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### Water Resources Research



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#### **Kev Points:**

- Differential Split Sample Testing of hydrological models should include use of best available analogues of expected climate changes
- For climate impact assessment use a multimodel ensemble with an objective averaging technique to combine members
- Evaluate parameter and model transferability using a range of climate analogues, catchment types, and performance criteria

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### **RESEARCH ARTICLE**

### methods between contrasting climatic periods Ciaran Broderick<sup>1</sup>, Tom Matthews<sup>2</sup>, Robert L. Wilby<sup>3</sup>, Satish Bastola<sup>4</sup>, and Conor Murphy<sup>1</sup>

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Transferability of hydrological models and ensemble averaging

Abstract Understanding hydrological model predictive capabilities under contrasting climate conditions enables more robust decision making. Using Differential Split Sample Testing (DSST), we analyze the performance of six hydrological models for 37 Irish catchments under climate conditions unlike those used for model training. Additionally, we consider four ensemble averaging techniques when examining interperiod transferability. DSST is conducted using 2/3 year noncontinuous blocks of (i) the wettest/driest years on record based on precipitation totals and (ii) years with a more/less pronounced seasonal precipitation regime. Model transferability between contrasting regimes was found to vary depending on the testing scenario, catchment, and evaluation criteria considered. As expected, the ensemble average outperformed most individual ensemble members. However, averaging techniques differed considerably in the number of times they surpassed the best individual model member. Bayesian Model Averaging (BMA) and the Granger-Ramanathan Averaging (GRA) method were found to outperform the simple arithmetic mean (SAM) and Akaike Information Criteria Averaging (AICA). Here GRA performed better than the best individual model in 51%-86% of cases (according to the Nash-Sutcliffe criterion). When assessing model predictive skill under climate change conditions we recommend (i) setting up DSST to select the best available analogues of expected annual mean and seasonal climate conditions; (ii) applying multiple performance criteria; (iii) testing transferability using a diverse set of catchments; and (iv) using a multimodel ensemble in conjunction with an appropriate averaging technique. Given the computational efficiency and performance of GRA relative to BMA, the former is recommended as the preferred ensemble averaging technique for climate assessment.

### 1. Introduction

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Evaluating hydrological responses to climate change is an important area of research. Conventional impact assessments typically involve the following: (i) projecting climate responses using General Circulation Model (GCM) simulations forced by greenhouse gas emission scenarios; (ii) postprocessing/downscaling GCM output; and (iii) estimating catchment scale impacts using hydrological models. This top-down approach introduces uncertainties at each step which vary depending on factors including the catchment and regional climate characteristics. Even so-called stress testing (or sensitivity-based) techniques—which move away from direct reliance on GCMs—are subject to uncertainties in hydrological model structures and parameter sets [Prudhomme et al., 2010, 2015; Whateley et al., 2014; Wilby et al., 2014].

Hydrological model uncertainty stems from errors in input (e.g., precipitation) and output (e.g., streamflow) data, as well as from deficiencies in model structures and nonuniqueness of model parameters. Previous studies have encountered difficulties when addressing structural uncertainty, particularly when trying to identify a single, optimum model for a given catchment type [Clark et al., 2008; van Esse et al., 2013; Coxon et al., 2014]. Similarly, uncertainty relating to model calibration/training arises due to equifinality or the inability to determine a globally optimum parameter set [Beven, 2006]. For climate impact studies, additional uncertainties arise due to hydrological models being applied to conditions outside those used for model training. Hence, the assumption of parametric stationarity—whereby parameters provide realistic simulations when applied under hydroclimatological conditions dissimilar to those used for model development—has been widely questioned. A number of authors have called for a more rigorous and systematic approach to interrogating transferability and model robustness for climate impact studies [Hartmann and

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Bárdossy, 2005; Wilby, 2005; Beven, 2006; Wilby and Harris, 2006; Andréassian et al., 2009; Vaze et al., 2010; Merz et al., 2011; Coron et al., 2012; Li et al., 2012; Seiller et al., 2012, 2015; Brigode et al., 2013; Westra et al., 2014; Thirel et al., 2015a, 2015b].

