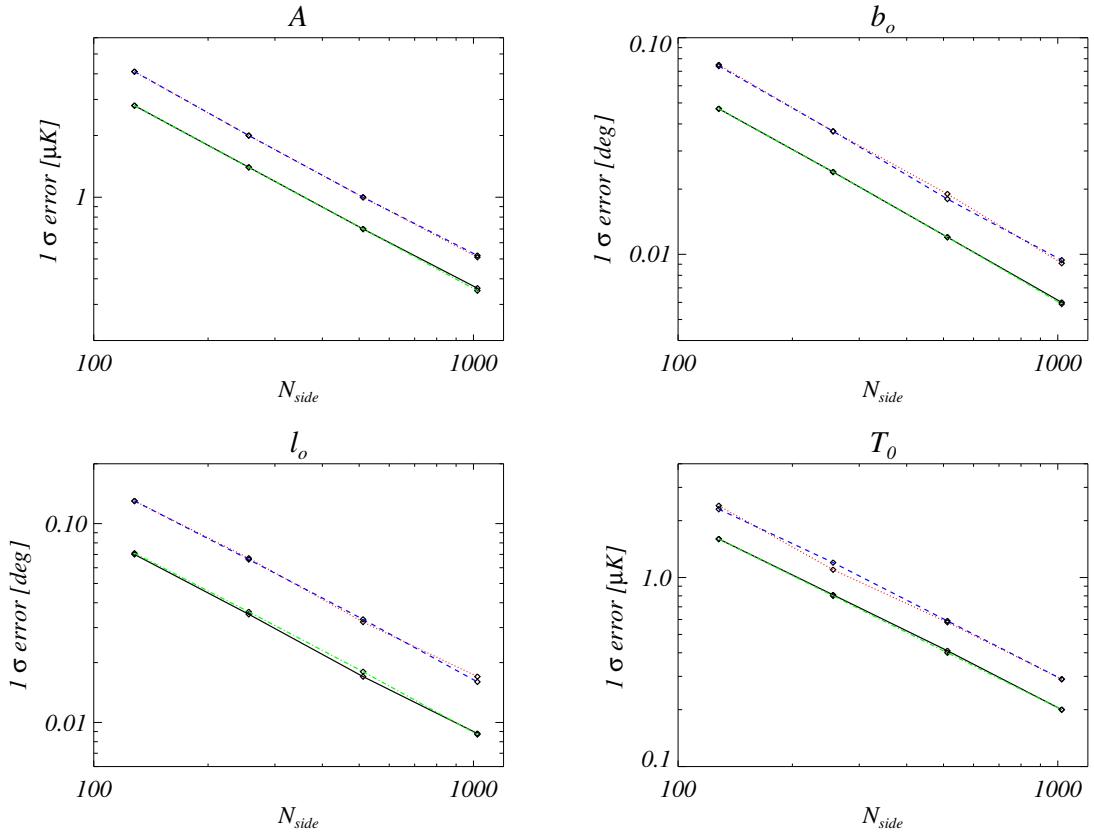


Figure 4. 1σ errors as function of HEALPix N_{side} values for the parameters A , b_0 , l_0 , and T_0 : dipole-only (solid black line); dipole+noise (green dot-dashed line); dipole+noise+mask (red dotted line); and dipole+noise+mask+systematics (blue dashed line). The chosen frequency channel is 60 GHz and the noise map corresponds to $7.5 \mu\text{K}\cdot\text{arcmin}^2$. The adopted mask is the *Planck* Galactic mask extended to cut out $\pm 30^\circ$ of the Galactic plane. The systematics correspond to the pessimistic expectation of calibration errors and sky (foreground, etc.) residuals. Notice that the pixelization error, due to the finite map resolution, is dominant over the noise for any N_{side} . While the impact of noise and systematics is negligible, we find that the effect of reducing the effective sky fraction is important.

While the effect of the systematics studied here on the *precision* of the parameter reconstruction is negligible, we find instead that they may have a moderate impact on the *accuracy*, introducing a bias in the central values of the estimates. Nonetheless, the bias is usually buried within the 1σ error, with the marginal exception of the estimate of l_0 for the 220-GHz band (in the case of pessimistic systematics).

In conclusion, our results show that the dipole recovery (in both amplitude A and direction angles b_0 and l_0) is completely dominated by the sky sampling resolution. We find that: the noise impact is negligible; the reduction of the sky fraction due to the presence of the Galactic mask impacts on the parameter error amplitude by increasing the 1σ errors on A , b_0 and l_0 by a factor of about 1.5, 1.6, and 1.9, respectively; and the effect of systematics slightly worsens the accuracy of the MCMC chain without affecting the error estimate.

The main point of our analysis is that, in order to achieve an increasing precision in the dipole reconstruction, high resolution measurements are required, in particular when a sky

mask has to be applied. This is especially relevant for dipole spectral distortion analyses, based on the high-precision, multi-frequency observations that are necessary to study the tiny signals expected.

5 Measuring Doppler and aberration effects in different maps

5.1 Boosting effects on the CMB fields

As discussed in the previous sections, a relative velocity between an observer and the CMB rest frame induces a dipole in the CMB temperature through the Doppler effect. The CMB dipole, however, is completely degenerate with an *intrinsic* dipole, which could be produced by the Sachs-Wolfe effect at the last-scattering surface due to a large-scale dipolar Newtonian potential [21]. For Λ CDM such a dipole should be of order of the Sachs-Wolfe plateau amplitude (i.e., 10^{-5}) [63, 64], nevertheless the dipole could be larger in the case of more exotic models. In addition to the dipole, a moving observer will also see velocity imprints at $\ell > 1$ in the CMB due to Doppler and aberration effects [30, 31]. Such effects can be measured as correlations among different ℓ s, as has been proposed in refs. [32, 33, 65] and subsequently demonstrated in ref. [34].

The aberration effect changes the arrival direction of photons from \hat{n}' to \hat{n} , which, at linear order in β , is completely degenerate with a lensing dipole. The Doppler effect modulates the CMB (an effect that is partly degenerate with an intrinsic CMB dipole⁶) changing the specific intensity I' in the CMB rest frame to the intensity I in the observer's frame⁷ by a multiplicative, direction-dependent factor as [30, 66]

$$I'(\nu', \hat{n}') = I(\nu, \hat{n}) \left(\frac{\nu'}{\nu} \right)^3, \quad (5.1)$$

where

$$\nu = \nu' \gamma (1 + \vec{\beta} \cdot \hat{n}'), \quad \hat{n} = \frac{\hat{n}' + [\gamma \beta + (\gamma - 1)(\hat{n}' \cdot \hat{\beta})] \hat{\beta}}{\gamma(1 + \vec{\beta} \cdot \hat{n}')}, \quad (5.2)$$

with $\gamma \equiv (1 - \vec{\beta}^2)^{-1/2}$. The temperature and polarization fields $X(\hat{n})$ in the CMB rest frame (where X stands for T , E or B) are similarly transformed as

$$X'(\hat{n}') = X(\hat{n}) \gamma (1 - \vec{\beta} \cdot \hat{n}). \quad (5.3)$$

Decomposing eq. (5.3) into spherical harmonics leads to an effect in the multipole ℓ of order β^ℓ . Although this effect is dominant in the dipole, it also introduces a small, non-negligible correction to the quadrupole, with a different frequency dependence, due to the conversion of intensity to temperature [67–70]. In addition, both aberration and Doppler effects couple multipoles ℓ to $\ell \pm n$ [65, 71]. This coupling is largest in the correlation between ℓ and $\ell \pm 1$ [30, 32, 33], which was measured by *Planck* at 2.8 and 4.0σ significance for the aberration and Doppler effects, respectively [34]. These $\mathcal{O}(\beta)$ couplings are present on all scales and the measurability of aberration is mostly limited by cosmic variance, which

⁶It has been shown in [21] that, in the Gaussian case, an intrinsic large scale dipolar potential exactly mimics on large scales a Doppler modulation.

⁷In this section we will use primes for the CMB frame and non-primes for the observer frame, following ref. [34].

constrains our ability to assume fully uncorrelated modes for $\ell \neq \ell'$. Hence, in order to improve their measurement, it is important to have as many modes as possible, which drives us to cosmic-variance-limited measurements of temperature and polarization up to very high ℓ_{\max} and coverage of a large fraction of the sky f_{sky} . CORE probes a larger ℓ_{\max} and covers a larger effective f_{sky} than *Planck* (as the extra frequency channels and the better sensitivity allow for an improved capability in doing component separation), hence it should achieve a detection of almost 13σ even with a 1.2-m telescope, as shown below.

As discussed in ref. [30], upon a boost of a CMB map X , the $a_{\ell m}$ coefficients of the spherical harmonic decomposition transform as

$$a_{\ell m}^X = \sum_{\ell'=0}^{\infty} {}_s K_{\ell' \ell m} a_{\ell' m}'^X, \quad (5.4)$$

where s indicates the spin of the quantity X . For scalars (such as the temperature), $s = 0$, while for spin-2 quantities (such as the polarization), $s = 2$.

The kernels ${}_s K_{\ell' \ell m}$ in general cannot be computed analytically and their numerical computation is not trivial, since this involves highly oscillatory integrals [71]. However, efficient methods using an operator approach in harmonic space have been developed [72], although for our estimates more approximate methods will suffice. It was shown in refs. [65, 72] that the kernels can be well approximated by Bessel functions as follows:

$$\begin{aligned} K_{(\ell-n)\ell m}^X &\simeq J_n \left(-2\beta \left[\prod_{k=0}^{n-1} [(\ell-k) {}_s G_{(\ell-k)m}] \right]^{1/n} \right); \\ K_{(\ell+n)\ell m}^X &\simeq J_n \left(2\beta \left[\prod_{k=1}^n [(\ell+k) {}_s G_{(\ell+k)m}] \right]^{1/n} \right). \end{aligned} \quad (5.5)$$

Here

$${}_s G_{\ell m} \equiv \sqrt{\frac{\ell^2 - m^2}{4\ell^2 - 1} \left[1 - \frac{s^2}{\ell^2} \right]}, \quad (5.6)$$

and $n \geq 1$ (where n is the difference in multipole between a pair of coupled multipoles, namely ℓ and $\ell \pm n$). It is also assumed that $\beta \ll 1$, although the formula above can be generalised to large β [65, 72]. These kernels couple different multipoles so that, by Taylor expanding, we find $\langle a_{\ell m} a_{(\ell+n)m}^* \rangle = \mathcal{O}(\beta\ell)^n$. For $\ell \ll 1/\beta$, the most important couplings are between neighbouring multipoles, ℓ and $\ell \pm 1$ (e.g. [30]). One may wonder about the importance of the couplings between non-neighbouring multipoles, i.e., ℓ and $\ell \pm n$, for $\ell \gtrsim 1/\beta$. However, quite surprisingly, for $\ell \gg 1/\beta$ we find that: (1) in the $(\ell, \ell \pm 1)$ correlations, terms that are higher order in $\beta\ell$ are negligible [65, 71]; and (2) most of the correlation seems to remain in the $(\ell, \ell \pm 1)$ coupling. For these reasons, from here onwards, we will ignore terms that are higher order in β and couplings between non-neighbouring multipoles (i.e., $n > 1$).

In order to measure deviations from isotropy due to the proper motion of the observer, we therefore compute the off-diagonal correlations $\langle a_{\ell m}^X a_{(\ell+1)m}^{X*} \rangle$. Assuming that in the rest frame the Universe is statistically isotropic and that parity is conserved, then in the boosted frame, for $\ell' = \ell + 1$, we find that (see refs. [30, 32, 33])

$$a_{\ell m}^X \simeq c_{\ell m}^- a_{(\ell-1)m}'^X + c_{\ell m}^+ a_{(\ell+1)m}'^X, \quad (5.7)$$

where

$$c_{\ell m}^+ = \beta(\ell + 2 - d)s G_{(\ell+1)m}, \quad c_{\ell m}^- = -\beta(\ell - 1 + d)s G_{\ell m}, \quad (5.8)$$

and d parametrizes the Doppler effect of dipolar modulation. It then follows that

$$\langle a_{\ell m}^X a_{(\ell+1)m}^{Y*} \rangle = \beta [(\ell + 2 - d) {}_{s_X}G_{(\ell+1)m} C_{\ell+1}^{XY} - (\ell + d) {}_{s_Y}G_{(\ell+1)m} C_{\ell}^{XY}] + O(\beta^2). \quad (5.9)$$

For $\ell \gtrsim 20$, we have ${}_2G_{\ell m} \simeq {}_0G_{\ell m}$. As will be shown, large scales are not important for measuring the boost, and thus it is not important to keep the indication of the spin. Thus from here onwards, we will drop s . The above equation reduces to

$$\langle a_{\ell m}^X a_{(\ell+1)m}^{Y*} \rangle = \beta G_{(\ell+1)m} [(\ell + 2 - d) C_{\ell+1}^{XY} - (\ell + d) C_{\ell}^{XY}] + O(\beta^2), \quad (5.10)$$

where the angular power spectra C_{ℓ}^{XY} are measured in the CMB rest frame. For the CMB temperature and polarization, $d = 1$, as observed from eqs. (5.1)–(5.2). In this case, no mixing of E - and B -polarization modes occurs, not even in higher orders in β [65, 72]. However, for $d \neq 1$, the coupling is non-zero already at first order in β [30, 72]. Maps estimated from spectra that are not blackbody have different Doppler coefficients,⁸ as we discuss in the next subsection.

Note that in practice one never measures temperature and polarization anisotropies directly, instead one measures anisotropies in *intensity* and then converts this to temperature and polarization. This distinction (though perhaps seeming trivial) is relevant for the Doppler effect, which induces a dipolar modulation of the CMB anisotropies, appearing with frequency-dependent factors [34, 73]. In particular such factors were shown to be proportional to a Compton y -type spectrum (exactly like the quadrupole correction [67–70] and therefore degenerate with the tSZ effect); they are measurable in the *Planck* maps at about 12σ and in the CORE maps even at 25 – 60σ [73], depending on the template that is used for contamination due to the tSZ effect. Such S/N ratios are much larger than those that can be obtained in temperature and polarization and so, at first sight, they may appear to represent a better way to measure the boosting effects. However, the peculiar frequency dependence is strictly a consequence of the intensity-to-temperature (or intensity-to-polarization) conversion and thus agnostic to the source of the dipole [34, 73] (i.e., whether it is from our peculiar velocity or is an intrinsic CMB dipole). For this reason we focus on the frequency-*independent* part of the dipolar modulation signal in eq. (5.10) (with $d = 1$), which is unlikely to be caused by an intrinsically large CMB dipole (see ref. [21] for details), in our forecast.

5.2 Going beyond the CMB maps

Since CORE will also measure the thermal Sunyaev-Zeldovich effect, the CIB, and the weak lensing signal over a wide multipole range, it is interesting to examine if these maps could also be used to measure the aberration and Doppler couplings.

The intensity of a tSZ Compton- y map is given by

$$I'_{tSZ}(\nu') = y \cdot g \left(\frac{h\nu'}{k_B T_0} \right) K(\nu'), \quad (5.11)$$

where $g(x') = x' \coth(x'/2) - 4$, $K(\nu')$ is the conversion factor that derives from setting $T = T_0 + \delta T$ in the Planck distribution and expanding to first order in δT , and $x' \equiv h\nu'/k_B T_0$

⁸Note that the kernel defined as in eq. (5.4) for $d \neq 1$ can be obtained from ${}_sK_{\ell'\ell m}$ using recursions [72].

(T_0 being the present temperature of the CMB). Explicitly $K(\nu')$ is given by

$$K(\nu') = \frac{2 h \nu'^3}{c^2} \frac{x' \exp(x')}{(\exp(x') - 1)^2}. \quad (5.12)$$

A boosted observer will see an intensity as defined in eq. (5.1). Such intensity, expanded at first order in β , will contain Doppler couplings with a non-trivial frequency dependence, similarly to what happens in the case of CMB fluctuations, where frequency-dependent boost factors are generated, as discussed in the previous subsection. For simplicity we only analyse the couplings that retain the same frequency dependence of the original tSZ signal, which come from aberration,⁹ and so we here set $d = 0$ in eq. (5.10).

For the intensity of the CIB map (see section 6.2 for further details), we assume the template obtained by ref. [42],

$$I'_{\text{CIB}} \propto \nu'^{0.64} \frac{\nu'^3}{\exp\left[\frac{h\nu'}{k_B 18.5\text{K}}\right] - 1}. \quad (5.13)$$

At low frequencies, the intensity scales as

$$I'_{\text{CIB}} = A_{\text{CIB}} \nu'^{2.64}, \quad (5.14)$$

where A_{CIB} is a constant related to the amplitude. In the boosted frame and to lowest order in β , we find that

$$I_{\text{CIB}}(\nu) = \left(\frac{\nu}{\nu'}\right)^3 A'_{\text{CIB}} \nu'^{2.64} \simeq A'_{\text{CIB}} [\gamma(1 - \vec{\beta} \cdot \hat{n})]^{-0.36} \nu^{2.64}. \quad (5.15)$$

Therefore, the boosted amplitude is $A_{\text{CIB}} \equiv A'_{\text{CIB}} / [\gamma(1 - \vec{\beta} \cdot \hat{n})]^{0.36}$, which implies $d = 0.36$. Note that in this case, since we work in a low-frequency approximation (relative to the peak of the CIB at around 3000 GHz), we do not have any frequency-dependent boost factors.

The CMB weak lensing maps can also be used to measure the boost. However, since the estimation of the weak lensing potential involves 4-point correlation functions of the CMB fields, the boost effect is more complex to estimate; hence we leave this analysis for a future study.

5.3 Estimates of the Doppler and aberration effect

For full-sky experiments, it has been shown in ref. [30] that, under a boost, the corrections to the power spectra are $\mathcal{O}(\beta^2)$, whereas for experiments with partial sky coverage there can be an $\mathcal{O}(\beta)$ correction [77–79]. Nevertheless, even for the partial-sky case, this correction to C_ℓ^{XY} would only propagate at $\mathcal{O}(\beta^2)$ in the correlations above. In what follows, we will neglect the effect of the sky coverage in the boost corrections. Also, since we will be restricting ourselves to $\mathcal{O}(\beta)$ effects, from here onwards we will drop $\mathcal{O}(\beta^2)$ from the equations.

⁹Also, sub-leading contributions, namely the kinetic Sunyaev-Zeldovich effect [74] and changes in the tSZ signal induced by the observer motion relative to the CMB rest frame [35], as well as relativistic corrections [75, 76], are specific to each particular cluster. Their inclusion could be considered in more detailed predictions in future, but represent higher-order corrections for the present study.

For the CMB fields, as it was shown in refs. [33, 65], that the fractional uncertainty in the estimator of $\langle a_{\ell m}^X a_{(\ell+1)m}^{Y*} \rangle$ is given by

$$\frac{\delta\beta}{\beta} \Big|_{XY} \simeq \left[\sum_{\ell} \sum_{m=-\ell}^{\ell} \frac{\langle a_{\ell m}^X a_{(\ell+1)m}^{Y*} \rangle^2}{\mathfrak{C}_{\ell}^{XX} \mathfrak{C}_{\ell+1}^{YY}} \right]^{-1/2} \quad (5.16)$$

(see also ref. [80]). Here, $\mathfrak{C}_{\ell}^{XX} \equiv (C_{\ell}^{XX} + N_{\ell,\text{total}}^{XX})/\sqrt{f_{\text{sky}}}$, where f_{sky} is the fraction of the sky covered by the experiment and $N_{\ell,\text{total}}^{XX}$ is the effective noise level on the map X . Thus \mathfrak{C}_{ℓ}^{XX} represents the sum of instrumental noise and cosmic variance. The effective noise is obtained by taking the inverse of the sum over the different channels i of the inverse of the individual $N_{\ell,i}^2$ [65],

$$N_{\ell,\text{total}} = \left[\sum_i^{\text{nchannel}} \frac{1}{N_{\ell,i}^2} \right]^{-1/2}. \quad (5.17)$$

The noise in each channel is given by a constant times a Gaussian beam characterised by the beam width θ_{FWHM} :

$$N_{\ell,i}^X = (\sigma^X)^2 \exp \left[\frac{\ell(\ell+1)\theta_{\text{FWHM}}^2}{8 \ln 2} \right], \quad (5.18)$$

where σ^X is the noise in $\mu\text{K}\cdot\text{arcmin}$ for the map X .

For the tSZ signal, we assume as a fiducial spectrum the one obtained in ref. [81] (slightly extrapolated to higher ℓ s). For the forecast noise spectrum we use the estimates obtained in ref. [82] using the NILC component separation technique (see figure 14 therein), where it was shown that residual foreground contamination is a large fraction of the total noise. For the CIB signal, we use the spectra obtained in ref. [83]; for the noise, we rely on the simulations carried out in ref. [4]. We also make the conservative assumption that the different channels of the CIB are 100% correlated. Since different channels pick up different redshifts, effectively the correlation is not going to be total and some extra signal can be obtained from multiple channels; however, since this makes the analysis much more complex (due to the need to have all the covariance matrices) and since the CIB turns out not to be promising for measuring aberration (see figure 5), we neglect these corrections.

We computed eq. (5.16) for the different maps of different experiments. We compared the detection potentials of CORE (see table 1) with those expected from both *Planck* and LiteBIRD [36]. For the *Planck* specifications, we use the values of the 2015 release, while the LiteBIRD specifications used in this analysis are listed in table 2.

In figure 5 we show the precision that could be reached by an ideal experiment with $f_{\text{sky}} = 1$ and limited by cosmic variance only. We show the results for: the range $\ell \in [2, \ell_{\text{max}}]$; the range $\ell \in [\ell_{\text{min}}, 5000]$; and for individual ℓ bins of width $\Delta\ell = 200$. The signal-to-noise ratios in the tSZ and CIB maps are considerably lower than in the CMB maps, which is due to the fact that the spectra are smoother, as explained later. For instance, for $\ell_{\text{max}} = 4000$, in the *TT* and *EE* maps separately we have $S/N > 16$, whereas in tSZ and in CIB we have $S/N \simeq 1$.

In figure 6 and table 3 we summarise our forecasts for CORE and compare them with both *Planck* and LiteBIRD forecasts. These results differ from the ideal case due to the inclusion of instrumental noise, foreground contamination (in the case of tSZ) and $f_{\text{sky}} \neq 1$. In the last panel we also show the total precision by combining all temperature and polarization channels assuming a negligible correlation among them (which was shown in ref. [33] to be a

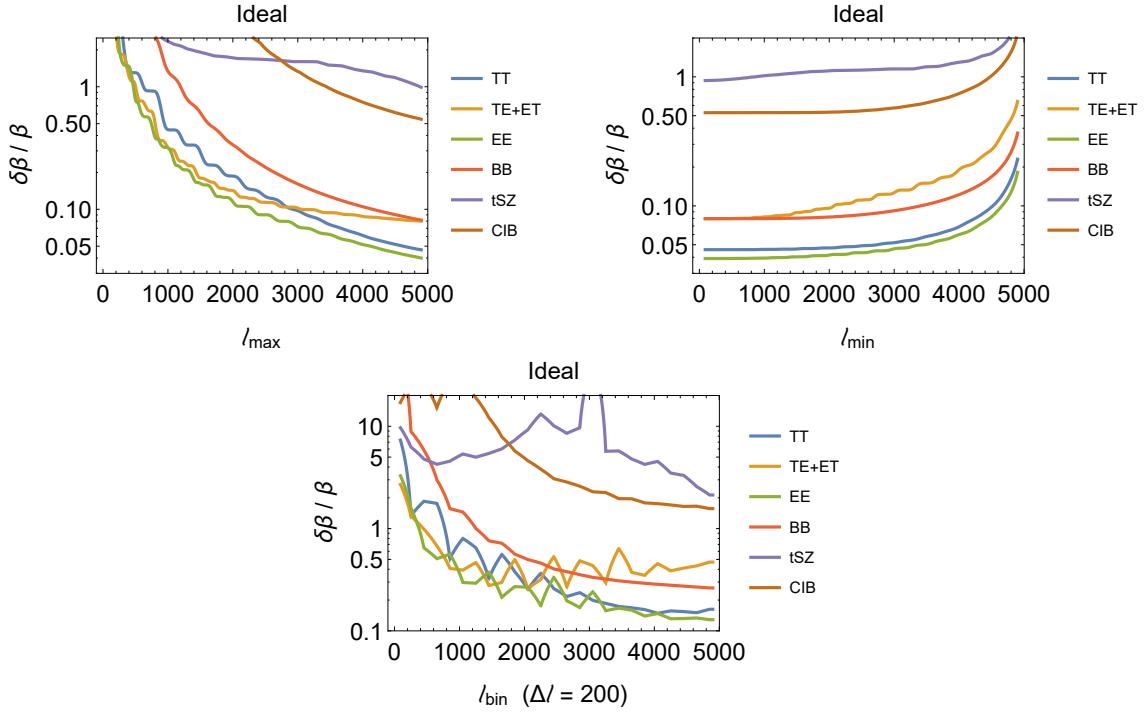


Figure 5. Achievable precision in estimating the velocity through aberration and Doppler effects in an ideal experiment (with $f_{\text{sky}} = 1$ and limited by cosmic variance only) for different maps. *Left:* as a function of ℓ_{\max} . *Right:* as a function of ℓ_{\min} (with fixed $\ell_{\max} = 5000$). *Bottom:* for individual bins with $\Delta\ell = 200$. We see that: (i) the first hundred ℓ s are not important for achieving a high S/N; and (ii) the non-CMB diffuse maps exhibit low precision and are not very useful for measuring β . Note that for simplicity we have assumed no primordial B -modes (our constraints are very weakly sensitive to this choice).

good approximation). Note also that the TE and ET correlation functions were shown to be independent in ref. [33] and both carry the same S/N. So we usually present the combined S/N for $TE + ET$, which is $\sqrt{2}$ times their individual S/N values.

As a side note, since the estimators for $\langle a_{\ell m}^X a_{(\ell+1)m}^{Y*} \rangle$ involve a sum over all ℓ s and m s and since m enters through $G_{\ell m}$ only, it is useful to use the following approximations, which are valid to very good accuracy for $\ell \gtrsim 20$ [65, 73]:

$$\sum_m G_{\ell,m} = 0.39(2\ell + 1); \quad \sum_m [G_{\ell,m}]^2 = 0.408^2(2\ell + 1). \quad (5.19)$$

Although we did not use these approximations in our results, they yield up to 1%-level accuracy and by allowing the sum over m s to be removed, they significantly simplify the calculation of the estimators.

The achievable precision in β through this method depends strongly on the shape of the power spectrum — strongly varying spectra give much lower uncertainties compared to smooth spectra. For instance, for the tSZ and CIB maps, many modes are in the cosmic-variance-limited regime, thus one might think that they would yield a good measurement of β . However, since their C_{ℓ} s are smooth functions of ℓ , they do not carry much information on the boost. To understand this and gain some insight, we rewrite eq. (5.9) by approximating

Channel [GHz]	Beam [arcmin]	ΔT [$\mu\text{K}\cdot\text{arcmin}$]	ΔP [$\mu\text{K}\cdot\text{arcmin}$]
40	108	42.5	60.1
50	86	26	36.8
60	72	20	28.3
68.4	63	15.5	21.9
78	55	12.5	17.7
88.5	49	10	14.1
100	43	12	17.
118.9	36	9.5	13.4
140	31	7.5	10.6
166	26	7	9.9
195	22	5	7.1
234.9	18	6.5	9.2
280	37	10	14.1
337.4	31	10	14.1
402.1	26	19	26.9

Table 2. LiteBIRD specifications used in this analysis.

$C_{\ell+1}$ as $C_\ell + dC_\ell/d\ell$ and adding the approximation that $dC_\ell/d\ell \ll C_\ell$ (note, however, that $\ell dC_\ell/d\ell$ could be comparable to C_ℓ at small scales). We thus find that

$$\sum_m \left\langle a_{\ell m}^X a_{(\ell+1)m}^{Y*} \right\rangle = 0.39(2\ell+1)\beta \left[(2-2d)C_\ell^{XY} - (\ell+d)\frac{dC_\ell^{XY}}{d\ell} \right]. \quad (5.20)$$

Assuming the cosmic-variance dominated regime (i.e., $\mathfrak{C}_\ell^{XX} \simeq C_\ell^{XX}$) for $\ell \gtrsim 20$ and putting $X = Y$, we find that

$$\left. \frac{\delta\beta}{\beta} \right|_{XX} \simeq \frac{1}{0.408\beta} \left[\sum_\ell (2\ell+1) \left[(2-2d) - \ell \left(1 - \frac{C_{\ell+1}^{XX}}{C_\ell^{XX}} \right) \right]^2 \right]^{-\frac{1}{2}}. \quad (5.21)$$

For the TE case, the formula is less useful. For the CMB temperature and polarization ($d = 1$), only the derivative term survives:

$$\left. \frac{\delta\beta}{\beta} \right|_{XX=TT,EE,BB} \simeq \frac{1}{0.408\beta} \left[\sum_\ell (2\ell+1) \left[\frac{d \ln C_\ell^{XX}}{d \ln \ell} \right]^2 \right]^{-\frac{1}{2}}. \quad (5.22)$$

Note that for the CIB the precision is smaller than for the CMB temperature and polarization, not only because the spectra are smoother, but also because there is a partial cancellation between the two terms in the summand of eq. (5.21).

In this analysis we relied only on the diffuse background components of the measured maps. Aberration and Doppler effects can in principle also be detected using point sources, since the boosting effects will change both their number counts, angular distribution, and redshift. For the upcoming CMB experiments, however, the number density of point sources is probably insufficient for a significant signal, since one needs more than about 10^6 objects to have a detection at greater than 1σ [84].

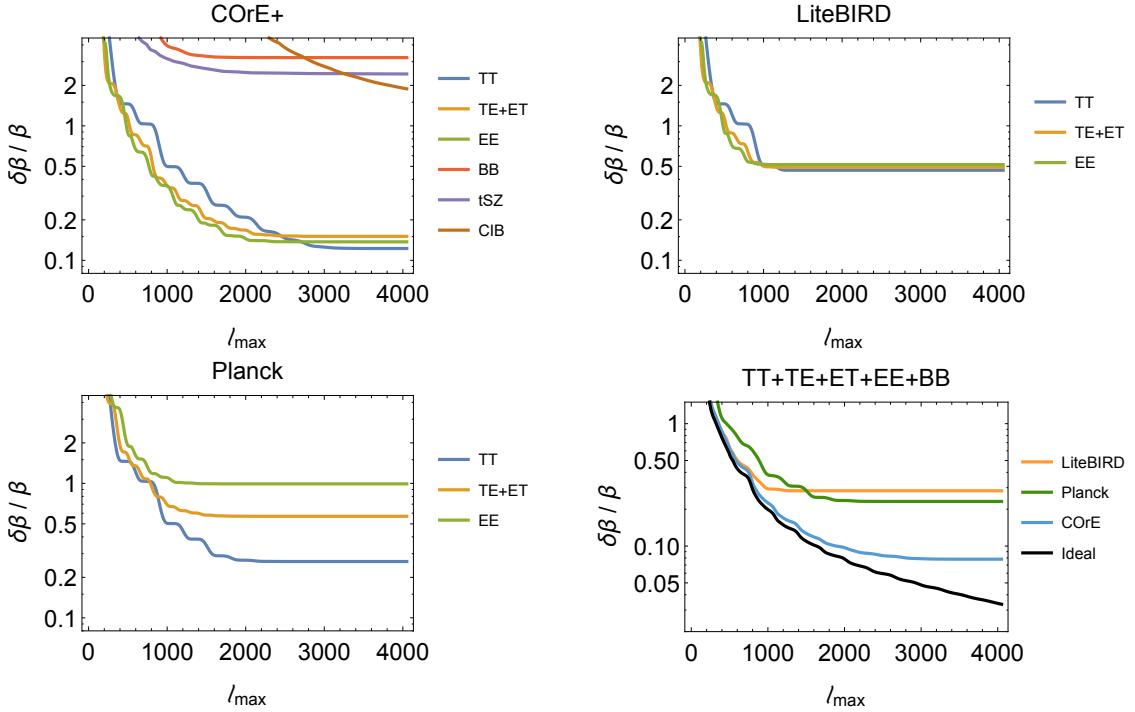


Figure 6. Similar to the left panel of figure 5 but for realistic experiments (described in detail in table 1) and assuming $f_{\text{sky}} = 0.8$. In the bottom right panel we compare the total precision after combining all temperature and polarization maps, including also the case of an ideal experiment (no instrumental noise and $f_{\text{sky}} = 1$).

6 Differential approach to CMB spectral distortions and the CIB

Using the complete description of the Compton-Getting effect [85] we compute full-sky maps of the expected effect at desired frequency. We start discussing the frequency dependence of the dipole spectrum [43, 44] and then extend the analysis beyond the dipole.

6.1 The CMB dipole

The dipole amplitude is directly proportional to the first derivative of the photon occupation number, $\eta(\nu)$, which is related to the thermodynamic temperature, $T_{\text{therm}}(\nu)$, i.e., to the temperature of the blackbody having the same $\eta(\nu)$ at the frequency ν , by

$$T_{\text{therm}} = \frac{h\nu}{k_B \ln(1 + 1/\eta(\nu))}. \quad (6.1)$$

The difference in T_{therm} measured in the direction of motion and in the perpendicular direction is given by [43]:

$$\Delta T_{\text{therm}} = \frac{h\nu}{k} \left\{ \frac{1}{\ln[1 + 1/\eta(\nu)]} - \frac{1}{\ln[1 + 1/\eta(\nu(1 + \beta))]} \right\}, \quad (6.2)$$

which, to first order, can be approximated by:

$$\Delta T_{\text{therm}} \simeq -\frac{x\beta T_0}{(1 + \eta)\ln^2(1 + 1/\eta)} \frac{d\ln\eta}{d\ln x}, \quad (6.3)$$

where $x \equiv h\nu/kT_0$ is the dimensionless frequency.

Experiment	Channel	θ_{FWHM}	σ^T	S/N	S/N	S/N	S/N
	[GHz]	[arcmin]	[$\mu\text{K}\cdot\text{arcmin}$]	TT	$TE + ET$	EE	Total
<i>Planck</i>	(all)	$\simeq 5.5$	$\simeq 13$	3.8	1.7	1.0	4.3
LiteBIRD	(all)	$\simeq 19$	$\simeq 1.7$	2.0	1.8	1.8	3.3
CORE	60	17.87	7.5	2.1	1.9	1.8	3.4
	70	15.39	7.1	2.5	2.4	2.2	4.1
	80	13.52	6.8	2.8	2.8	2.6	4.8
	90	12.08	5.1	3.5	3.4	3.3	5.9
	100	10.92	5	3.9	3.7	3.7	6.5
	115	9.56	5	4.3	4.2	4.2	7.3
	130	8.51	3.9	5.1	4.9	5.	8.6
	145	7.68	3.6	5.7	5.3	5.5	9.5
	160	7.01	3.7	6.1	5.6	5.8	10.1
	175	6.45	3.6	6.5	5.8	6.1	10.7
	195	5.84	3.5	7.1	6.1	6.5	11.4
	220	5.23	3.8	7.5	6.3	6.7	11.9
	255	4.57	5.6	7.5	5.9	6.2	11.4
	295	3.99	7.4	7.5	5.7	5.8	11.
	340	3.49	11.1	7.	5.1	4.9	9.9
	390	3.06	22	5.8	3.8	3.1	7.6
	450	2.65	45.9	4.5	2.3	1.4	5.3
	520	2.29	116.6	2.9	1.	0.3	3.1
	600	1.98	358.3	1.4	0.3	0.	1.4
	(all)	$\simeq 4.5$	$\simeq 1.4$	8.2	6.6	7.3	12.8
Ideal ($\ell_{\text{max}} = 2000$)	(all)	0	0	5.3	7.1	8.7	12.7
Ideal ($\ell_{\text{max}} = 3000$)	(all)	0	0	10	9.8	14	21
Ideal ($\ell_{\text{max}} = 4000$)	(all)	0	0	16	11.4	19	29
Ideal ($\ell_{\text{max}} = 5000$)	(all)	0	0	22	12.6	26	38

Table 3. *Aberration and Doppler effects with CORE.* We assume $f_{\text{sky}} = 0.8$ for all experiments (and $f_{\text{sky}} = 1$ in the ideal cases) in order to make comparisons simpler. For CORE we assume the 1.2-m telescope configuration, but with extended mission time to match the 1.5-m noise in $\mu\text{K}\cdot\text{arcmin}$. For CORE and LiteBIRD we assume $\sigma^P = \sqrt{2}\sigma^T$, while for *Planck* we use the 2015 values. The combined channel estimates are effective values that best approximate eq. (5.18) in the ℓ range of interest. Note that CORE will have $\text{S/N} \geq 5$ in 14 different frequency bands. Also, by combining all frequencies, CORE will have similar S/N in TT , $TE + ET$ and EE .