Studies employing Differential Split Sample Testing (DSST) [Klemeš, 1986] show dependence of model parameters on the climate and meteorological conditions dominating the training period and their role in activating different rainfall-runoff processes [Wagener, 2003; Choi and Beven, 2007; Herman et al., 2013]. One consequence is that identification of a "best" hydrological model becomes intractable, as relative performances vary in time. This highlights the importance of employing a multiple rather than single model strategy and understanding potential deficiencies in model performance when extrapolated beyond training conditions. Such difficulties are further compounded by the absence of universally accepted metrics to benchmark performance [Krause et al., 2005]. Model ensembles that better characterize the structural uncertainty space are one practical solution; the ensemble may reflect the strengths of individual models which may each omit or provide a biased representation of system processes. The importance of including model components which capture processes associated with particular catchment types—as a means to improving performance and physical realism in the structure—is demonstrated by previous multimodel studies [van Esse et al., 2013; Coxon et al., 2014]. While previous research shows that using a multimodel ensemble is superior to relying on an individual model, the best way of combining ensemble members remains an area of active research [e.g., Shamseldin et al., 1997; Abrahart and See, 2002; Ajami et al., 2006; Hansen, 2008; Diks and Vrugt, 2010; Arsenault et al., 2015].

Only when critical uncertainties have been addressed [Clark et al., 2016], and sufficient testing has been conducted to establish performance under a range of conditions, can model projections be used to make well informed adaptation decisions (including under "stress test" conditions). To this end, the present study uses DSST to examine temporal transferability of a multimodel hydrological ensemble. The study has two aims. First, we analyze the performance of six lumped conceptual rainfall-runoff (CRR) models applied under climate conditions that differ from those used for model training, for catchments across the Island of Ireland (IoI). Previous studies have assessed climate change impacts on Irish catchments [Steele-Dunne et al., 2008; Bastola et al., 2011, 2012], but systematic appraisal of model transferability has yet to be undertaken. In addition, there is limited information about which model(s) perform best across catchments with contrasting hydrological and climate characteristics. Second, we examine through comparison of multiple methods, the extent to which an ensemble offers improved transferability beyond reliance on individual model structures. This study expands on existing research [Vaze et al., 2010; Merz et al., 2011; Coron et al., 2012; Li et al., 2012]—and the work of Seiller et al., [2012, 2015] in particular—by contributing to knowledge of model limitations under nonstationary conditions. In particular, we quantify how model performance may be diminished by transference and whether this is greater with respect to wetter/drier conditions and specific seasonal precipitation regimes. We also examine the suitability of using observed records as an analogue to determine predictive performance under possible future conditions, demonstrate an approach for training and unbiased model evaluation, and examine methods to improve model application in climate impact studies.

The following section describes the study catchments, hydrological models, and averaging techniques employed. We also outline the criteria for selecting contrasting climate periods. Section 3 presents the results of the analyses. Section 4 discusses the new insights gained from the transferability and ensemble averaging assessment before suggesting priorities for further research.

### 2. Methods

### 2.1. Study Catchments and Data

The study was undertaken using 37 catchments from Iol (Figure 1; Table 1): 35 from the Irish Reference Network (IRN) [*Murphy et al.*, 2013]; two from the UK Benchmark Network [*Hannaford and Marsh*, 2008]. These catchments have near natural flow regimes, are minimally influenced by human activity and possess quality-assured, long-term observational records. Catchments along the western seaboard are more exposed to Atlantic weather systems and subject to more pronounced orographic enhancement. As a result they tend to have higher annual precipitation totals.



Figure 1. Study catchments and Met Éireann synoptic stations. Catchment identification codes are shown; red lines denote the respective catchment boundaries.

Daily streamflow, precipitation and potential evapotranspiration (PET) data for the period 1970–2010 were used. Observed streamflow data for the Republic of Ireland were provided by the Office of Public Works (OPW; http://www.opw.i.e./hydro/) and the Environmental Protection Agency. Data for Northern Ireland (Gauge ID 201008 and 201005) were obtained from the UK National River Flow Archive (http://nrfa.ceh.ac. uk/). Not all catchments have continuous records for the study period, hence model transferability was only assessed using periods with at least 90% data coverage.