In figure 7 we show the dipole spectrum derived for two well-defined deviations from the Planck distribution, namely the BE and Comptonization distortions induced by unavoidable energy injections in the radiation field occurring at different cosmic times, early and late, respectively. We briefly discuss below their basic properties and the signal levels expected from different processes.

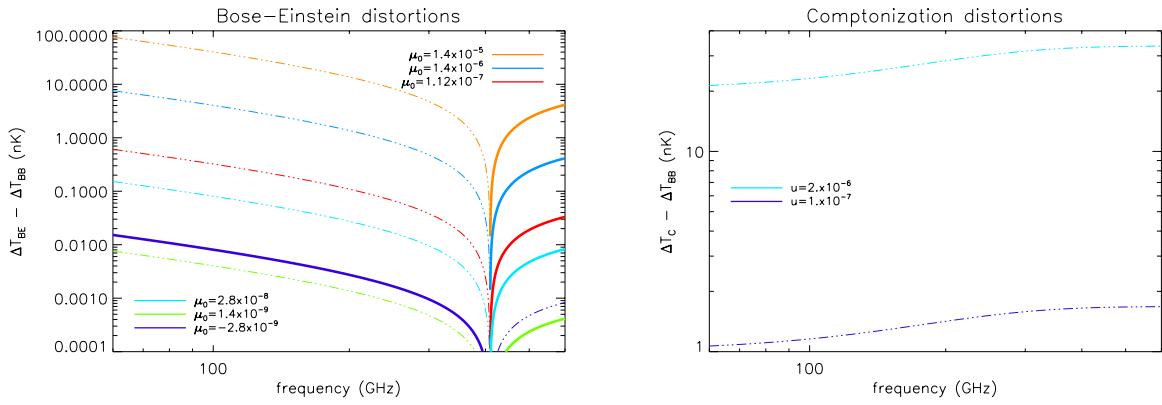


Figure 7. Spectrum of dipole (in equivalent thermodynamic, or CMB, temperature) expressed as the difference between that produced by a distorted spectrum and that corresponding to the blackbody at the current temperature T_0 . Thick solid lines (or thin three dots-dashes) correspond to positive (or negative) values. *Left:* the case of BE distortions for $\mu_0 = -2.8 \times 10^{-9}$ (representative of adiabatic cooling; green dots, note the opposite signs with respect to the cases with positive μ_0), $\mu_0 = 1.4 \times 10^{-5}$, 1.4×10^{-6} (representative of improvements with respect to FIRAS upper limits), $\mu_0 = 1.12 \times 10^{-7}$, 2.8×10^{-8} , and 1.4×10^{-9} (representative of primordial adiabatic perturbation dissipation). *Right:* the case of Comptonization distortions for $u = 2 \times 10^{-6}$ (upper curves) and $u = 1 \times 10^{-7}$ (lower curves), representative of imprints by astrophysical or minimal reionization models, respectively.

A BE-like distorted spectrum is produced by two distinct processes. Firstly there is the dissipation of primordial perturbations at small scales [86, 87], which generates a positive chemical potential. Secondly we have Bose condensation of CMB photons by colder electrons, as a consequence of the faster decrease of the matter temperature relative to the radiation temperature in an expanding Universe, which generates a negative chemical potential [88, 89].

The photon occupation number of the BE spectrum is given by [49]

$$\eta_{\text{BE}} = \frac{1}{e^{x_e + \mu} - 1}, \quad (6.4)$$

where μ is the chemical potential that quantifies the fractional energy, $\Delta\epsilon/\varepsilon_i$, exchanged in the plasma during the interaction,¹⁰ $x_e = x/\phi(z)$, $\phi(z) = T_e(z)/T_{\text{CMB}}(z)$, with $T_e(z)$ being the electron temperature. For a BE spectrum, $\phi = \phi_{\text{BE}}(\mu)$. The dimensionless frequency x is redshift invariant, since in an expanding Universe both T_{CMB} and the physical frequency ν scale as $(1+z)$. For small distortions, $\mu \simeq 1.4\Delta\epsilon/\varepsilon_i$ and $\phi_{\text{BE}} \simeq (1 - 1.11\mu)^{-1/4}$. The current FIRAS 95 % CL upper limit is $|\mu_0| < 9 \times 10^{-5}$ [41], where μ_0 is the value of μ at the redshift z_1 corresponding to the end of the kinetic equilibrium era. At earlier times μ can be significantly higher, and the ultimate limits on $\Delta\epsilon/\varepsilon_i$ before the thermalization redshift (when any distortion can be erased) comes from cosmological nucleosynthesis.

These two kinds of distortions are characterised by a $|\mu_0|$ value in the range, respectively, $\sim 10^{-9}\text{--}10^{-7}$ (and in particular $\simeq 2.52 \times 10^{-8}$ for a primordial scalar perturbation spectral index $n_s = 0.96$, without running), and $\simeq 3 \times 10^{-9}$. Since very small scales that are not explored by current CMB anisotropy data are relevant in this context, a broad set of primordial spectral indices needs to be explored. A wider range of chemical potentials is

¹⁰Here, the subscript i denotes the initial time of the dissipation process.

found by [90], allowing also for variations in the amplitude of primordial perturbations at very small scales, as motivated by some inflation models.

Cosmological reionization associated with the early stages of structure and star formation is an additional source of photon and energy production. This mechanism induces electron heating that is responsible for Comptonization distortions [91]. The characteristic parameter for describing this effect is

$$u(t) = \int_{t_i}^t [(\phi - \phi_i)/\phi] (k_B T_e / m_e c^2) n_e \sigma_T c dt. \quad (6.5)$$

In the case of small energy injections and integrating over the relevant epochs then $u \simeq (1/4)\Delta\varepsilon/\varepsilon_i$. In eq. (6.5), $\phi_i = \phi(z_i) = (1 + \Delta\epsilon/\varepsilon_i)^{-1/4} \simeq 1 - u$ is the ratio between the equilibrium matter temperature and the radiation temperature evaluated at the beginning of the heating process (i.e., at z_i). The distorted spectrum is then

$$\eta_C \simeq \eta_i + u \frac{x/\phi_i \exp(x/\phi_i)}{[\exp(x/\phi_i) - 1]^2} \left(\frac{x/\phi_i}{\tanh(x/2\phi_i) - 4} \right), \quad (6.6)$$

where η_i is the initial photon occupation number (before the energy injection).¹¹

Typically, reionization induces Comptonization distortions with *minimal* values $u \simeq 10^{-7}$ [94]. In addition to this, the variety of energy injections expected in astrophysical reionization models, including: energy produced by nuclear reactions in stars and/or by nuclear activity that mechanically heats the intergalactic medium (IGM); super-winds from supernova explosions and active galactic nuclei; IGM heating by quasar radiative energy; and shocks associated with structure formation. Together these induce much larger values of u (\simeq several $\times 10^{-6}$) [95, 96], i.e., not much below the current FIRAS 95% CL upper limit of $|u| < 1.5 \times 10^{-5}$ [41]. Free-free distortions associated with reionization [97] are instead more relevant at the lowest frequencies (below 10 GHz), and thus we do not consider them in this paper.

We could also consider the possible presence of unconventional heating sources. Decaying and annihilating particles during the pre-recombination epoch may affect the CMB spectrum, with the exact distorted shape depending on the process timescale and, in some cases, being different from the one produced by energy release. This is especially interesting for decaying particles with lifetimes $t_X \simeq \text{few} \times 10^8\text{--}10^{11}$ sec [98–100]. Superconducting cosmic strings would also produce copious electromagnetic radiation, creating CMB spectral distortion shapes [101] that would be distinguishable with high accuracy measurements. Evaporating primordial black holes provide another possible source of energy injection, with the shape of the resulting distortion depending on the black hole mass function [102]. CMB spectral distortion measurements could also be used to constrain the spin of non-evaporating black holes [103]. The CMB spectrum could additionally set constraints on the power spectrum of small-scale magnetic fields [104], the decay of vacuum energy density [105], axions [106], and other new physical processes.

6.2 The CIB dipole

Multi-frequency measurements of the dipole spectrum will allow us to constrain the CIB intensity spectrum [43, 44]. The spectral shape of the CIB is hard to determine directly

¹¹Here and in eq. (6.4) we neglect the effect of photon emission/absorption processes, which is instead remarkable at low frequencies (see [92] and [93]).

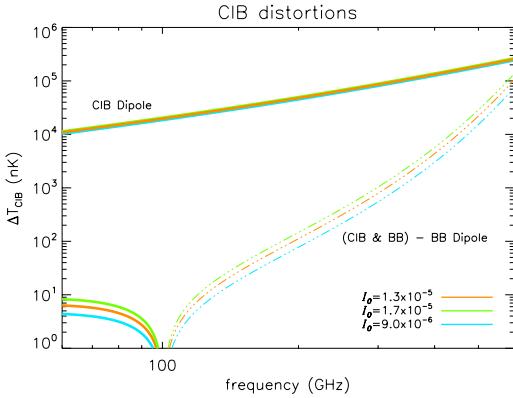


Figure 8. Expected behaviour of the dipole spectrum. The upper lines show the spectrum of the (pure) CIB dipole, while the lower lines show the spectrum coming from the dipole pattern computed from the CIB distribution function added to the blackbody (at temperature T_0) distribution function, minus the dipole pattern computed by the blackbody distribution function. Thick solid lines (or thin three dots-dashes) correspond to positive (or negative) values. The analytic representation of the CIB spectrum by [42] is adopted here, considering the best-fit amplitude and the range of $\pm 1\sigma$.

because it requires absolute intensity measurements, which are also compromised by Galactic and other foregrounds. Although the dipole amplitude is about 10^{-3} of the monopole, its spatial form is already known and hence this indirect route may provide the most robust measurements of the CIB in the future.

Figure 8 shows the CIB dipole spectrum computed according to eq. (6.2), using the analytic representation of the CIB spectrum (observed at present time) given in ref. [42]:

$$\eta_{\text{CIB}} = \frac{c^2}{2h\nu^3} I_{\text{CIB}}(\nu) = I_0 \left(\frac{k_B T_{\text{CIB}}}{h\nu_0} \right)^{k_F} \frac{x_{\text{CIB}}^{k_F}}{\exp(x_{\text{CIB}}) - 1}, \quad (6.7)$$

where $T_{\text{CIB}} = (18.5 \pm 1.2)$ K, $x_{\text{CIB}} = h\nu/k_B T_{\text{CIB}} = 7.78(\nu/\nu_0)$, $\nu_0 \simeq 3 \times 10^{12}$ Hz and $k_F = 0.64 \pm 0.12$. Here I_0 sets the CIB spectrum amplitude, its best-fit value being 1.3×10^{-5} [42]. On the other hand, the uncertainty of the CIB amplitude is currently quite high, with I_0 only known to a 1σ accuracy of about 30 %.

The CIB dipole amplitude, in terms of thermodynamic temperature, increases rapidly with frequency, reaching $257 \mu\text{K}$ (or 652 Jy sr^{-1}) at 600 GHz and $420 \mu\text{K}$ (or 1306 Jy sr^{-1}) at 800 GHz. The measurement of the CIB dipole amplitude will be dependent on systematic effects from the foreground Galaxy subtraction, which has a similar spectrum to the CIB [28]. Although the calibration of the dipole signal at different frequencies is not trivial (since the orbital part of the dipole will be used for calibration), the *Planck* experience is that with sufficient care the limitation is removal of the Galactic signals, not calibration uncertainty. Hence the CIB dipole should be clearly detectable by CORE in its highest frequency bands. Such a detection will provide important constraints on the CIB intensity; its amplitude uncertainty constitutes a major current limitation in our understanding of the dust-obscured star-formation phase of galaxy evolution.

6.3 Beyond the dipole

A generalization of the considerations of the previous section allows us to evaluate the effect of peculiar velocity on the whole sky. To achieve this, we generate maps and, using the Lorentz-

invariance of the distribution function, we can include all orders of the effect, coupling them with the geometrical properties induced at low multipoles. To compute the maps at each multipole¹² $\ell \geq 1$, we first derive the maps at all angular scales, both for the distorted spectra and for the blackbody at the current temperature T_0 . From the dipole direction found in the *Planck* (HFI+LFI combined) 2015 release and defining the motion vector of the observer, we produce the maps in a pixelization scheme at a given observational frequency ν by computing the photon distribution function, η^{BBdist} , for each considered type of spectrum at a frequency given by the observational frequency ν but multiplied by the product $(1 - \hat{n} \cdot \vec{\beta})/(1 - \vec{\beta}^2)^{1/2}$ to account for all the possible sky directions with respect to the observer peculiar velocity. Here the notation ‘BBdist’ stands for BB, CIB, BE, or Comptonization (C). Hence, the map of the observed signal in terms of thermodynamic temperature is given by generalising eq. (6.1):

$$T_{\text{therm}}^{\text{BB/dist}}(\nu, \hat{n}, \vec{\beta}) = \frac{xT_0}{\log(1/(\eta(\nu, \hat{n}, \vec{\beta}))^{\text{BB/dist}} + 1)}, \quad (6.8)$$

where $\eta(\nu, \hat{n}, \vec{\beta}) = \eta(\nu')$ with $\nu' = \nu(1 - \hat{n} \cdot \vec{\beta})/(1 - \vec{\beta}^2)^{1/2}$.

We adopt the **HEALPix** pixelization scheme to discretise the sky at the desired resolution. We decompose the maps into spherical harmonics and then regenerate them considering the a_{lm} only up to a desired multipole ℓ_{max} . We start setting $\ell_{\text{max}} = 5$ and then iterate the process with a decreasing ℓ_{max} . We produce maps containing the power at a single multipole by taking the difference of the map at ℓ_{max} from the map at $\ell_{\text{max}-1}$. We then compute the difference of maps having specific spectral distortions from the purely blackbody maps. As seen in figures 9–11, the expected signal is important for the dipole, can be considerable for the quadrupole and, depending on the distortion parameters, still not negligible for the octupole (although this will depend on the amplitude relative to experimental noise levels, as we discuss below). For higher-order multipoles, the signal is essentially negligible.

Note that the maps present a clear and obvious symmetry with respect to the axis of the observer’s peculiar velocity.¹³ This is simply due to the angular dependence in eq. (6.8). For coordinates in which the positive z -axis is aligned with the dipole, the only angular dependence comes from $\hat{n} \cdot \vec{\beta} \equiv \beta \cos \theta_d$. In terms of the spherical harmonic expansion, this implies that higher-order multipoles will appear as polynomial functions of $\cos \theta_d$, with different frequency-dependent factors depending on the specific type of spectral distortion being considered.

In the above considerations we assumed that each multipole pattern can be isolated from that of the other multipoles. In reality, a certain leakage is expected (particularly between adjacent multipoles), especially as a result of masking for foregrounds. The sources of astrophysical emission are highly complex, and their geometrical properties mix with their frequency behaviour. Furthermore, in real data analysis, there is an interplay between the determination of the calibration and zero levels of the maps, and this issue is even more critical when data in different frequency domains are used to improve the component-separation process. The analysis of these aspects is outside the scope of the present paper, but deserves further investigation.

¹²For the sake of generality and for the purpose of cross-checking, we also include the monopole term, which can be easily subtracted afterwards.

¹³For real experiments, these patterns are weakly modulated (and their perfect symmetry broken) by the second-order (‘orbital dipole’) effect coming from the Earth’s motion around the Sun and (for spacecraft moving around the Earth-Sun L2 point), by the further contribution from motion in the Lissajous orbit.

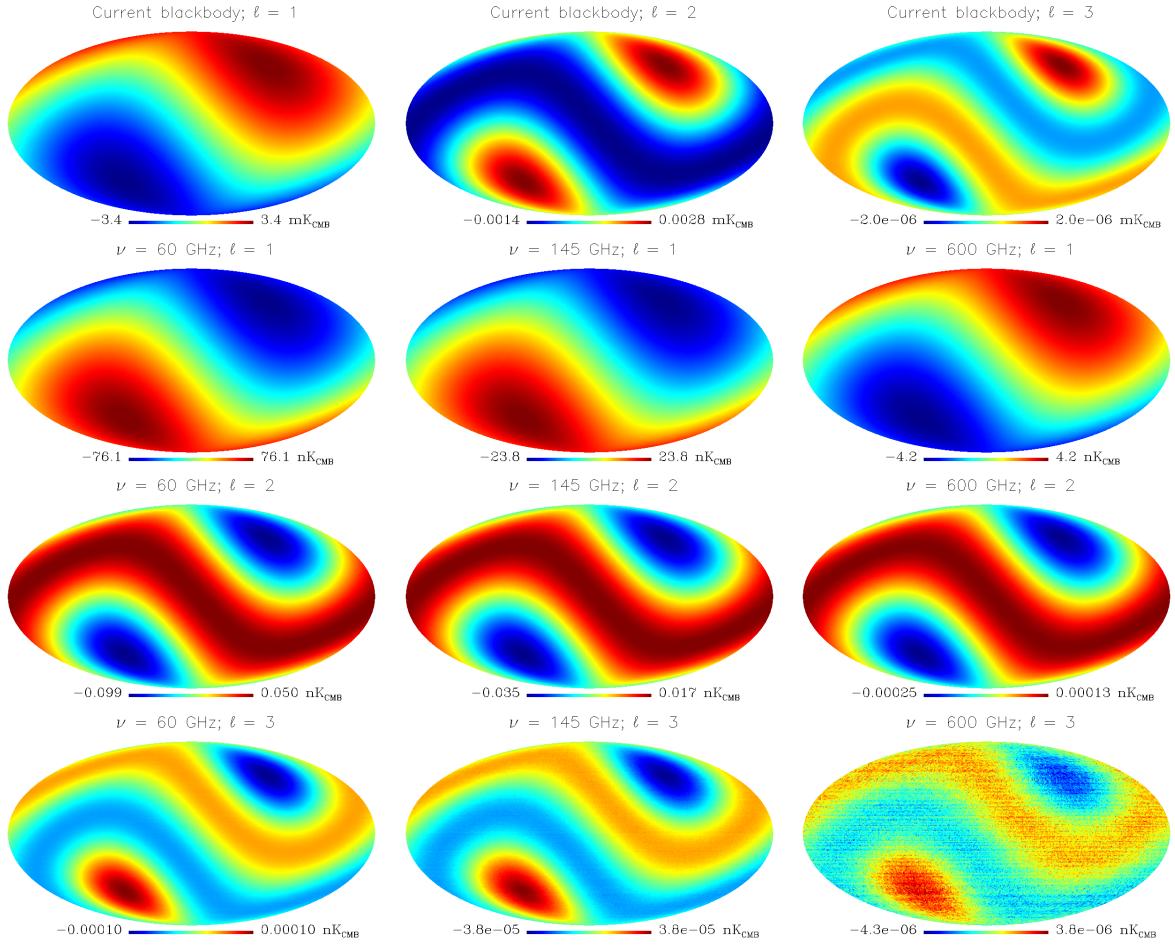


Figure 9. Top row: maps of the dipole, quadrupole and octupole computed assuming a CMB blackbody spectrum at the current temperature T_0 , for reference. In all other cases we show the maps of the dipole (second row), quadrupole (third row), and octupole (bottom row) at three different frequencies (namely 60, 145, and 600 GHz, from left to right), in terms of the difference between the pattern computed for a BE distortion with $\mu_0 = 1.5 \times 10^{-5}$ and that computed for a blackbody at the present-day temperature T_0 .