Catchment average rainfall was estimated from a quality-assured 1 km  $\times$  1 km gridded data set provided by Met Éireann [*Walsh*, 2012]. Daily PET, estimated via the Penman method [*Allen et al.*, 1998], was also provided by Met Éireann for the closest synoptic station to each catchment centroid (Figure 1). Gaps in the records were infilled through regression with highly correlated (Pearson's coefficient >0.7) neighboring stations. Additionally, to ensure a robust statistical relationship donor sites that provided an overlapping period of >5 years were selected.

No previous study has developed a typology of catchments for lol [e.g., *Chiverton et al.*, 2015]. Here we use the Base Flow Index (BFI) to characterize differences in our catchment sample. The BFI is defined as the proportion of catchment outflow derived from saturated groundwater storage or base flow as opposed to direct runoff [*Sear et al.*, 1999]. Generally, catchments with a high BFI have greater recharge and storage capacity, and thus potential to sustain flow during drier periods. Such catchments also tend to have a slower (i.e., time to peak) and more damped response to storm events [*Chiverton et al.*, 2015]. While the

Table 1. Hydroclimatic and Physical Descriptors for the 37 Selected Catchments<sup>a</sup>

_						Precipitation (mm) 1976–2005			
Gauge ID	Area (km²)	Mean Elevation (m)	BFI	(mm yr <sup><math>-1</math></sup> )	Start Date	Annual	Winter	Summer	
6013	308	84	0.60	432	Jul-75	881	497	384	
6014	270	84	0.61	510	Jun-75	919	526	393	
7009	1683	85	0.70	471	Jan-73	890	496	393	
7012	2460	91	0.68	491	Jan-73	908	508	400	
12001	1031	161	0.69	650	Jan-73	1095	632	463	
14007	114	136	0.62	538	Jan-73	915	520	395	
14019	1702	94	0.65	417	Oct-81	868	486	382	
15001	444	118	0.52	500	Jan-73	971	559	413	
15003	297	209	0.38	634	Oct-73	1027	584	443	
15006	2417	137	0.62	528	Dec-76	975	558	417	
16008	1091	138	0.63	702	May-72	1037	606	431	
16009	1583	139	0.64	656	Jan-73	1078	632	445	
18002	2329	165	0.62	807	Jul-77	1267	773	495	
18003	1257	181	0.54	873	Jan-73	1357	845	511	
18005	378	158	0.71	725	Jan-73	1189	699	491	
18006	1055	188	0.50	975	Jan-73	1379	862	517	
18050	250	210	0.38	1073	Jan-72	1588	999	589	
19001	103	100	0.59	744	May-81	1236	753	483	
21002	66	247	0.21	2031	Jan-73	2277	1422	855	
23002	647	196	0.28	1082	Oct-75	1443	880	563	
25001	647	153	0.53	758	Jan-73	1185	679	505	
25002	222	190	0.48	854	Oct-75	1291	742	550	
25006	1188	89	0.69	460	Jan-73	922	515	406	
25030	278	136	0.54	918	Feb-80	1196	703	493	
26009	90	91	0.43	570	Jan-73	1065	609	456	
26021	1072	90	0.82	559	Jan-73	967	547	420	
26029	117	217	0.23	1308	Jan-73	1569	923	646	
27002	511	73	0.70	651	Jan-73	1319	787	532	
32012	145	131	0.56	1285	Jan-73	1690	1027	663	
34001	1971	81	0.77	907	Jan-73	1334	811	523	
35002	76	198	0.40	1352	Jan-73	1631	984	647	
35005	639	100	0.63	820	Jan-73	1268	747	521	
36010	771	124	0.60	580	Jan-73	1028	584	444	
38001	111	186	0.26	1528	Nov-76	1899	1140	759	
39006	245	131	0.46	1129	Jan-73	1530	929	601	
201005	277	163	0.47	793	Jan-74	1141	649	492	
201008	335	172	0.32	1340	Jan-73	1676	1007	668	

<sup>a</sup>Flow indices are estimated from daily data for the period 1974–2010. The Base Flow Index (BFI) is calculated according to *Gustard* et al. [1992]. Mean annual (hydrological year) and 6 month winter/summer (ONDJFM/AMJJAS) precipitation totals for the period 1976–2005 are shown.

extent of surface/groundwater dominance and the associated BFI value is typically linked to catchment geology [*Coxon et al.*, 2014], it is associated with other characteristics including: vegetation, topography, climatic history, land cover, and soil type [*Bloomfield et al.*, 2009; *Price*, 2011]. Our focus on this index follows *Coxon et al.* [2014] who used the index as a key property when differentiating model performance for UK catchments. Similarly, *van* Esse *et al.* [2013] distinguish between groundwater and surface runoff dominated catchments when comparing model structures for 237 French catchments.

The hydrograph separation technique of *Gustard et al.* [1992] is used to estimate the BFI. This involves dividing the discharge series into nonoverlapping, 5 day blocks, then calculating the minimum for each block. Minima less than 0.9 times surrounding 5 day blocks are taken as the base flow separation line. Daily base flow values are estimated using linear interpolation between the identified central minima. Values above observed daily flow are (re)set to the observed value. The index is estimated as the ratio between the total volume of flow and the volume of flow beneath the base flow line. The range of BFI values in our catchment network is shown in Table 1.

### 2.2. Hydrological Models

Six lumped CRR models (NAM, HyMod, Tank, HBV, GR4J, and AWBM) are used to explore transferability under contrasting climate conditions. Developing a competent ensemble necessitates using models of sufficient diversity to ensure structural uncertainty is well represented and the ensemble has good performance

Table 2. Structural Components of the Six Lumped Conceptual Rainfall-Runoff Models<sup>a</sup>

Model	Number of Free Parameters	Represented Catchment Stores	Represented Flow Component/ Routing Mechanism
NAM	9	Surface; root zone; groundwater	Overland (ls); interflow (ls); base flow (ls)
HyMod	5	Soil; "quick" flow reservoirs (×3); "slow" groundwater	Overland (three ls in series); base flow (single ls in parallel)
Tank	15	Soil; intermediate (upper and lower); groundwater	Sum of lateral outflow from each model store
HBV	9	Soil; lower soil; groundwater	Triangular weighting of combined lateral outflow from the lower soil and groundwater store
GR4J	4	Production; routing	10:90 split between direct (uh) and delayed (using a uh and single routing nls) routing
AWBM	10	Variable soil surface stores ( $\times$ 3); surface runoff; groundwater store	Overland (Is); base flow (Is)

<sup>a</sup>Routing mechanisms are abbreviated as unit hydrograph (uh), nonlinear store (nls), and linear store (ls), respectively.

potential under a range of hydroclimatological conditions [*Thiboult et al.*, 2016]. From a structural perspective, the inclusion of "quick" flow pathways through upper layers and routing algorithms that regulate the volume and timing of peak flow events is important in "flashier" catchments. Conversely, structures which provide a better representation of longer-term storage components, with delayed outlet, interstore routing and enhanced infiltration and exchange processes are needed for catchments with higher base flow contributions [*van* Esse *et al.*, 2013]. Hence, selecting physically plausible structures which also provide contrasting conceptualizations and numerical descriptions of the main rainfall-runoff mechanisms were key criteria in model choice. Models were also selected on the basis that they have (i) been used previously in similar intercomparison studies, (ii) demonstrated performance as functional across diverse conditions, and (iii) modest computational/data requirements that are amenable to climate impact assessment [*Bastola et al.*, 2011; *Seiller et al.*, 2012].