6.4 Detectability

Here we discuss the detectability of the dipolar and quadrupolar signals introduced in sections 6.1–6.3. To this end we compare the dipole signal with the noise dipole as a function of frequency. Note that since the prediction includes the specific angular dependence of the dipole, there is no cosmic-variance related component in the noise. The noise for each frequency is determined by table 1, assuming full-sky coverage for simplicity.¹⁴

In figure 12 we show the dipole signal for BE and Comptonization distortions (left and right, respectively), defined as the temperature dipole coming from eq. (6.8) subtracted from the CMB dipole (shown as coloured lines). In black we show the CORE noise as a function of frequency. For BE distortions, the signal is clearly above the CORE noise up to about 200 GHz for $\mu_0 \gtrsim 10^{-6}$ and comparable or slightly above the aggregated noise below about

¹⁴Sampling variance, as specified by the adopted masks, will be taken into account in the next section.

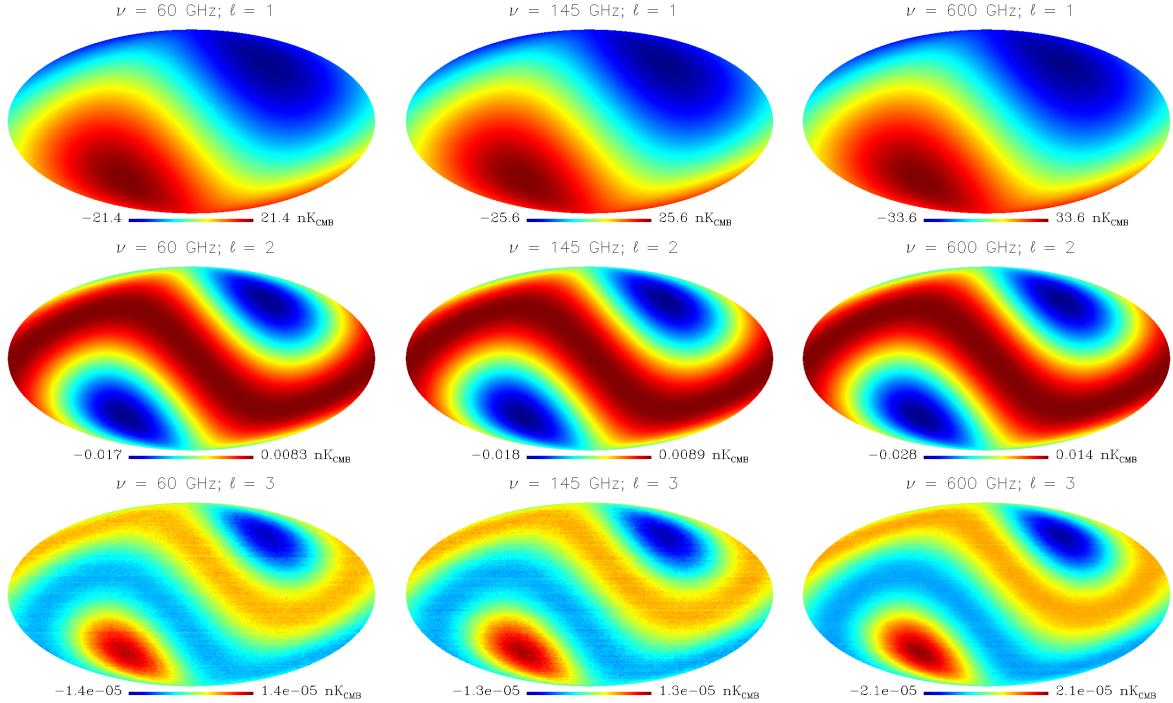


Figure 10. The same as in figure 9, but for the case of a Comptonization distortion with $u = 2 \times 10^{-6}$.

100 GHz for $\mu_0 \gtrsim 10^{-7}$, while for Comptonization distortions, the signal is clearly above the noise up to around 500 GHz for $u \gtrsim 2 \times 10^{-6}$ and comparable to or above the noise between approximately 100 GHz and 300 GHz for $u \gtrsim 10^{-7}$. The analogous analysis for the quadrupole (shown for simplicity only for the largest values of μ_0 and u) shows that, for CORE sensitivity, noise dominates at any frequency for CMB spectral distortion parameters compatible with FIRAS limits, thus experiments beyond CORE are needed to use the quadrupole pattern to infer constraints on CMB spectral distortions. In figure 13 we show the dipole signal of the difference between Comptonization and BE distortion maps. In figure 14 we show the size of the dipole signal (the quadrupole is shown as dashed curves) for the CIB (where we have removed the CMB dipole) compared to noise. The signal is always above the noise except at about 100 GHz. Due to the large uncertainty in the amplitude of the CIB spectra (I_0), we show also deviations of $\pm 1\sigma$ from the best-fit value of 1.3×10^{-5} (as well as their difference from the best fit). The signal is orders of magnitude above the noise at high frequencies and moreover, the quadrupole is above the noise at frequencies greater than about 400 GHz, although it is always much smaller than the dipole (since it is suppressed by an extra factor of β).

Comparing figure 14 with figure 12, it is evident that the dipole power expected from the CIB is above those predicted for CMB spectral distortions at $\nu \gtrsim 200$ GHz for the classes of processes and parameter values discussed here. Since the dependence of the quoted power on the CMB spectral distortion parameter is quadratic, the above statement does not hold for larger CMB distortions, even just below the FIRAS limits. Although they are not predicted by standard scenarios, they may be generated by unconventional dissipation processes, such those discussed at the end of section 6.1, according to their characteristic parameters.

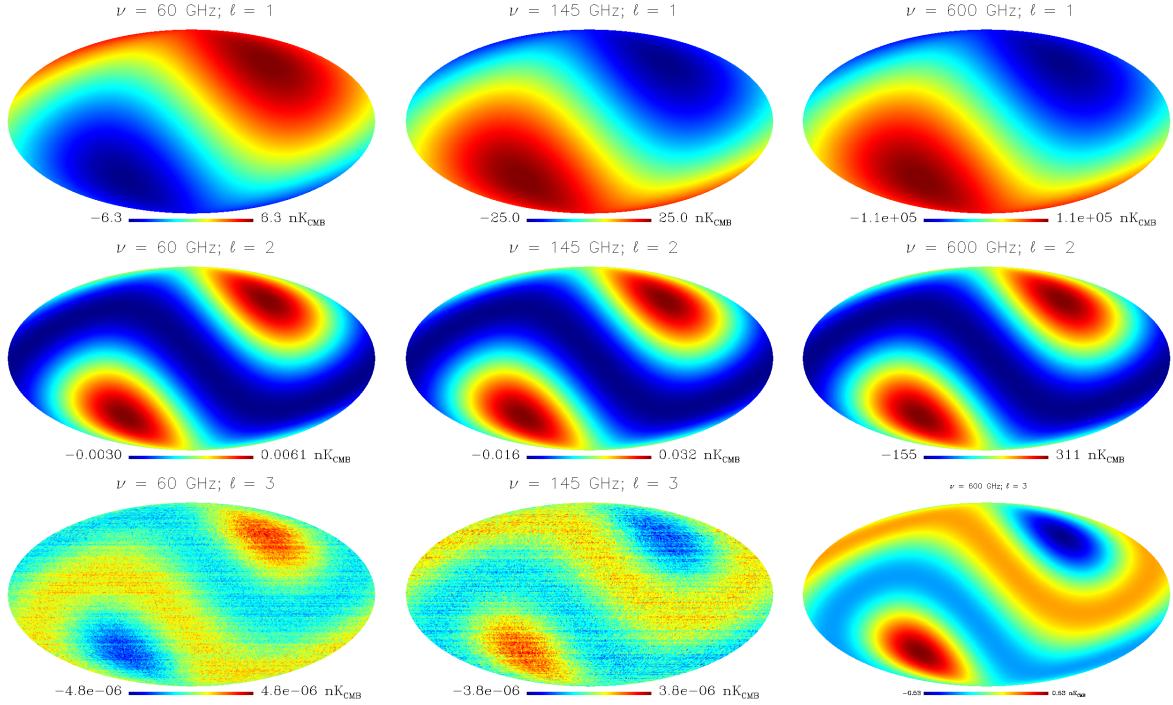


Figure 11. The same as in figure 9, but for the case of the CIB with amplitude set at the best-fit value found by FIRAS. More precisely, we display the temperature pattern of the CIB distribution function added to the blackbody one, minus the temperature pattern coming from the blackbody.

We computed for comparison the power spectrum sensitivity of LiteBIRD (see table 2): it is similar to that of CORE around 300 GHz and significantly worse at $\nu \lesssim 150$ GHz, a range suitable in particular for BE distortions. As discussed in sections 2 and 4, resolution is important to achieve the sky sampling necessary for ultra-accurate dipole analysis, thus adopting a resolution changing from a range of $\simeq 2\text{--}18$ arcmin to a range of $\simeq 0.5^\circ\text{--}1.5^\circ$ is certainly critical. Furthermore, the number of frequency channels is relevant, in particular (see next section) when one compares between pairs of frequencies, the number of which scales approximately as the square of the number of frequency channels. In addition, a large number of frequency channels and especially the joint analysis of frequencies around 300 GHz and above 400 GHz (not foreseen in LiteBIRD) is crucial for separating the various types of signals, and, in particular, to accurately control the contamination by Galactic dust emission.

The analysis carried out here will be extended to include all frequency information in the following section. This will also include a discussion of the impact of residual foregrounds.

7 Simulation results for CMB spectral distortions and CIB intensity

In order to quantify the ideal CORE sensitivity to measure spectral distortion parameters and the CIB amplitude, we carried out some detailed simulations. The idea here is to simulate the sky signal assuming a certain model and to quantify the accuracy level at which (in the presence of noise and of potential residuals) we can recover the key input parameters. We consider twelve reference cases, physically or observationally motivated, based on considerations and works quoted in section 6.2 (cases 2–4) and section 6.1 (cases 8–12), namely:

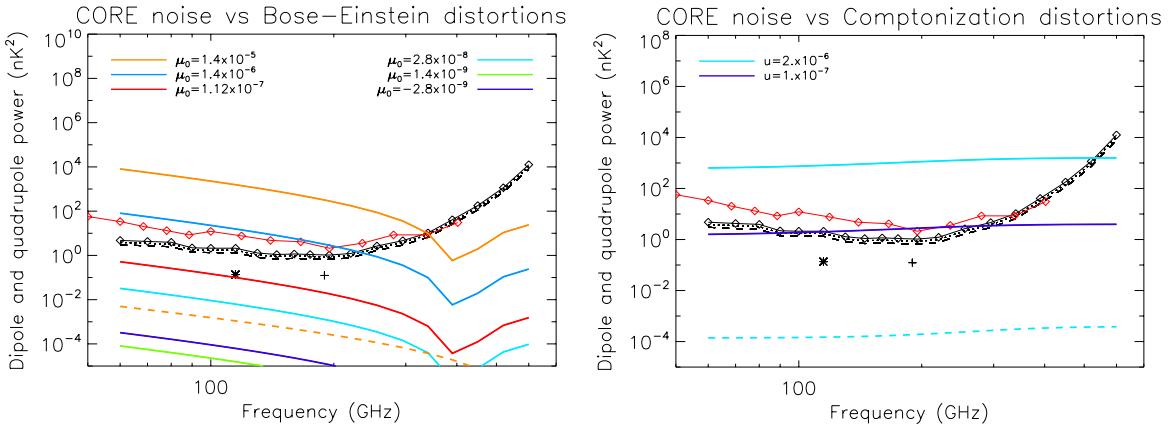


Figure 12. Angular power spectrum of the dipole map, derived from the difference between distorted spectra and the current blackbody spectrum versus CORE sensitivity. The CORE white noise power spectrum (independent of multipole, shown as the black upper solid curve and with diamonds for different frequency channels) and its rms uncertainty (for $\ell = 1$, using dots, and for $\ell = 2$, using dashes) are plotted in black. The cross (asterisk) displays aggregated CORE noise from all channels (up to 220 GHz). We show also for comparison the LiteBIRD white noise power spectrum (red solid curve and diamonds for different frequency channels). *Left:* BE distortions for $\mu_0 = -2.8 \times 10^{-9}$ (representative of adiabatic cooling), $\mu_0 = 1.4 \times 10^{-5}$, 1.4×10^{-6} (representative of improvements with respect to FIRAS upper limits), $\mu_0 = 1.12 \times 10^{-7}$, 2.8×10^{-8} , and 1.4×10^{-9} (representative of primordial adiabatic perturbation dissipation). For $\mu_0 = 1.4 \times 10^{-5}$ we show also the angular power spectrum of the quadrupole map. *Right:* comptonization distortions for $u = 2 \times 10^{-6}$ (upper solid curve for the dipole map and bottom dashed curve for the quadrupole map) and $u = 10^{-7}$ (lower solid curve for the dipole map), representative of imprints by astrophysical and minimal reionization models, respectively.

- (1) a (reference) blackbody spectrum defined by T_0 ;
- (2) a CIB spectrum at the FIRAS best-fit amplitude;
- (3) a CIB spectrum at the FIRAS best-fit amplitude plus 1σ error;
- (4) a CIB spectrum at the FIRAS best-fit amplitude minus 1σ error;
- (5) a BE spectrum with $\mu_0 = 1.12 \times 10^{-7}$, representative of a distortion induced by damping of primordial adiabatic perturbations in the case of relatively high power at small scales;
- (6) a BE spectrum with $\mu_0 = 1.4 \times 10^{-5}$, a value 6.4 times smaller than the FIRAS 95 % upper limits;
- (7) a BE spectrum with $\mu_0 = 1.4 \times 10^{-6}$, a value 64 times smaller than the FIRAS 95 % upper limits;
- (8) a BE spectrum with $\mu_0 = 1.4 \times 10^{-9}$, representative of the typical minimal distortion induced by the damping of primordial adiabatic perturbations;
- (9) a BE spectrum with $\mu_0 = 2.8 \times 10^{-8}$, representative of the typical distortion induced by damping of primordial adiabatic perturbations;

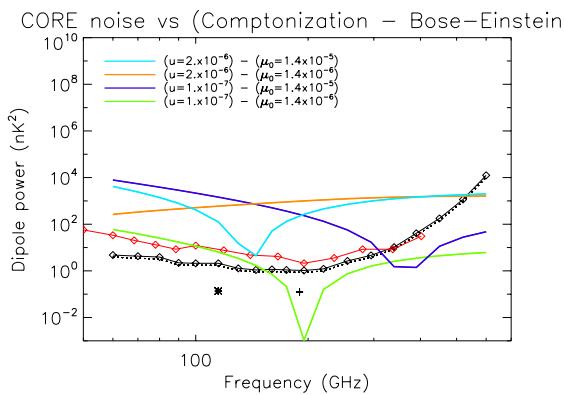


Figure 13. The same as in figure 12, but comparing the two above cases of Comptonization distortions with the two above cases of BE distortions with the largest values of μ_0 .

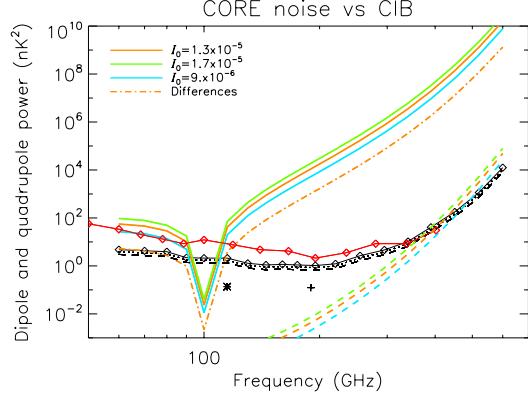


Figure 14. The same as in figure 12, but for the CIB (assuming the model from [42]). Also shown is the quadrupole signal (dashes). The different values of I_0 in eq. (6.8) are the best-fit value and deviations by $\pm 1\sigma$.

- (10) a BE spectrum with $\mu_0 = -2.8 \times 10^{-9}$, representative of the typical distortion induced by BE condensation (adiabatic cooling);
- (11) a Comptonised spectrum with $u = 10^{-7}$, representative of minimal reionization models;
- (12) a Comptonised spectrum with $u = 2 \times 10^{-6}$, representative of typical astrophysical reionization models.

For each model listed we generate both an ideal sky (the “prediction”) and a sky with noise realizations (“simulated data”) according to the sensitivity of CORE (see table 1), at each of its 19 frequency channels. For a suitable number of cases we repeated the analysis working with maps simply containing only the dipole term and verified that the major contribution to the significance comes from the dipole, i.e., the quadrupole (the only other possibly relevant term) contributes almost negligibly,¹⁵ in agreement with section 6.4. For the sake of simplicity our noise realizations assume Gaussian white noise. Our simulation set consists of 10 realizations for each of the 19 CORE frequencies (giving 190 independent noise realizations). These are generated at $N_{\text{side}} = 64$ (roughly 1° resolution). We will also consider the inclusion of certain systematics in the following subsections. We then compare each theoretical prediction with all maps of our simulated data. We calculate $\Delta\chi^2$ for each combination, summarised in a 12×12 matrix, quantifying the significance level at which each model can be potentially detected or ruled out. We report our results in terms of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$, which directly gives the significance in terms of σ levels, since we only consider a single parameter at a time.¹⁶

¹⁵In some cases we found it affects only the last digit (reported in the tables) of the estimated $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$.