Our sample includes complex models with a relatively large number of empirically estimated (free) parameters alongside more parsimonious structures. All were applied in a lumped configuration at a daily time step using the same PET and precipitation inputs. Each model includes routines for evaporative losses and soil moisture accounting. The temperate lol climate means snowfall occurs relatively infrequently and generally remains on the ground for only 1–2 days—although heavier snowfalls can persist for 10–12 days [*Murphy*, 2012; *Sweeney*, 2014]. Consequently, snowpack development is not a significant component of the hydrological regime and thus a snowmelt routine is not included. All models divide saturation excess between slower/quicker responding pathways and allow temporal distribution of individual and combined flow components. They differ in the number/type/configuration of stores (e.g., interception, root zone, and series/parallel), the constituents of total flow included (e.g., interflow and overland flow), and the routing mechanisms employed (e.g., (non)linear storage, unit hydrograph). Full model descriptions can be found in the literature so only a brief synopsis is provided for each below and in Table 2.

*NAM* (Nedbor-Afstromnings-Model) [*Madsen*, 2000] simulates runoff using three storage components: surface storage, root zone storage, and a groundwater store. Stores are depleted through evaporative loss, lateral flow, and infiltration. Overland flow is generated when capacity in the surface store is exceeded. A proportion of this excess also infiltrates to the root and lower groundwater zones. Surface and interflow contributions are routed through two linear reservoirs; base flow is routed through a single linear reservoir.

*HyMod* (Hydrologic Model) [*Wagener et al.*, 2001] has five reservoirs including a nonlinear soil moisture store, three "quick" flow linear reservoirs (in series) and a parallel groundwater reservoir. Actual evapotranspiration depends on saturation of the soil moisture store and evapotranspiration at the potential rate. It is noted that HBV and HyMod share a similar soil moisture accounting routine.

*Tank* [*Sugawara*, 1995], with 15 parameters, is the most complex model employed in the study. It has a hierarchy of four vertical nonlinear storage reservoirs simulating, lateral flow, saturated flow, and unsaturated moisture fluxes. Each tank discharges both vertically and horizontally. Parameters control the height of the horizontal outlet from each tank and their discharge rate; parameters also regulate the vertical infiltration rate. The lateral contribution from successive stores captures total runoff contributions from surface, intermediate, subbase, and base flow, respectively.



**Figure 2.** Flow diagram of the Differential Split Sample Testing (DSST) procedure used—incorporating training and performance assessment for an independent control and testing period, respectively. This DSST procedure is used for estimation of weights in the Generalized Likelihood Uncertainty Estimation (GLUE) procedure (section 2.4) and for model averaging (section 2.5).

*HBV* (Hydrologiska Byråns Vattenbalansavdelning) [*Seibert*, 1996] generates runoff using three storage reservoirs, including a soil moisture zone along with an upper and lower subsurface reservoir. It incorporates a set of runoff response algorithms and a function for streamflow routing. Within HBV groundwater recharge and actual evaporation are estimated as a function of water levels in the upper storage zone. Discharge occurs both laterally—through the lower (one linear outflow) and upper zone (two linear outflows)—and vertically from the upper zone only; a triangular weighting function is used to route their combined outflows.

*GR4J* (Génie Rural à 4 paramètres Journalier) [*Perrin et al.*, 2003] is the most parsimonious structure used, incorporating only four free parameters. Effective rainfall and soil moisture are estimated from net precipitation. Fluxes from the soil moisture zone along with effective rainfall are partitioned as a 10:90 split between two routing channels representing direct and delayed runoff, respectively. The first routing applies a single unit hydrograph and the second a unit hydrograph and nonlinear storage function. Groundwater exchanges with deeper aquifers and/or adjoining catchments are represented using a gain/loss function applied to each routing channel.

*AWBM* (Australian Water Balance Model) [*Boughton*, 2004] uses three area-weighted surface reservoirs with different storage capacities to simulate partial areas of runoff. Water levels in each are iteratively adjusted according to daily rainfall and evaporative loss. The observed input evaporation series is subject to a multiplicative correction factor to adjust for any potential over estimation of PET. This factor is treated as an additional model parameter (sampling range 0.9–1.0) and estimated accordingly (section 2.4). Saturation excess from the soil moisture routine is partitioned and routed between a base flow and surface runoff store; total runoff is taken as their combined outflows.

#### 2.3. Differential Split Sampling

We adopted a modified version of the DSST approach of *Klemeš* [1986] involving an initial fitting or "*train-ing*" procedure, followed by performance evaluation for independent "*control*" conditions (similar to training) and "*testing*" period (representing the opposing precipitation regime to the control). Using the period employed for model training as a benchmark to assess transferability precludes an unbiased estimate of how well models generalize across different climate regimes. Hence, to remove bias toward the training data an independent control period was used. Figure 2 describes the DSST procedure which is applied both for identification of model parameters (section 2.4) and model averaging (section 2.5). Differences in performance between the control (e.g., A in Figure 2) and testing (e.g., B in Figure 2) periods are indicative of transferability when trained under dissimilar conditions (e.g., use B to simulate regime type A in Figure 2).

Two sets of DSST were conducted. First, for each catchment we examined transferability between the "wettest" and "driest" years—identified from total annual precipitation statistics. Second, we examined transferability between years with contrasting annual precipitation patterns. In both cases, hydrological years

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Figure 3. (a, b) Precipitation totals (1974–2010) for the hydrological year (1 October to 30 September; catchment ID 15006). (c) Winter (ONDJFM; x axis) and summer (AMJJAS; y axis) seasonal precipitation for 6 month periods of the hydrological year. Training and testing periods used to assess transferability between "wet"/"dry" (D, W) years (Figures 3a and 3b) are highlighted, as are periods (Figure 3c) used to examine transferability between each of four (DD, WW, DW, and WD) seasonal precipitation regimes.

(1 October to 30 September) were used. For the former, each CRR model was trained using the first, third, and fifth ranked wettest years. Model performance on the second, fourth, and sixth ranked wettest years (taken as the wet period control) provide a benchmark to test the transferability of models trained on the contrasting first, third, and fifth ranked driest years (Figures 3a and 3b). The opposing transferability assessment was also conducted using the 6 driest years. Differences in rainfall (mm yr<sup>-1</sup>) between DSST periods are smallest for Gauge ID 19001 (21/23% drier/wetter) and greatest for Gauge ID 18006 (33/50% drier/wetter). Differences in wet/dry DSST periods relative to the 1976–2005 climatological mean for each catchment are shown in Figure 4a.

Climate model projections suggest wetter winters and drier summers for Iol [*Steele-Dunne et al.*, 2008; *Bastola et al.*, 2011, 2012; *Matthews et al.*, 2016], necessitating transferability of models to an amplified seasonal regime. This is particularly important given how the dynamics of intraseasonal processes during training (the rate, timing, and distribution of storage recharge and reduction through the year) may affect the model response when used to simulate more extreme wetting-up and drying episodes [*Wagener*, 2003; *Herman et al.*, 2013]. The type of seasonal regime is expected to influence the structural components/parameters for soil moisture accounting and the behavior of longer-term stores, as well as the threshold and time delay of different flow paths. Hence, under transference the training scenario used has particular implications for accurate simulation of base flow and storm event dynamics.

To explore the role of interseasonal precipitation differences, hydrological years were split into two 6 month blocks representing summer (April–September, AMJJAS) and winter (October–March, ONDJFM), respectively. For each season, anomalies were calculated and a *z*-score transformation applied. Results were plotted with summer and winter anomalies located on the *y* and *x* axes, respectively. Depending on location within each quadrant, individual hydrological years were classified as follows: Dry-Dry, Wet-Wet, Dry-Wet, or Wet-Dry. The first and third ranked years were used for model training; the second and fourth ranked years were used both as the control and for assessing transferability from seasonal regimes in other quadrants.

Figure 3c shows the location of individual years within each quadrant. Note that seasonal totals are not plotted using z-score transformation. Instead, values were centered to give zero mean and scaled to have standard deviation equal to one. The experimental design recognizes that testing based on annual precipitation totals alone can mask significant variations *within* years with similar totals [*Wilby et al.*, 2015a, 2015b].