¹⁶The adopted number of realizations allows to provide an estimate the rms of the quoted significance values suitable to check (particularly for some results based, for simplicity, on a single realization) they are not in the tail of distribution, to quantitatively compare pros and cons of the three adopted approaches, and to spot in the results the effects of coupling between signal and noise/residuals realizations. With much more realizations it is obviously possible to refine these estimates, but it is not relevant in this work that deals with wide ranges of residual parameters.

σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$							$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$	
		I_0^{bf}	$+1\sigma$	-1σ	8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}	
			1.3	1.7	0.9	1.12×10^{-7}	1.4×10^{-5}	1.4×10^{-6}	1.4×10^{-9}	2.8×10^{-8}	-2.8×10^{-9}	10^{-7}	2×10^{-6}
Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
(1)	0	3650	4740	2540	1.63	175.	17.9	0.0998	0.532	-0.137	7.95	154.	
(2)	3650	0	1100	1110	3650	3640	3650	3650	3650	3650	3650	3620	
(3)	4740	1100	0	2210	4740	4740	4740	4740	4740	4740	4740	4710	
(4)	2540	1110	2200	0	2540	2540	2540	2540	2540	2540	2540	2510	
(5)	0.403	3650	4740	2540	0	174.	16.5	0.384	-0.111	0.445	6.83	153.	
(6)	174.	3640	4740	2540	173.	0	157.	174.	174.	174.	168.	108.	
(7)	17.0	3650	4740	2540	15.6	158.	0	17.0	16.6	17.0	11.8	140.	
(8)	-0.0975	3650	4740	2540	1.62	175.	17.9	0	0.514	-0.165	7.93	154.	
(9)	-0.346	3650	4740	2540	1.28	175.	17.6	-0.342	0	-0.352	7.66	153.	
(10)	0.142	3650	4740	2540	1.67	175.	17.9	0.176	0.567	0	7.98	154.	
(11)	7.25	3650	4740	2540	6.22	169.	12.8	7.23	6.98	7.27	0	146.	
(12)	153.	3620	4710	2510	152.	108.	140.	153.	153.	153.	145.	0	

Table 4. Average values of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ from a Monte Carlo simulation at $N_{\text{side}} = 64$, full-sky coverage, adopting perfect foreground subtraction and calibration, and considering each of the 19 frequency channels.

We perform the $\sqrt{\Delta\chi^2}$ analysis for three different approaches:

- (a) using each of the 19 frequency channels, assuming they are independent;
- (b) using the 171 ($19 \times 18/2$) combinations coming from the differences of the maps from pairs of frequency bands;
- (c) combining cases (a) and (b) together.

When differences of maps from pairs of frequency bands are included in the analysis, in the corresponding contributions to the χ^2 the variance comes from the sum of the variances at the two considered frequencies.

Approach (a) essentially compares the amplitude of dipole of a distorted spectrum with that of the blackbody, being so sensitive to the overall difference between the two cases, while approach (b) compares the dipole signal at different frequencies for each type of spectrum, being so sensitive to its slope.

7.1 Ideal case: perfect calibration and foreground subtraction

Tables 4 and 15 (and tables 5 and 16, tables 6 and 17, respectively) report the results of approach a (approach b, and c, respectively) in terms of average and rms of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ (see appendix B).

We find that, in general, the analysis of the difference of pairs of frequency channels (approach b) tends to substantially increase the significance of the recovery of the CIB amplitude, which is due to the very steep frequency shape of the CIB dipole spectrum. For the opposite reason, the same does not occur in general for CMB distortion parameters, and, in particular, approach (b) can make the recovery of the Comptonization distortion more difficult. These results are in agreement with the shapes displayed in figures 12, 13, and 14. It is important to note that, in general, the rms values found in approach (b) are larger than

σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$						$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$	
		I_0^{bf}	$+1\sigma$	-1σ	8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}
		1.3	1.7	0.9	μ_0						u	
Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
(1)	0	14000	18200	9740	1.96	271.	27.8	0.124	0.666	-0.170	-0.229	43.7
(2)	14000	0	4180	4240	14000	14100	14000	14000	14000	14000	14000	14000
(3)	18200	4190	0	8430	18200	18200	18200	18200	18200	18200	18200	18200
(4)	9740	4240	8420	0	9740	9810	9750	9740	9740	9740	9740	9730
(5)	0.0596	14000	18200	9740	0	269.	25.6	0.0456	-0.249	0.0910	1.44	45.7
(6)	269.	14000	18200	9810	267.	0	242.	269.	269.	269.	271.	312.
(7)	26.0	14000	18200	9750	23.8	244.	0	26.0	25.4	26.1	28.1	69.6
(8)	-0.122	14000	18200	9740	1.93	271.	27.8	0	0.644	-0.205	-0.209	43.7
(9)	-0.386	14000	18200	9740	1.51	271.	27.2	-0.384	0	-0.391	0.228	44.2
(10)	0.178	14000	18200	9740	2.00	271.	27.9	0.220	0.708	0	-0.267	43.6
(11)	2.66	14000	18200	9740	4.69	273.	29.9	2.68	3.11	2.62	0	41.4
(12)	46.4	14000	18200	9730	48.4	314.	72.0	46.4	46.4	44.1	44.1	0

Table 5. The same as in table 4, but considering all 171 independent combinations of pairs of different frequency channels.

σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$						$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$	
		I_0^{bf}	$+1\sigma$	-1σ	8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}
		1.3	1.7	0.9	μ_0						u	
Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
(1)	0	14400	18800	10100	2.67	323.	33.1	0.157	0.844	-0.214	7.83	160.
(2)	14500	0	4320	4380	14500	14500	14500	14500	14500	14500	14500	14400
(3)	18800	4330	0	8710	18800	18800	18800	18800	18800	18800	18800	18800
(4)	10100	4380	8710	0	10100	10100	10100	10100	10100	10100	10100	10100
(5)	0.369	14400	18800	10100	0	320.	30.5	0.346	-0.105	0.413	7.24	159.
(6)	321.	14500	18800	10100	318.	0	288.	321.	320.	321.	319.	330.
(7)	31.1	14500	18800	10100	28.5	290.	0	31.0	30.4	31.1	30.5	157.
(8)	-0.153	14400	18800	10100	2.64	323.	33.1	0	0.816	-0.259	7.82	160.
(9)	-0.537	14400	18800	10100	2.07	322.	32.4	-0.532	0	-0.547	7.61	160.
(10)	0.224	14400	18800	10100	2.73	323.	33.1	0.277	0.900	0	7.85	160.
(11)	7.92	14400	18800	10100	8.03	321.	32.5	7.92	7.87	7.93	0	152.
(12)	160.	14400	18800	10000	160.	332.	157.	160.	160.	160.	152.	0

Table 6. The same as in table 4, but considering each of the 19 frequency channels independently and all 171 independent combinations of pairs of different frequency channels.

those found in approach (a), seemingly relatively more stable. We interpret this as an effect of larger susceptibility of approach (b) to realization combinations. On the other hand, for the estimation of the CIB amplitude this rms amplification does not spoil the improvement in significance. We find that combining the two approaches, as in (c), typically results in an overall advantage, with an improvement in significance larger than the possible increasing of the quoted rms. We anticipate that these results will still be valid when including potential residuals, as discussed below.

We remark that in the present analysis both pure theoretical maps and maps polluted with noise are pixelised in the same way. So, the sampling problem discussed in sections 2 and 4 is automatically by-passed. This is not a limitation for the present analysis, given

the high resolution achieved by CORE, and because it is clear that we could in principle perform our simulations at the desired resolution. Working at roughly 1° resolution makes our analysis feasible without supercomputing facilities, with no significant loss of information. Nonetheless, we also report some results carried out at higher resolution. In particular, in appendix C we present results of the analysis repeated at $N_{\text{side}} = 512$ (i.e., at about 7 arcmin resolution), for a single realization. The results are fully compatible, within the statistical variance, with those derived working at $N_{\text{side}} = 64$.

The matrices reported in each of these tables perhaps require a little more explanation. Firstly, we should point out that the diagonals are zero by construction. We found that the reduced χ^2 ($\chi_r^2 = \chi^2 / (n_d - 1)$, where n_d is the global number of data being treated and we are considering the estimate of a single parameter, namely CMB distortion or CIB amplitude), is always extremely close to unity, which is an obvious validation cross-check. Note that, in principle, when potential residuals are included, one should specify the variance pixel-by-pixel in the estimation of χ^2 .¹⁷ This requires a precise local characterization of residuals. While this can easily be included by construction in our analyses, we explicitly avoid implementing this in the χ^2 analysis, but instead perform our forecasts assuming knowledge of only the average level of the residuals in the sky region being considered. Secondly, we note that the matrices are not perfectly symmetric, due to the cross-terms in the squares (from noise and signal) entering into the χ^2 . Thirdly, the off-diagonal terms are sometimes negative, but with absolute values compatible with the quoted rms. These second and third effects are clearly statistical in nature.

The results found in this section (see also appendix C) identify the ideal sensitivity target for CMB spectral distortion parameters and CIB amplitude that are achievable from the dipole frequency behaviour.

Elements¹⁸ (2:4, 2:4) of the matrix quantify the sensitivity to the CIB amplitude. Comparison with FIRAS in terms of the σ level of significance can be extracted directly from the tables; the ideal improvement ranges from a factor of about 1000 to 4000.

The ideal improvement found for CMB spectral distortion parameters is also impressive. Elements (1, 5:10) and (5:10, 1) and elements (1, 11:12) and (11:12, 1) refer to comparisons between the blackbody and BE and Comptonization distortions, respectively. The comparison with FIRAS is simply quoted by the element of the matrix of the table multiplied by the ratio between the FIRAS 1σ upper limit on μ_0 or u and the distortion parameter value considered in the table. The sensitivity on u is clearly enough to disentangle between minimal models of reionization and a variety of astrophysical models that predict larger amounts of energy injection by various types of source. The ideal improvement with respect to FIRAS limits is about 500–600. The level of (negative) BE distortions is much lower, and the same holds also for BE distortions predicted for the damping of primordial adiabatic perturbations. Only weak, tentative constraints on models with high power at small scales could be set with this approach, for a mission with the sensitivity of CORE. Nonetheless, the ideal improvement with respect to FIRAS limits on BE distortions lies in the range 600–1000.

¹⁷This holds also in the case that the instrument sensitivity varies across the sky because of non-uniform sky coverage from the adopted scanning strategy (an aspect that is not so crucial in the case of the relatively uniform sky coverage expected for CORE [1, 107]) is included in the analysis. Note also that, in principle, pixel-to-pixel correlations introduced by noise correlations and potential residual morphologies should be included in the χ^2 . This aspect, although important in the analysis of real data, is outside the scope of the present paper. Nonetheless, it does not affect the main results of our forecasts.

¹⁸We adopt the convention (row index range, column index range).

σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$							$(\Delta\varepsilon/\varepsilon_i)_{late}$	
					8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}	
		I_0^{bf}	$+1\sigma$	-1σ	μ_0							u	
Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
(1)	0	13.7	17.7	9.61	-0.00676	10.4	0.833	-0.00264	-0.00996	0.00383	0.166	4.83	
(2)	12.8	0	4.37	3.48	12.8	16.6	12.8	12.8	12.8	12.8	12.8	13.1	
(3)	16.8	3.44	0	7.58	16.8	19.9	16.9	16.8	16.8	16.8	16.8	16.9	
(4)	8.75	4.39	8.45	0	8.76	13.7	8.83	8.75	8.75	8.75	8.72	9.47	
(5)	0.0391	13.7	17.7	9.61	0	10.3	0.686	0.0385	0.0307	0.0400	0.133	4.76	
(6)	10.5	17.3	20.6	14.3	10.4	0	9.41	10.5	10.4	10.5	10.2	6.51	
(7)	0.821	13.7	17.7	9.67	0.739	9.39	0	0.821	0.799	0.825	0.611	3.93	
(8)	0.00270	13.7	17.7	9.61	-0.00701	10.4	0.830	0	-0.00967	0.00473	0.166	4.83	
(9)	0.0139	13.7	17.7	9.61	-0.0100	10.4	0.788	0.0135	0	0.0146	0.163	4.82	
(10)	-0.00370	13.7	17.7	9.61	-0.00658	10.4	0.836	-0.00451	-0.0102	0	0.166	4.84	
(11)	0.0337	13.7	17.6	9.57	-0.0402	10.2	0.505	0.0330	0.0210	0.0346	0	4.60	
(12)	4.56	13.9	17.7	10.1	4.48	6.28	3.57	4.56	4.54	4.56	4.32	0	

Table 7. Average values of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ from a Monte Carlo simulation at $N_{\text{side}} = 64$, with full-sky coverage, adopting $E_{\text{for}} = 10^{-2}$ and $E_{\text{cal}} = 10^{-4}$, and considering each of the 19 frequency channels.

The other elements of the matrix refer to the comparison of distorted spectra; note in particular the elements (6:7, 11:12) and (11:12, 6:7) that show how Comptonization distortions can be distinguished from BE distortions, for the two larger values considered for μ_0 , as suggested by figure 13.

7.2 Including potential foreground and calibration residuals

We expect that potential residuals from imperfect foreground subtraction and calibration may affect the results presented in the previous section, depending on their level. To assess this, we have carried out a wide set of simulations in order to quantify the accuracy in recovering the CMB distortion parameters and CIB amplitude under different working assumptions.

We first perform simulations adopting $E_{\text{for}} = 10^{-2}$ and $E_{\text{cal}} = 10^{-4}$ (defined by the parametric model introduced in section 3) at $N_{\text{side}} = 64$, and then add many tests exploring combinations of possible improvements in foreground characterization (assuming $E_{\text{for}} = 10^{-3}$ or $E_{\text{for}} = 10^{-2}$, but at larger N_{side}), as well as different levels of calibration accuracy (including possible worsening at higher frequencies).

7.2.1 Monte Carlo results at about 1° resolution

To understand the typical implications of different assumptions, we first perform a series of Monte Carlo simulations, identical to that described in section 7.1, but including potential foreground and calibration residuals, modelled according to section 3, assuming $E_{\text{for}} = 10^{-2}$ and $E_{\text{cal}} = 10^{-4}$. The main results (the average values of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$) are presented in tables 7, 8, and 9, while the corresponding rms values are reported in appendix D (see tables 19, 20, and 21).

With these levels of potential residuals, the improvement with respect to FIRAS in the recovery of the CIB amplitude ranges from a factor of approximately 4 (with an rms of about 1 in the estimate of this improvement factor) for approach (a) to a factor of about 15 or 20 (with an rms of about 3) for approaches (b) and (c), respectively.

σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$							$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$	
					8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}	
		I_0^{bf}	$+1\sigma$	-1σ	μ_0							u	
Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
(1)	0	49.9	64.7	35.0	-0.224	6.67	-0.311	-0.0267	-0.117	0.0379	0.211	1.15	
(2)	47.7	0	15.6	13.4	47.7	49.9	47.8	47.7	47.7	47.7	47.6	47.4	
(3)	62.4	13.3	0	28.4	62.4	64.5	62.6	62.4	62.4	62.4	62.4	62.2	
(4)	32.7	15.8	30.6	0	32.7	35.2	32.9	32.7	32.7	32.7	32.7	32.5	
(5)	0.250	49.9	64.7	35.0	0	6.61	-0.324	0.248	0.214	0.253	0.314	1.21	
(6)	8.51	52.3	66.9	37.7	8.44	0	7.71	8.51	8.48	8.51	8.54	9.31	
(7)	1.15	50.1	64.9	35.2	1.08	5.84	0	1.15	1.13	1.15	1.20	2.06	
(8)	0.0268	49.9	64.7	35.0	-0.223	6.67	-0.310	0	-0.114	0.0465	0.212	1.15	
(9)	0.121	49.9	64.7	35.0	-0.196	6.66	-0.314	0.118	0	0.127	0.239	1.17	
(10)	-0.0378	49.9	64.7	35.0	-0.227	6.67	-0.310	-0.0463	-0.122	0	0.208	1.15	
(11)	-0.206	49.9	64.7	35.0	-0.289	6.71	-0.322	-0.207	-0.230	-0.203	0	1.11	
(12)	-0.710	49.6	64.4	34.7	-0.706	7.40	-0.391	-0.709	-0.708	-0.711	-0.703	0	

Table 8. The same as in table 7, but considering all 171 independent combinations of pairs of different frequency channels.

σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$							$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$	
					8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}	
		I_0^{bf}	$+1\sigma$	-1σ	μ_0							u	
Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
(1)	0	51.8	67.0	36.3	-0.191	12.4	0.142	-0.0230	-0.101	0.0327	0.309	5.10	
(2)	49.4	0	16.2	13.9	49.4	52.6	49.5	49.4	49.4	49.4	49.3	49.2	
(3)	64.6	13.7	0	29.4	64.7	67.5	64.8	64.7	64.7	64.6	64.6	64.4	
(4)	33.9	16.4	31.8	0	33.9	37.7	34.1	33.9	33.9	33.9	33.9	33.9	
(5)	0.222	51.8	67.1	36.3	0	12.3	0.0689	0.220	0.189	0.225	0.402	5.05	
(6)	13.5	55.1	70.0	40.2	13.4	0	12.2	13.5	13.5	13.5	13.4	11.4	
(7)	1.48	52.0	67.3	36.5	1.38	11.2	0	1.48	1.46	1.49	1.43	4.57	
(8)	0.0231	51.8	67.0	36.3	-0.190	12.4	0.142	0	-0.0987	0.0401	0.309	5.10	
(9)	0.105	51.8	67.0	36.3	-0.169	12.4	0.123	0.102	0	0.110	0.338	5.09	
(10)	-0.0326	51.8	67.0	36.3	-0.193	12.4	0.145	-0.0399	-0.106	0	0.308	5.10	
(11)	-0.143	51.7	67.0	36.3	-0.324	12.3	-0.0738	-0.147	-0.200	-0.136	0	4.86	
(12)	4.35	51.5	66.8	36.2	4.26	9.77	3.06	4.35	4.33	4.35	4.10	0	

Table 9. The same as in table 7, but considering each of the 19 frequency channels independently and all 171 independent combinations of pairs of different frequency channels.

The improvement found for the recovery of CMB spectral distortion parameters is also very promising. The sensitivity to u improves with respect to FIRAS by a factor of 20 (except for the less stable approach (b)), which is suitable for detecting reionization imprints (of the sort predicted in astrophysical reionization models) at about 5σ , while the improvement on BE distortions is about a factor of 40 (approach (c)). Note that these results are derived considering the full sky, and thus we could expect to obtain improvements by applying masks to avoid regions with significant potential contamination, as discussed in the next section.

σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$						$(\Delta\varepsilon/\varepsilon_i)_{late}$	
		I_0^{bf}	$+1\sigma$	-1σ	8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}
		1.3	1.7	0.9	1.12×10^{-7}	1.4×10^{-5}	1.4×10^{-6}	1.4×10^{-9}	2.8×10^{-8}	-2.8×10^{-9}	10^{-7}	2×10^{-6}
Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
(1)	0	73.5	95.1	51.8	0.139	14.8	1.50	0.00844	0.0473	-0.0113	-0.385	5.29
(2)	69.1	0	23.7	19.4	69.1	72.7	69.3	69.1	69.1	69.1	69.0	68.7
(3)	90.6	19.2	0	41.0	90.6	93.9	90.8	90.6	90.6	90.6	90.6	90.2
(4)	47.3	23.8	45.4	0	47.4	51.6	47.6	47.3	47.3	47.3	47.3	47.0
(5)	0.0920	73.5	95.1	51.8	0	14.7	1.38	0.0905	0.0611	0.0950	-0.422	5.22
(6)	14.7	76.9	98.2	55.7	14.6	0	13.3	14.7	14.7	14.7	14.6	12.2
(7)	1.45	73.7	95.3	52.0	1.33	13.3	0	1.45	1.42	1.46	1.22	4.53
(8)	-0.00818	73.5	95.1	51.8	0.138	14.8	1.50	0	0.0457	-0.0137	-0.386	5.29
(9)	-0.0223	73.5	95.1	51.8	0.109	14.8	1.47	-0.0227	0	-0.0213	-0.398	5.27
(10)	0.0121	73.5	95.1	51.8	0.142	14.8	1.50	0.0150	0.0506	0	-0.384	5.29
(11)	0.558	73.5	95.0	51.7	0.541	14.6	1.44	0.558	0.551	0.559	0	5.00
(12)	6.10	73.2	94.7	51.6	6.04	12.6	5.46	6.10	6.08	6.10	5.81	0

Table 10. Values of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ for a single realization at $N_{\text{side}} = 64$, using the *Planck* mask-76 extended to exclude regions at $|b| \leq 30^\circ$. We adopt $E_{\text{for}} = 10^{-2}$ and $E_{\text{cal}} = 10^{-4}$, and consider each of the 19 frequency channels and all 171 independent combinations of pairs of different frequencies.

7.2.2 Application of masks

We performed some additional tests assuming $E_{\text{for}} = 10^{-2}$ and $E_{\text{cal}} = 10^{-4}$, but applying appropriate masks to the sky. Clearly, in this way we reduce the available statistical information (as we verified through tests carried out under ideal conditions of perfect foreground subtraction and calibration), but in realistic cases we may expect to improve the quality of results by reducing the impact of potential residuals.

We use the “*Planck* common mask 76” (in temperature) and the extension of this mask that excludes all pixels at $|b| \leq 30^\circ$.¹⁹

Having already addressed the rms uncertainty in the $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ estimates, in this test (as well as in the following ones) we will consider a single realization only, in order to avoid repeating a huge number of unnecessary simulations. For the sake of simplicity, we omit reporting the results found in the less stable approach (b).

In the case of the extended mask and including also the cross-comparisons between different frequency channels (approach (c)), we found a significant improvement (see table 10) with respect to the results based on the full sky; the significance of the CIB amplitude recovery improves by about 50 % and that on the BE distortion improves by about 20 %. This indicates the relevance of optimising the selection of the sky region for which the analysis is applied, and of comparing results obtained with different masks.

¹⁹We also considered a mask that excludes also all pixels within 30° of the Ecliptic plane, to avoid zodiacal-light contamination, but the resulting map has considerably less statistical power due to the low overall sky fraction.

7.2.3 Varying assumptions on potential foreground and calibration residuals

We now consider the implications of different levels of potential residuals, evaluating both better and worse cases with respect to the reference case analysed before. Given the results obtained in the previous section we will focus on the case of the extended mask. We present here the main outcomes of this analysis, while the tables with the corresponding numerical results are reported in appendix E for sake of completeness.

- **Improving foreground subtraction**

We now evaluate the improvement in component separation of total intensity maps by considering the case of $E_{\text{for}} = 10^{-3}$. The results, summarised in table 22 (for approach (c)), can be compared with those of table 10. We find an improvement by a factor of approximately 10 in the recovery of the CIB amplitude, in line with that assumed in foreground removal, and by a factor of 5 (or 6) in the recovery of μ_0 (or u), implying that calibration uncertainty is relatively more important for estimating CMB distortion parameters than for estimating the CIB amplitude. In fact, the CIB is better constrained at higher frequencies, where foregrounds are more relevant.

- **The case of poorer calibration**

We discuss here the degradation in sensitivity entailed by keeping $E_{\text{for}} = 10^{-2}$, but replacing CORE’s calibration-accuracy goal of $E_{\text{cal}} = 10^{-4}$ with $E_{\text{cal}} = 10^{-3}$ at $\nu \leq 295$ GHz and $E_{\text{cal}} = 10^{-2}$ at $\nu \geq 340$ GHz.

The results, summarised in table 23 (for approach (c)), can be compared with those of table 10. In spite of the assumed degradation in calibration accuracy at high frequencies (particularly relevant for the CIB), we find that the recovery of the CIB amplitude is very weakly affected, while the significance of the μ_0 (or u) determination degrades by factor of approximately 2 (or 25–30%). This result strengthens the conclusion of the previous subsection that calibration uncertainty is relatively more important for estimating CMB distortion parameters than for the CIB amplitude.

For the set of assumptions adopted here, we find an improvement with respect to FIRAS by factor of around 20 in the recovery of the CIB amplitude, 15 on the constraints on the Comptonization parameter u (or for its detection, at a level of about 3–4 σ for astrophysical reionization models), and about 24 for the constraints on chemical potential μ_0 .

We finally consider a worst case scenario with $E_{\text{for}} = E_{\text{cal}} = 10^{-2}$. Even in this situation, we find an improvement with respect to FIRAS by a factor of 17 in the recovery of the CIB amplitude, and a factor of a few for CMB spectral distortion parameters, specifically around 4 for BE distortions and a marginal detection of astrophysical reionization models for Comptonization distortions.

- **Poorer calibration together with improved foreground subtraction**

We now consider a combination of the two cases above, i.e., a further improvement in component separation of total intensity maps represented by $E_{\text{for}} = 10^{-3}$ and a calibration accuracy parameterised by $E_{\text{cal}} = 10^{-3}$ at $\nu \leq 295$ GHz and $E_{\text{cal}} = 10^{-2}$ at $\nu \geq 340$ GHz.

The results obtained in approach (c) are summarised in table 24. We find that the significance of CIB amplitude recovery is intermediate between the results found in

the previous cases, while the degradation due to the poorer calibration is approximately compensated by the improvement due to better foreground subtraction in the case of Comptonization distortions, but only partially compensated in the case of BE distortions.

Overall, our analysis indicates that the relevance of calibration accuracy increases from CIB amplitude to Comptonization-distortion and to BE-distortion recovery, while the relevance of the quality of foreground subtraction increases from BE distortions to Comptonization distortions and to CIB amplitude recovery. This conclusion reflects the increase of the foreground level and of the relative amplitude of the imprints left by the three types of signals at increasing frequencies (for CORE).

- **Varying the reference angular scale**

We finally consider assumptions of errors in foreground subtraction and in calibration in the range discussed above, but at smaller angular scales, specifically at $N_{\text{side}} = 256$. The corresponding pixel linear size ($\simeq 13.7$ arcmin) is similar to the FWHM resolution of CORE channels at $\nu \lesssim 80$ GHz that are necessary for the mitigation of low-frequency foreground emission.

With this adopted set-up and considering the most advantageous approach (i.e., approach (c)), assuming a foreground mitigation parameterised by $E_{\text{for}} = 10^{-3}$, we find (see table 25) an improvement with respect to FIRAS by a factor of 80–90 for the recovery of CIB amplitude, around 80 on the constraints for the Comptonization parameter u (implying a precise measure of the energy injections associated to astrophysical reionization models), and about 150 on the constraints on chemical potential μ_0 . Adopting $E_{\text{for}} = 10^{-2}$, we find instead an improvement by a factor of 75 for the recovery of CIB amplitude, 50 for the constraints on the Comptonization parameter u , and 80 for the constraints on the chemical potential μ_0 .

We further consider the same set-up but at $N_{\text{side}} = 128$, i.e., with a pixel side 2 times larger. As expected, we find results intermediate between those derived at $N_{\text{side}} = 64$ and 256.

7.3 Summary of simulation results

We have presented above a large set of simulations for different choices of the parameters characterising foreground and calibration residual levels. The main results are summarised in table 11 in terms of improvements with respect to FIRAS, in order to parametrically quantify the accuracy required to achieve significant improvements. For other values of E_{for} and E_{cal} , we find an almost linear dependence on them for the improvement factor in parameter recovery.

8 Discussion and conclusions

We have carried out a detailed investigation of three distinct scientific implications coming from exploitation of the observer’s peculiar velocity effects in CORE maps. The determination of the CMB dipole amplitude and direction is an important observable in modern cosmology. It provides information on our velocity with respect to the CMB reference frame, which is expected to dominate the effect. Related investigations in other wavebands, which

	$E_{\text{cal}} (\%)$	$E_{\text{for}} (\%)$	CIB amplitude	Bose-Einstein	Comptonization
Ideal case, all sky	–	–	$\simeq 4.4 \times 10^3$	$\simeq 10^3$	$\simeq 6.0 \times 10^2$
All sky	10^{-4}	10^{-2}	$\simeq 15$	$\simeq 42$	$\simeq 18$
P76	10^{-4}	10^{-2}	$\simeq 19$	$\simeq 42$	$\simeq 18$
P76ext	10^{-2}	10^{-2}	$\simeq 17$	~ 4	~ 2
P76ext	10^{-4}	10^{-2}	$\simeq 22$	$\simeq 47$	$\simeq 21$
P76ext	10^{-4}	10^{-3}	$\simeq 2.1 \times 10^2$	$\simeq 2.4 \times 10^2$	$\simeq 1.1 \times 10^2$
P76ext	$10_{(\leq 295)}^{-3} - 10_{(\geq 340)}^{-2}$	10^{-2}	$\simeq 19$	$\simeq 26$	$\simeq 11$
P76ext	$10_{(\leq 295)}^{-3} - 10_{(\geq 340)}^{-2}$	10^{-3}	$\simeq 48$	$\simeq 35$	$\simeq 15$
P76ext, $N_{\text{side}} = 128$	$10_{(\leq 295)}^{-3} - 10_{(\geq 340)}^{-2}$	10^{-2}	$\simeq 38$	$\simeq 51$	$\simeq 23$
P76ext, $N_{\text{side}} = 128$	$10_{(\leq 295)}^{-3} - 10_{(\geq 340)}^{-2}$	10^{-3}	$\simeq 43$	$\simeq 87$	$\simeq 39$
P76ext, $N_{\text{side}} = 256$	$10_{(\leq 295)}^{-3} - 10_{(\geq 340)}^{-2}$	10^{-2}	$\simeq 76$	$\simeq 98$	$\simeq 44$
P76ext, $N_{\text{side}} = 256$	$10_{(\leq 295)}^{-3} - 10_{(\geq 340)}^{-2}$	10^{-3}	$\simeq 85$	$\simeq 1.6 \times 10^2$	$\simeq 73$

Table 11. Predicted improvement in the recovery of the distortion parameters discussed in the text with respect to FIRAS for different calibration and foreground residual assumptions. This table summarizes the results derived with approach (c). “P06” stands for the *Planck* common mask, while “P06ext” is the extended P06 mask. When not explicitly stated, all values refer to E_{cal} and E_{for} at $N_{\text{side}} = 64$.

exploit signals from different types of astrophysical sources, probe different shells in redshift, and together provide an important test of fundamental principles in cosmology. In particular, the alignment of the CMB dipole with those independently measured from galaxy and cluster catalogues is regarded as indirect proof of the kinematic origin of the CMB dipole. The specific relation between the amplitudes of the CMB and large-scale structure dipoles, predicted by the linear perturbation theory, has been used to obtain estimates of the redshift-space distortion parameter independent of (but consistent with) those coming from redshift surveys. It is thus important to look for possible departures from a purely kinematic character for the CMB dipole. In this context, surveys from space are clearly appealing, since they represent the best (and perhaps only) way to precisely measure this large-scale signal.

We performed detailed simulations in the context of a mission like CORE, to understand the expectations, and potential issues arising from future CMB surveys beyond the already excellent results produced by *Planck*. The sampling of the sky turns out to be the main limiting factor for the precise measurement of the dipole direction and (obviously together with calibration) also a crucial limiting factor for the precise measurement of dipole amplitude. We found that the recovered uncertainty scales linearly with the map pixel linear size (i.e., inversely with N_{side}). Although maps can be oversampled through a proper scanning strategy and by setting the sampling time of the data acquisition well below that corresponding to the beam resolution, it is clear that the experimental resolution plays a crucial role in this respect. Among CMB space missions proposed for the future, CORE has the best angular resolution. The dipole direction determination can be averaged over the various frequency channels, improving accuracy and providing cross-checks for systematics. With the assumption of a pure blackbody, the same holds for the amplitude. However, when searching for

dipole spectral signatures, increasing the accuracy at each frequency (which results from a better sky sampling) turns out to be even more important.

An observer moving with respect to the CMB rest frame will also see boosting imprints on the CMB at $\ell > 1$, due to Doppler and aberration effects, which can be measured in harmonic space as correlations between ℓ and $\ell+1$ modes (assuming that the CMB is statistically isotropic in its rest frame). Such a signal can be measured independently in temperature and polarization, which constitutes a new consistency check, with a signal-to-noise ratio of about 8 for TT , 7 for $TE + ET$ and 7 for EE . Overall, CORE can achieve a signal-to-noise ratio of almost 13, which improves on the capabilities of *Planck* (about $S/N \simeq 4$, only in TT) and is essentially that of an ideal cosmic-variance-limited experiment up to $\ell \simeq 2000$. We stress the importance of performing high-sensitivity measurements at close to arcminute resolution in order to be sensitive to the correlations at high multipoles that yield most of the signal. Since CORE will also provide good measurements of the tSZ effect and the CIB, which are also assumed to be statistically isotropic in the CMB rest frame, we additionally investigated boosting effects in these maps. However, we found that the aberration effect on tSZ maps and the boosting effects on the CIB are smaller than in the CMB maps, and that the predicted signal-to-noise is less than 1 in both cases.

Beyond FIRAS, great hopes are expected for PIXIE, which has been proposed to NASA to observe CMB polarization and the CMB spectrum with degree resolution and is designed to have a precision about 10^3 times better than FIRAS, mainly relying on the achievement of extreme quality in its absolute calibration, and a corresponding similar improvement on CMB spectral distortion parameters [60]. Note that even if PIXIE fails to fully achieve these ambitious goals, an improvement in calibration precision of even one or two orders of magnitude with respect to FIRAS calibration, in addition to being intrinsically interesting for strengthening the limits on CMB distortion parameters, will imply an analogous improvement for the calibration of other CMB projects. In general, combining results from experiments like PIXIE and CORE will offer a chance to have maps with substantially improved calibration, sensitivity, and resolution.

CMB anisotropy missions will not perform absolute measurements of the CMB spectrum, but can observe the frequency spectral behaviour of the CMB and CIB dipoles. We exploit the sensitivity of an experiment like CORE for the recovery of the parameters u and μ_0 of Comptonization and BE spectral distortions, as well as for the amplitude of the CIB spectrum. Assuming perfect relative calibration and absence of foreground contamination, the CORE sensitivity and frequency coverage, combined with its resolution (to cope with sampling uncertainty), could allow us to achieve an improvement with respect to FIRAS by a factor of around $1\text{--}4 \times 10^3$, 500–600, and 600–1000 in the recovery of the CIB spectrum amplitude, u , and μ_0 , respectively; the best results are obtained from the joint information contained in each of the frequency channels independently *and* in all the independent combinations of pairs of different frequencies. Combining pairs of different frequencies turns out to be particularly advantageous for the CIB dipole spectrum, since it exhibits a steeper frequency behaviour.

As expected, foregrounds are critical in both absolute and differential methods. Relative calibration accuracy is an important limiting factor in CMB anisotropy experiments in general and even more so for analyses based on the dipole. In current data analysis pipelines the dipole itself is in fact typically used for calibration, which raises the issue of a circular argument. However, for all-sky mapping experiments (like *WMAP* and *Planck*), the *orbital* dipole from the Earth and satellite motion is ultimately used for calibration, rather than

the CMB dipole itself. Precise calibration is always challenging, and it is unclear what the limiting step will be for any new experiment. Nevertheless, in principle it will be possible to measure the spectrum of the dipole with an anisotropy experiment. In general, improving and extending calibration methods is crucial for these analyses. Various approaches can be integrated into the data reduction design, ranging from a better instrumental characterization to cross-correlation between different CMB surveys and substantial refinements in astronomical calibration sources.

We have carried out a large set of simulations, summarised in table 11, to parametrically quantify the accuracy required to achieve significant improvements with respect to FIRAS.

We find that the importance of the impact of calibration errors decreases from BE distortions to Comptonization distortions and to the CIB amplitude, while the opposite holds for the impact of foreground contamination (in agreement with the increase with frequency of foreground level and of the relative amplitude of the imprints left by the three types of signal). Applying suitable masks also yields an improvement in parameter estimation.