Figure 4. Percent differences in total seasonal/annual precipitation relative to 1976–2005 (Table 1) for DSST testing/control periods. (a) Differences in contrasting "wet"/"dry" hydrological years (1 October to 30 September) are shown. (b–e) Relative differences for 6 month winter (ONDJFM) and summer (AMJJAS) periods are shown for each seasonal (Wet-Dry, Dry-Wet, Wet-Wet, and Dry-Dry) DSST scenario.

Here only 2 years are used for training/testing due to some catchments having few occurrences of the four seasonal regime types. Figures 4b–4e present differences in rainfall seasonality used for DSST. Differences in summer precipitation for DSST periods, estimated relative to the long-term seasonal mean, range from +44% (Dry-Wet; 39006) to -40% (Wet-Dry; 19001). The winter period differences vary between -34% (Dry-Dry; 19001) and +25% (Wet-Wet; 14007).

We use the coding system X/Y to identify which scenario of temporal transference is examined. Here X and Y identify which independent training and evaluation period was used. Identification codes with the same first and second letter indicate training and evaluation under two similar regimes selected from the observed record. An independent "control" is used to remove inherent bias toward the training period. Different first and second letters denote training and testing under an opposing set of conditions. For example, D/W (W/D) identifies the scenario of training on the driest (wettest) and testing on the wettest (driest) years, respectively. The same applies to the seasonal experiment (e.g., DD/DD), whereby the first and last two letters indicate the seasonal precipitation regime (e.g., DD indicates Dry-Dry) used for training and testing/control, respectively.

Previous DSST studies have generally employed 5–10 year training/testing periods using both block sampling and noncontinuous years [*Yapo et al.*, 1996; *Anctil et al.*, 2004; *Hartmann and Bárdossy*, 2005; *Merz et al.*, 2011; *Coron et al.*, 2012; *Li et al.*, 2012; *Seiller et al.*, 2012, 2015]. Assessing model suitability for climate impact assessment—for which models are applied under a projected climate that may diverge significantly from conditions experienced during observations—necessitates evaluating performance under as demanding a set of conditions as possible. This requires a compromise between maximizing difference in periods used to assess transferability versus achieving potentially more robust training. Given the short record length available (~30 years) and temperate nature of the lol climate (which moderates the occurrence of extreme interannual/seasonal variability) DSST was undertaken using 3/2 year noncontinuous periods. This was considered sufficient to examine transferability under strict conditions yet provide sufficient training. Also, the shortened record lengths available for some catchments may omit years with more pronounced variability leading to a less strict DSST. However, based on relative differences in the rainfall regime between training/testing conditions for all IRN catchments, those with a shorter record length provide a similar level of diversity in precipitation (Figure 4).

The Nash-Sutcliffe efficiency (NSE) [*Nash and Sutcliffe*, 1970] criterion and a volumetric error measure (PBIAS) were used to assess performance when transferring models between control and testing periods. NSE is known to be biased toward higher flows. To provide a more balanced measure of performance across the hydrograph, NSE<sup>1/3</sup> (NSE<sub>cubrt</sub>) was also used. PBIAS provides a measure of the models' systematic error, as squared or absolute value terms are absent. In contrast, the Nash-Sutcliffe criterion squares the deviation thereby weighting positive and negative outliers equally, thus providing a measure of performance in reproducing patterns of variability in the observed series [*Gupta et al.*, 2009]. The NSE and NSE<sub>cubrt</sub> are defined as equations (1) and (2), respectively:

NSE= 
$$1 - \frac{\sum_{t=1}^{T} (Q_o^t - Q_m^t)^2}{\sum_{t=1}^{T} (Q_o^t - \overline{Q}_o^t)^2}$$
 (1)

$$NSE_{cubrt} = 1 - \frac{\sum_{t=1}^{T} \left( \sqrt[3]{Q_o^t} - \sqrt[3]{Q_m^t} \right)^2}{\sum_{t=1}^{T} \left( \sqrt[3]{Q_o^t} - \frac{\sqrt[3]{Q_m^t}}{\sqrt[3]{Q_o^t}} \right)^2}$$
(2)