In the case of 1% accuracy (at a reference scale of about 1°) in both foreground removal and relative calibration (i.e., $E_{\text{for}} = E_{\text{cal}} = 10^{-2}$), CORE will be able to improve the recovery of the CIB spectrum amplitude of a factor of about 17, to achieve a marginal detection of the energy release associated with astrophysical reionization models, and to improve by a factor of approximately 4 the limits on early energy dissipations. On the other hand, an improvement of a factor of 20 for CIB amplitude, of 10 for u , and of around 25 for the chemical potential μ_0 , is found by improving the relative calibration error to $\simeq 0.1\%$. Any further improvement in foreground mitigation and calibration will enable still more precise results to be achieved.

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A Likelihoods of CMB dipole parameters

For the sake of completeness, we report here the likelihoods computed for CMB dipole parameters and the confidence levels in their estimation. We limit the presentation here to the lowest and highest resolutions among those exploited in this analysis.

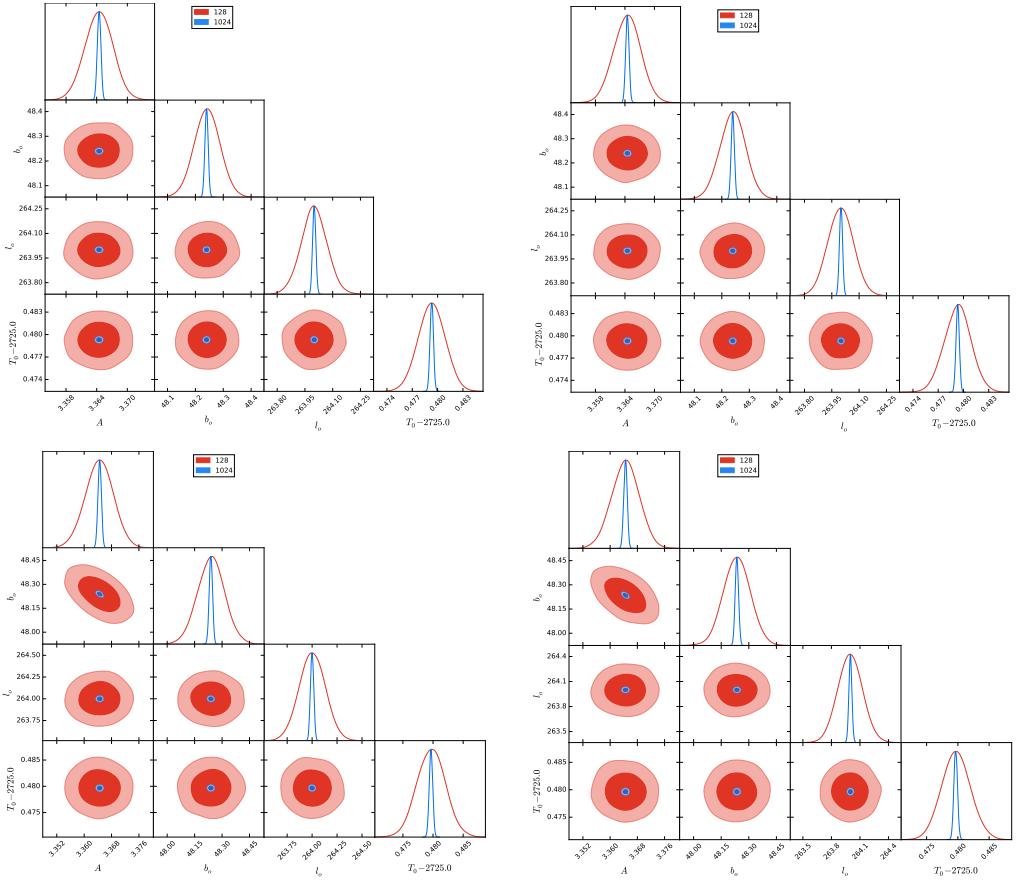


Figure 15. Marginalised likelihoods, and 68% and 95% contours of the parameters A , b_0 , l_0 , and T_0 at $N_{\text{side}} = 128$ (red) and at $N_{\text{side}} = 1024$ (blue): top left, dipole only; top right, dipole+noise; bottom left, dipole+noise+mask; and bottom right, dipole+noise+mask+systematics. The reference frequency channel is 60 GHz and the noise is $7.5 \mu\text{K}\cdot\text{arcmin}^2$. The mask used here is the *Planck* Galactic mask extended to cut out $\pm 30^\circ$ of the Galactic plane. The level of systematics correspond to the pessimistic expectation of calibration errors and sky residuals.

$N_{\text{side}} = 128$	$A(\text{mK})$	$b_0(\text{°})$	$l_0(\text{°})$	$T_0(\text{mK})$
dipole	3.3644 ± 0.0028	48.242 ± 0.047	263.999 ± 0.070	2725.4793 ± 0.0016
dip+noi	3.3644 ± 0.0028	48.240 ± 0.047	263.998 ± 0.071	2725.4793 ± 0.0016
dip+noi+mask	3.3644 ± 0.0041	48.240 ± 0.075	264.00 ± 0.13	2725.4797 ± 0.0024
dip+noi+mask+sys	3.3645 ± 0.0041	48.235 ± 0.074	264.00 ± 0.13	2725.4797 ± 0.0023
$N_{\text{side}} = 1024$	$A(\text{mK})$	$b_0(\text{°})$	$l_0(\text{°})$	$T_0(\text{mK})$
dipole	3.36447 ± 0.00036	48.2399 ± 0.0060	264.0002 ± 0.0088	2725.47930 ± 0.00020
dip+noi	3.36450 ± 0.00035	48.2398 ± 0.0059	264.0005 ± 0.0087	2725.47931 ± 0.00020
dip+noi+mask	3.36454 ± 0.00051	48.2387 ± 0.0091	264.000 ± 0.017	2725.47966 ± 0.00029
dip+noi+mask+sys	3.36451 ± 0.00052	48.2352 ± 0.0092	264.000 ± 0.016	2725.47965 ± 0.00029

Table 12. 68% confidence levels of the parameters A , b_0 , l_0 , and T_0 from figure 15.

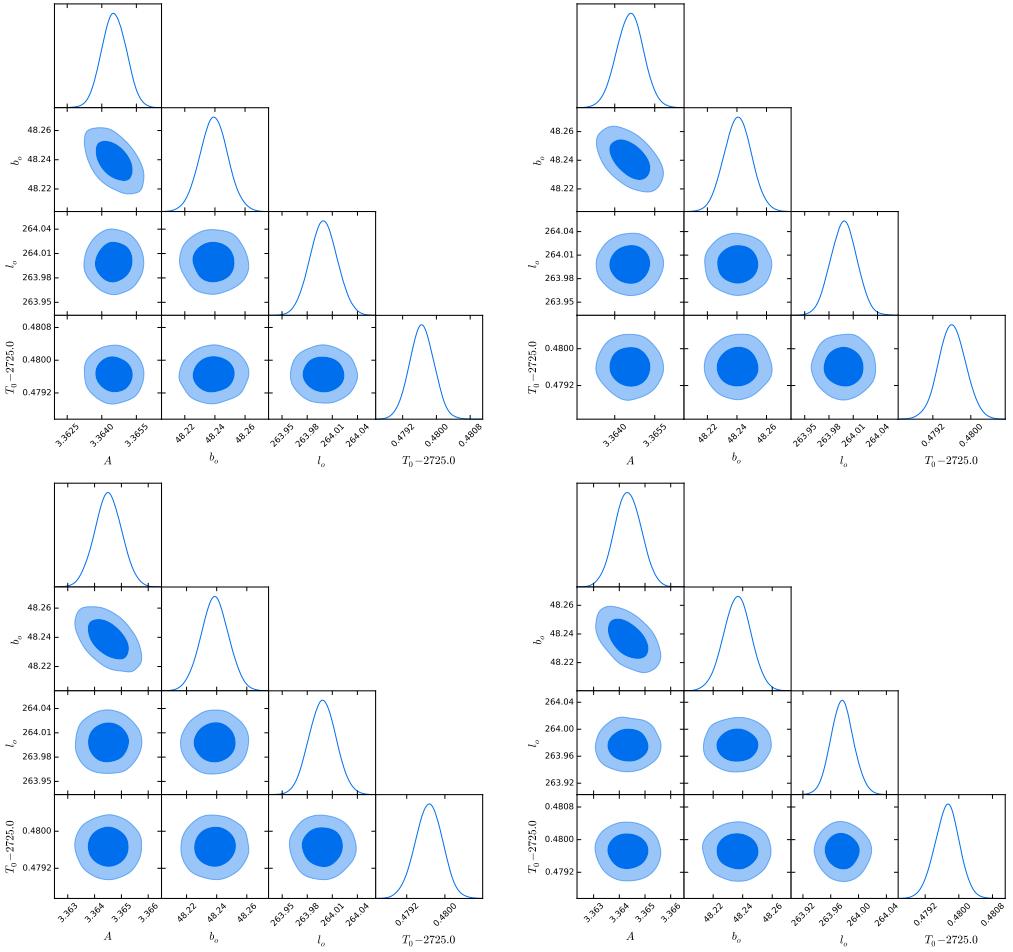


Figure 16. Marginalised likelihoods, and 68% and 95% contours of the parameters A , b_0 , l_0 , and T_0 . Input maps are at $N_{\text{side}} = 1024$, with noise, mask and residuals (calibration errors and sky residuals). *Top:* 100 GHz with optimistic (left) and pessimistic (right) systematics. *Bottom:* 220 GHz with optimistic (left) and pessimistic (right) systematics.

$N_{\text{side}} = 1024$	$A(\text{mK})$	$b_0(^{\circ})$	$l_0(^{\circ})$	$T_0(\text{mK})$
60 GHz, good sys	3.36454 ± 0.00052	48.2387 ± 0.0093	263.999 ± 0.016	2725.47965 ± 0.00029
60 GHz, bad sys	3.36451 ± 0.00052	48.2352 ± 0.0092	264.000 ± 0.016	2725.47965 ± 0.00029
100 GHz, good sys	3.36453 ± 0.00053	48.2393 ± 0.0093	264.000 ± 0.016	2725.47965 ± 0.00029
100 GHz, bad sys	3.36457 ± 0.00051	48.2406 ± 0.0093	263.998 ± 0.016	2725.47961 ± 0.00029
145 GHz, good sys	3.36452 ± 0.00052	48.2391 ± 0.0093	263.999 ± 0.017	2725.47967 ± 0.00029
145 GHz, bad sys	3.36434 ± 0.00051	48.2391 ± 0.0091	263.996 ± 0.017	2725.47965 ± 0.00029
220 GHz, good sys	3.36451 ± 0.00051	48.2387 ± 0.0092	263.998 ± 0.016	2725.47966 ± 0.00029
220 GHz, bad sys	3.36434 ± 0.00052	48.2364 ± 0.0094	263.977 ± 0.016	2725.47972 ± 0.00029

Table 13. 68 % confidence level of the parameters A , b_0 , l_0 , and T_0 at 60, 100, 145 and 220 GHz (see figure 16 for the likelihoods at 100 and 220 GHz).

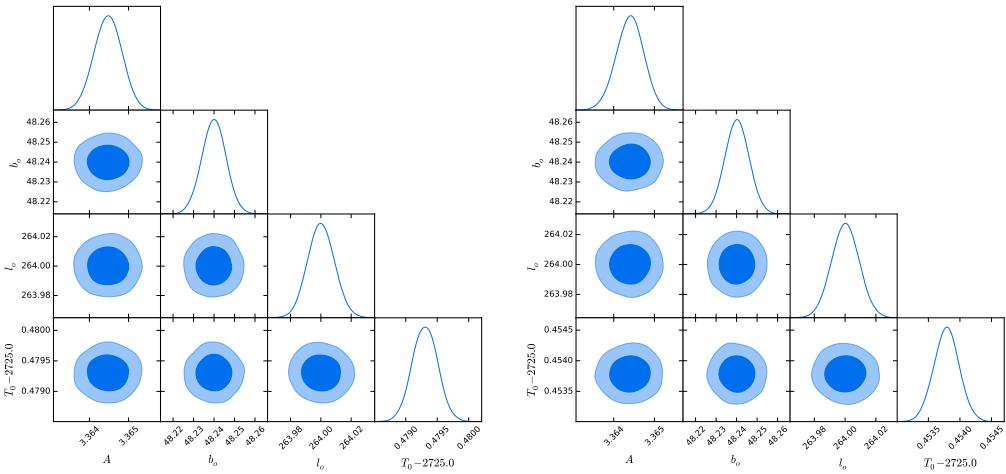


Figure 17. Marginalised likelihoods, and 68% and 95% contours of the parameters A , b_0 , l_0 , and T_0 . Input maps are dipole-only, at 60 GHz and at $N_{\text{side}} = 1024$. On the left: blackbody. On the right: Bose-Einstein (chemical potential $\mu_0 = 1.4 \times 10^{-5}$).

$N_{\text{side}} = 1024$	$A(\text{mK})$	$b_0(^{\circ})$	$l_0(^{\circ})$	$T_0(\text{mK})$
blackbody	3.36447 ± 0.00036	48.2399 ± 0.0060	264.0002 ± 0.0088	2725.47930 ± 0.00020
Bose-Einstein	3.36440 ± 0.00034	48.2402 ± 0.0059	264.0002 ± 0.0090	2725.45379 ± 0.00020

Table 14. 68 % confidence level of the parameters A , b_0 , l_0 , and T_0 of figure 17.

B Rms values from Monte Carlo simulations: ideal case

We present here the tables with the estimates of the rms of the $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ quoted from a Monte Carlo simulation at $N_{\text{side}} = 64$, using all-sky maps and adopting perfect foreground subtraction and calibration.

Rms of σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})	$(\Delta\varepsilon/\varepsilon_i)_{z_1}$								$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$	
			I_0^{bf}		$+1\sigma$		-1σ		μ_0		μ_0	
			1.3	1.7	0.9	1.12 $\times 10^{-7}$	1.4 $\times 10^{-5}$	1.4 $\times 10^{-6}$	1.4 $\times 10^{-9}$	2.8 $\times 10^{-8}$	-2.8 $\times 10^{-9}$	10 $^{-7}$
Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
(1)	0	4.83	6.99	3.16	0.872	0.568	0.621	0.129	0.562	0.183	0.976	1.06
(2)	4.22	0	4.22	0.00	4.22	5.27	5.16	4.22	4.22	4.22	5.16	5.16
(3)	6.99	3.16	0	5.16	6.99	4.22	6.99	6.99	6.99	6.99	6.99	6.75
(4)	0.00	3.16	5.16	0	0.00	4.22	3.16	0.00	0.00	0.00	3.16	0.00
(5)	1.06	4.83	6.99	3.16	0	0.675	0.621	1.06	0.976	1.07	1.05	1.06
(6)	0.667	6.75	6.32	4.22	0.738	0	0.823	0.667	0.738	0.568	0.667	1.08
(7)	0.636	4.83	6.75	3.16	0.636	0.675	0	0.636	0.632	0.635	0.657	1.14
(8)	0.129	4.83	6.99	3.16	0.871	0.568	0.610	0	0.549	0.224	0.976	1.06
(9)	0.578	4.83	6.99	3.16	0.813	0.675	0.619	0.564	0	0.606	0.993	1.06
(10)	0.182	4.83	6.99	3.16	0.873	0.667	0.613	0.223	0.587	0	0.974	1.06
(11)	1.04	5.16	6.75	3.16	1.14	0.568	0.620	1.05	1.07	1.04	0	0.994
(12)	0.994	5.16	6.32	3.16	0.919	1.05	1.08	0.994	1.07	0.994	0.966	0

Table 15. Rms values of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ from a Monte Carlo simulation at $N_{\text{side}} = 64$, full sky, adopting perfect foreground subtraction and calibration, and considering each of the 19 frequency channels.

Rms of σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$						$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$			
		I_0^{bf}	$+1\sigma$		-1σ		8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}
			1.3	1.7	0.9					μ_0				u
Case	(1)	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
(1)	0.00	31.6	42.2	14.8	2.93	2.67	2.52	0.342	1.52	0.485	2.89	2.18		
(2)	31.6	0	6.75	6.67	0.00	51.6	0.00	31.6	0.00	31.6	31.6	31.6	31.6	31.6
(3)	42.2	5.16	0	8.43	42.2	42.2	31.6	42.2	42.2	42.2	42.2	42.2	51.6	51.6
(4)	10.8	8.23	11.4	0	10.8	12.9	12.9	10.8	10.8	10.8	10.8	11.7	12.9	
(5)	3.11	31.6	42.2	14.8	0	2.59	2.53	3.09	2.70	3.15	4.15	2.20		
(6)	2.30	51.6	42.2	14.5	2.49	0	2.33	2.33	2.67	2.30	2.50	2.46		
(7)	2.59	31.6	31.6	14.5	2.64	2.56	0	2.62	2.60	2.60	2.58	2.31		
(8)	0.343	31.6	42.2	14.8	2.91	2.56	2.51	0	1.48	0.594	2.91	2.19		
(9)	1.56	31.6	42.2	14.8	2.58	2.59	2.53	1.52	0	1.63	3.29	2.20		
(10)	0.484	31.6	42.2	14.8	2.96	2.67	2.53	0.593	1.60	0	2.85	2.18		
(11)	2.39	31.6	42.2	14.8	2.93	2.81	2.48	2.40	2.60	2.36	0	2.20		
(12)	2.10	31.6	52.7	14.0	2.13	2.59	2.30	2.09	2.12	2.12	2.10	0		

Table 16. The same as in table 15, but considering all 171 independent combinations of pairs of different frequency channels.

Rms of σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$						$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$			
		I_0^{bf}	$+1\sigma$		-1σ		8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}
			1.3	1.7	0.9					μ_0				u
Case	(1)	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
(1)	0	52.7	31.6	31.6	2.69	2.17	2.14	0.340	1.50	0.482	1.40	1.57		
(2)	51.6	0	8.43	6.75	51.6	0.00	51.6	51.6	51.6	51.6	51.6	51.6	31.6	
(3)	31.6	5.16	0	11.0	31.6	52.7	31.6	31.6	31.6	31.6	31.6	31.6	51.6	51.6
(4)	31.6	6.32	12.6	0	31.6	0.00	0.00	31.6	31.6	31.6	31.6	31.6	51.6	51.6
(5)	3.10	52.7	31.6	31.6	0	2.28	2.14	3.08	2.68	3.14	2.15	1.40		
(6)	2.20	0.00	48.3	31.6	2.21	0	2.17	2.06	2.21	2.20	2.21	2.21	2.59	
(7)	2.23	51.6	31.6	31.6	2.23	2.27	0	2.22	2.22	2.22	2.22	2.57	1.65	
(8)	0.340	52.7	31.6	31.6	2.68	2.17	2.12	0	1.46	0.591	1.40	1.57		
(9)	1.53	52.7	31.6	31.6	2.40	2.28	2.16	1.49	0	1.61	1.58	1.57		
(10)	0.481	52.7	31.6	31.6	2.72	2.31	2.14	0.589	1.57	0	1.38	1.57		
(11)	1.48	51.6	31.6	31.6	2.15	2.18	2.48	1.49	1.65	1.46	0	1.57		
(12)	1.23	31.6	52.7	51.6	1.58	2.72	1.87	1.23	1.23	1.23	1.23	0		

Table 17. The same as in table 15, but considering each of the 19 frequency channels and all 171 independent combinations of pairs of different frequency channels.

C Ideal case at high resolution

We repeat here the same analysis carried out in the previous section, but now working at $N_{\text{side}} = 512$, i.e., at about 7 arcmin resolution, and considering a single realization. The results are reported in table 18 relative to approach (c).

σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$						$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$			
		I_0^{bf}	$+1\sigma$		-1σ		8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}
			1.3	1.7	0.9	1.12 $\times 10^{-7}$							10^{-7}	2×10^{-6}
Case	(1)	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
(1)	0	14400	18800	10100	-1.39	320.	30.5	-0.326	-1.31	0.467	8.65	161.		
(2)	14500	0	4380	4380	14500	14500	14500	14500	14500	14500	14500	14500	14400	
(3)	18800	4330	0	8710	18800	18800	18800	18800	18800	18800	18800	18800	18800	
(4)	10100	4380	8710	0	10100	10100	10100	10100	10100	10100	10100	10100	10000	
(5)	3.90	14400	18800	10100	0	317.	27.9	3.86	3.19	3.97	9.06	160.		
(6)	323.	14500	10100	10100	321.	0	291.	323.	323.	323.	322.	332.		
(7)	33.8	18800	18800	10100	31.2	288.	0	33.8	33.1	33.8	33.4	158.		
(8)	0.329	14400	18800	10100	-1.41	320.	30.4	0	-1.29	0.575	8.66	161.		
(9)	1.60	14400	18800	10100	-1.64	319.	29.8	1.55	0	1.69	8.69	160.		
(10)	-0.458	14400	18800	10100	-1.35	320.	30.5	-0.559	-1.36	0	8.65	161.		
(11)	7.27	14400	18800	10100	6.56	318.	29.7	7.26	7.01	7.30	0	153.		
(12)	159.	14500	18800	10000	159.	328.	156.	159.	159.	159.	151.	0		

Table 18. Values of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ for a single realization at $N_{\text{side}} = 512$, for the full sky, adopting perfect foreground subtraction and calibration, and considering each of the 19 frequency channels and all 171 independent combinations of pairs of different frequencies.

D Rms values from Monte Carlo simulations: including potential residuals

We report here tables with the estimates of the rms of the $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ quoted from a Monte Carlo simulation at $N_{\text{side}} = 64$, with all-sky data, and including potential foreground and calibration residuals.

Rms of σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$						$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$			
		I_0^{bf}	$+1\sigma$		-1σ		8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}
			1.3	1.7	0.9	1.12 $\times 10^{-7}$							10^{-7}	2×10^{-6}
Case	(1)	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
(1)	0	0.798	0.804	0.802	0.274	0.471	0.673	0.0308	0.137	0.0435	0.416	0.469		
(2)	0.838	0	0.792	0.973	0.846	0.637	0.819	0.838	0.838	0.838	0.838	0.701		
(3)	0.829	0.981	0	0.871	0.829	0.682	0.806	0.829	0.829	0.829	0.829	0.823	0.753	
(4)	0.859	0.788	0.799	0	0.857	0.578	0.837	0.859	0.860	0.859	0.841	0.667		
(5)	0.276	0.798	0.804	0.800	0	0.480	0.746	0.274	0.239	0.280	0.359	0.472		
(6)	0.490	0.605	0.657	0.529	0.495	0	0.486	0.490	0.480	0.481	0.484	0.509		
(7)	0.788	0.795	0.808	0.768	0.775	0.477	0	0.788	0.784	0.789	0.775	0.474		
(8)	0.0308	0.798	0.804	0.802	0.272	0.471	0.673	0	0.134	0.0533	0.415	0.470		
(9)	0.138	0.798	0.804	0.802	0.237	0.478	0.702	0.134	0	0.145	0.399	0.469		
(10)	0.0435	0.798	0.804	0.802	0.277	0.486	0.670	0.0533	0.144	0	0.418	0.469		
(11)	0.455	0.798	0.798	0.784	0.383	0.482	0.768	0.454	0.437	0.457	0	0.469		
(12)	0.539	0.709	0.733	0.624	0.542	0.525	0.591	0.539	0.539	0.538	0.543	0		

Table 19. Rms values of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ from a Monte Carlo simulation at $N_{\text{side}} = 64$, full sky, adopting $E_{\text{for}} = 10^{-2}$ and $E_{\text{cal}} = 10^{-4}$, and considering each of the 19 frequency channels.

Rms of σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$						$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$			
		I_0^{bf}	$+1\sigma$		-1σ		8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}
			1.3	1.7	0.9	1.12 $\times 10^{-7}$	1.4×10^{-5}	1.4×10^{-6}	1.4×10^{-9}	2.8×10^{-8}	-2.8×10^{-9}	10^{-7}	2×10^{-6}	
Case	Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
(1)	0	2.69	2.69	2.68	0.332	1.77	1.34	0.0362	0.164	0.0512	0.359	1.54		
(2)	2.67	0	2.77	2.88	2.67	2.69	2.67	2.67	2.67	2.67	2.67	2.66		
(3)	2.65	2.91	0	2.70	2.64	2.68	2.67	2.65	2.65	2.65	2.65	2.65		
(4)	2.69	2.76	2.70	0	2.69	2.72	2.71	2.69	2.69	2.69	2.69	2.68		
(5)	0.320	2.69	2.69	2.68	0	1.78	1.28	0.318	0.278	0.324	0.483	1.56		
(6)	1.39	2.69	2.71	2.64	1.38	0	1.38	1.39	1.37	1.39	1.38	1.40		
(7)	1.08	2.69	2.69	2.68	1.04	1.85	0	1.08	1.08	1.09	1.12	1.59		
(8)	0.0362	2.69	2.69	2.68	0.329	1.77	1.34	0	0.160	0.0627	0.361	1.54		
(9)	0.161	2.69	2.69	2.68	0.286	1.78	1.33	0.157	0	0.169	0.395	1.55		
(10)	0.0512	2.69	2.69	2.68	0.336	1.77	1.35	0.0629	0.172	0	0.355	1.54		
(11)	0.360	2.69	2.72	2.67	0.491	1.77	1.38	0.362	0.397	0.356	0	1.51		
(12)	1.64	2.69	2.69	2.66	1.68	1.79	2.08	1.64	1.65	1.64	1.60	0		

Table 20. The same as in table 19, but considering all 171 independent combinations of pairs of different frequency channels.

Rms of σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$						$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$			
		I_0^{bf}	$+1\sigma$		-1σ		8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}
			1.3	1.7	0.9	1.12 $\times 10^{-7}$	1.4×10^{-5}	1.4×10^{-6}	1.4×10^{-9}	2.8×10^{-8}	-2.8×10^{-9}	10^{-7}	2×10^{-6}	
Case	Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
(1)	0	2.79	2.82	2.79	0.411	1.10	1.48	0.0458	0.205	0.0647	0.469	0.638		
(2)	2.79	0	2.87	3.03	2.79	2.74	2.78	2.79	2.79	2.79	2.79	2.75		
(3)	2.77	3.04	0	2.84	2.76	2.75	2.79	2.76	2.76	2.77	2.77	2.75		
(4)	2.82	2.86	2.81	0	2.82	2.73	2.82	2.82	2.82	2.82	2.80	2.74		
(5)	0.406	2.79	2.79	2.78	0	1.10	1.43	0.404	0.352	0.411	0.534	0.649		
(6)	1.02	2.71	2.76	2.62	1.02	0	1.01	1.02	1.02	1.02	1.02	1.34		
(7)	1.18	2.79	2.79	2.78	1.14	1.10	0	1.18	1.17	1.18	1.21	0.853		
(8)	0.0457	2.79	2.82	2.79	0.409	1.10	1.48	0	0.199	0.0794	0.470	0.638		
(9)	0.204	2.79	2.82	2.79	0.356	1.08	1.47	0.199	0	0.214	0.475	0.642		
(10)	0.0647	2.79	2.82	2.79	0.417	1.10	1.48	0.0794	0.215	0	0.467	0.637		
(11)	0.503	2.81	2.82	2.78	0.547	1.11	1.54	0.503	0.513	0.502	0	0.636		
(12)	0.842	2.76	2.78	2.74	0.876	1.55	1.87	0.843	0.849	0.840	0.859	0		

Table 21. The same as in table 19, but considering each of the 19 frequency channels and all 171 independent combinations of pairs of different frequency channels.

E Results for different assumptions on potential foreground and calibration residuals

We report here some of the results discussed in section 7.2.3.

σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})	$(\Delta\varepsilon/\varepsilon_i)_{z_1}$							$(\Delta\varepsilon/\varepsilon_i)_{late}$	
			8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}	
			I_0^{bf}	$+1\sigma$	-1σ	μ_0					u
Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11) (12)
(1)	0.00	700.	911.	487.	0.859	75.7	7.85	0.0689	0.341	-0.0956	2.35 30.7
(2)	699.	0.00	211.	213.	699.	715.	700.	699.	699.	699.	699. 696.
(3)	910.	211.	0.00	424.	910.	926.	911.	910.	910.	910.	910. 907.
(4)	486.	213.	424.	0.00	486.	504.	487.	486.	486.	486.	486. 483.
(5)	-0.103	700.	911.	487.	0.00	75.1	7.24	-0.122	-0.276	-0.0379	2.19 30.5
(6)	75.1	716.	926.	505.	74.5	0.00	67.6	75.1	75.0	75.1	74.6 69.5
(7)	7.23	701.	912.	488.	6.62	68.2	0.00	7.22	7.07	7.24	7.00 28.7
(8)	-0.0680	700.	911.	487.	0.851	75.7	7.84	0.00	0.331	-0.116	2.35 30.7
(9)	-0.266	700.	911.	487.	0.697	75.6	7.70	-0.262	0.00	-0.275	2.30 30.7
(10)	0.0979	700.	911.	487.	0.875	75.7	7.86	0.121	0.361	0.00	2.35 30.8
(11)	-1.06	700.	911.	487.	-1.04	75.1	7.19	-1.06	-1.09	-1.05	0.00 29.3
(12)	28.5	697.	907.	484.	28.3	69.3	26.4	28.5	28.5	27.0	0.00

Table 22. Values of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ for a single realization at $N_{\text{side}} = 64$, using *Planck* mask-76 extended to exclude regions at $|b| \leq 30^\circ$. We adopt $E_{\text{for}} = 10^{-3}$ and $E_{\text{cal}} = 10^{-4}$, and consider each of the 19 frequency channels and all 171 independent combinations of pairs of different frequencies.

σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})	$(\Delta\varepsilon/\varepsilon_i)_{z_1}$							$(\Delta\varepsilon/\varepsilon_i)_{late}$	
			8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}	
			I_0^{bf}	$+1\sigma$	-1σ	μ_0					u
Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11) (12)
(1)	0	65.2	84.3	46.0	-0.193	7.80	0.376	-0.0227	-0.101	0.0322	0.563 3.96
(2)	61.2	0	20.9	17.1	61.2	63.0	61.3	61.2	61.2	61.2	61.2 60.9
(3)	80.3	17.0	0	36.3	80.3	82.0	80.4	80.3	80.3	80.3	80.2 79.9
(4)	41.9	21.1	40.2	0	41.9	44.0	42.1	41.9	41.9	41.9	41.9 41.7
(5)	0.214	65.2	84.3	46.0	0	7.73	0.286	0.212	0.183	0.217	0.595 3.94
(6)	8.44	67.0	86.0	48.0	8.37	0	7.62	8.44	8.42	8.44	8.39 8.11
(7)	1.09	65.3	84.4	46.1	1.02	6.98	0	1.08	1.07	1.09	1.18 3.84
(8)	0.0228	65.2	84.3	46.0	-0.192	7.80	0.375	0	-0.0980	0.0395	0.563 3.96
(9)	0.103	65.2	84.3	46.0	-0.169	7.78	0.355	0.100	0	0.108	0.570 3.95
(10)	-0.0322	65.2	84.3	46.0	-0.195	7.80	0.378	-0.0394	-0.105	0	0.562 3.96
(11)	-0.517	65.2	84.2	45.9	-0.560	7.71	-0.481	-0.518	-0.529	-0.516	0 3.80
(12)	2.00	64.8	83.9	45.6	1.94	6.61	1.42	1.99	1.98	2.00	1.82 0

Table 23. Values of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ for a single realization at $N_{\text{side}} = 64$, using *Planck* mask-76 extended to exclude regions at $|b| \leq 30^\circ$. We adopt $E_{\text{for}} = 10^{-2}$ and $E_{\text{cal}} = 10^{-3}$ at $\nu \leq 295$ GHz and $E_{\text{cal}} = 10^{-2}$ at $\nu \geq 340$ GHz, and consider each of the 19 frequency channels and all 171 independent combinations of pairs of different frequencies.

σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$							$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$	
		I_0^{bf}	$+1\sigma$	-1σ	8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}	
		1.3	1.7	0.9	1.12×10^{-7}	1.4×10^{-5}	1.4×10^{-6}	1.4×10^{-9}	2.8×10^{-8}	-2.8×10^{-9}	10^{-7}	2×10^{-6}	
Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
(1)	0	161.	209.	112.	-0.601	8.97	-1.83	-0.0680	-0.303	0.0962	0.963	6.15	
(2)	157.	0	49.8	46.4	157.	160.	157.	157.	157.	157.	157.	156.	
(3)	205.	45.9	0	94.4	205.	208.	205.	205.	205.	205.	205.	204.	
(4)	109.	50.2	98.2	0	109.	112.	109.	109.	109.	109.	109.	108.	
(5)	0.615	161.	209.	112.	0	8.88	-1.78	0.611	0.531	0.622	1.14	6.17	
(6)	13.1	164.	212.	116.	13.1	0	12.0	13.1	13.1	13.2	13.1	13.8	
(7)	2.43	161.	209.	113.	2.31	7.81	0	2.43	2.40	2.43	2.59	6.46	
(8)	0.0680	161.	209.	112.	-0.598	8.97	-1.83	0	-0.296	0.118	0.966	6.15	
(9)	0.305	161.	209.	112.	-0.522	8.95	-1.82	0.297	0	0.320	1.01	6.15	
(10)	-0.0961	161.	209.	112.	-0.609	8.97	-1.83	-0.118	-0.318	0	0.959	6.15	
(11)	-0.909	161.	209.	112.	-1.09	8.87	-2.07	-0.912	-0.959	-0.904	0	5.91	
(12)	1.65	160.	208.	111.	1.48	8.00	-1.60	1.64	1.61	1.65	1.27	0	

Table 24. Values of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ for a single realization at $N_{\text{side}} = 64$, using *Planck* mask-76 extended to exclude regions at $|b| \leq 30^\circ$. We adopt $E_{\text{for}} = 10^{-3}$ and $E_{\text{cal}} = 10^{-3}$ at $\nu \leq 295$ GHz and $E_{\text{cal}} = 10^{-2}$ at $\nu \geq 340$ GHz, and consider each of the 19 frequency channels and all 171 independent combinations of pairs of different frequencies.

σ level significance	Current blackbody	FIRAS CIB amplitude (units 10^{-5})			$(\Delta\varepsilon/\varepsilon_i)_{z_1}$							$(\Delta\varepsilon/\varepsilon_i)_{\text{late}}$	
		I_0^{bf}	$+1\sigma$	-1σ	8×10^{-8}	10^{-5}	10^{-6}	10^{-9}	2×10^{-8}	-2×10^{-9}	4×10^{-7}	8×10^{-6}	
		1.3	1.7	0.9	1.12×10^{-7}	1.4×10^{-5}	1.4×10^{-6}	1.4×10^{-9}	2.8×10^{-8}	-2.8×10^{-9}	10^{-7}	2×10^{-6}	
Case	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	
(1)	0	286.	371.	200.	-1.12	48.6	2.74	-0.133	-0.589	0.189	2.12	21.3	
(2)	278.	0	88.9	81.7	278.	289.	278.	278.	278.	278.	278.	276.	
(3)	363.	81.0	0	167.	363.	373.	364.	363.	363.	363.	363.	361.	
(4)	192.	89.7	175.	0	192.	205.	193.	192.	192.	192.	192.	191.	
(5)	1.26	286.	371.	200.	0	48.2	2.25	1.25	1.08	1.28	2.38	21.2	
(6)	52.1	297.	381.	213.	51.7	0	47.1	52.1	52.0	52.1	51.6	46.2	
(7)	6.57	286.	371.	201.	6.15	43.5	0	6.57	6.47	6.58	6.52	19.9	
(8)	0.134	286.	371.	200.	-1.12	48.5	2.74	0	-0.574	0.232	2.12	21.3	
(9)	0.606	286.	371.	200.	-0.989	48.5	2.62	0.590	0	0.636	2.18	21.3	
(10)	-0.189	286.	371.	200.	-1.14	48.6	2.75	-0.231	-0.617	0	2.11	21.3	
(11)	-1.60	286.	371.	200.	-2.06	48.0	-0.489	-1.61	-1.74	-1.59	0	20.3	
(12)	17.7	284.	369.	199.	17.4	40.4	14.8	17.7	17.6	17.7	16.7	0	

Table 25. Values of $\sqrt{|\Delta\chi^2|} \text{ sign}(\Delta\chi^2)$ for a single realization at $N_{\text{side}} = 256$, using *Planck* mask-76 extended to exclude regions at $|b| \leq 30^\circ$. We adopt $E_{\text{for}} = 10^{-3}$ and $E_{\text{cal}} = 10^{-3}$ at $\nu \leq 295$ GHz and $E_{\text{cal}} = 10^{-2}$ at $\nu \geq 340$ GHz, and consider each of the 19 frequency channels and all 171 independent combinations of pairs of different frequencies.

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