where  $Q_m$  and  $Q_o$  represent simulated and observed daily runoff, respectively;  $\overline{Q_o}$  is the mean observed streamflow for the estimation period, t is the time step, and T is the number of data points. Similarly  $\sqrt[3]{Q_m}$  and  $\sqrt[3]{Q_o}$  represent simulated and observed daily runoff with a cube root transformation applied;  $\sqrt[3]{Q_o}$  is the mean observed cube root transformed streamflow. The PBIAS measure (equation (3)) is described by

$$\mathsf{PBIAS} = \frac{\sum_{t=1}^{T} Q_m^t - Q_o^t}{\sum_{t=1}^{T} Q_o^t} \times 100 \tag{3}$$

### 2.4. Parameter Selection

Parameter values sampled from different regions of parameter space can provide equally valid simulations of system behavior [*Beven*, 2006]. This may, in part, be attributed to the overparameterization of hydrological models, as well as to issues of parameter interdependence and identifiability. Although parameter sets may perform comparably well during training, their values are tuned to the training data used, meaning

they can respond very differently when applied under dissimilar conditions [*Uhlenbrook et al.*, 1999]. Additionally, parameters may exhibit differing sensitivities depending on the climate conditions experienced during training; this has implications for identifiability and performance under contrasting conditions [*Merz et al.*, 2011].

To address parameter uncertainty we employ the Generalized Likelihood Uncertainty Estimation (GLUE) procedure [*Beven and Binley*, 1992], a Monte Carlo based approach to model training and uncertainty assessment which is employed extensively in hydrological and environmental modeling [*Blasone et al.*, 2008; *Bastola et al.*, 2011; *Shafii and Tolson*, 2015]. The GLUE procedure is applied to the training data (Figure 2); evaluation was undertaken using the control and testing data.

For each model, 10,000 simulations were conducted for the period 1970–2010 using parameter sets drawn randomly from a uniform (noninformative) prior distribution using Latin Hypercube Sampling [*McKay et al.*, 1979]. We use the period 1970–1973 as a spin-up period to equalize model stores, the proceeding years (up to 2010) are used for DSST (Figure 2). The GLUE procedure was applied using identified noncontinuous 2/3 year DSST training scenarios. By simulating the full series and then extracting nonsequential 2/3 years periods for training/testing, the temporal dynamics and internal consistency of catchment stores are maintained.

A likelihood measure was used to distinguish between behavioral and nonbehavioral parameter sets conditional on the input data and observations. In this case, the root-mean-squared error (RMSE) was applied to square root transformed streamflow series (equation (4)):

$$\mathsf{RMSE}_{\mathsf{sqrt}} = \sqrt{\frac{\sum_{t=1}^{T} \left(\sqrt{Q_m^t} - \sqrt{Q_o^t}\right)^2}{T}}$$
(4)

where  $\sqrt{Q_o^t}$  and  $\sqrt{Q_m^t}$  represent the square root of observed and simulated runoff at time step *t*, respectively; *T* is the total number of observations. This measure reduces bias toward higher flows associated with the standard RMSE and is a general purpose criterion for hydrograph fitting [*Oudin et al.*, 2006a, 2006b]. Using a set of performance measures different to the likelihood function above removes potential bias toward the training criterion, allowing more equitable assessment of transferability.

The top 10% parameter sets ranked according to  $\text{RMSE}_{\text{sqrt}}$  for the training period were retained as behavioral and the associated  $\text{RMSE}_{\text{sqrt}}$  values were used to estimate respective weights. Performance of the median simulation under control and opposing testing period(s) was used to examine model transferability. Here the median simulator refers to the combined fiftieth percentile of daily flow which is derived from the weighted flow series simulated by the retained parameter sets. As the likelihood measure does not conform to the properties of a formal objective function, and can return values greater than 1, a transformation function was required. Following *Blasone et al.* [2008] and *Mertens et al.* [2004], the posterior likelihood function for accepted parameter sets was calculated as the reciprocal of the returned efficiency criterion multiplied by a normalizing factor. In this case, the posterior likelihood function  $L(\theta_i|Q)$  for each behavioral set  $(\theta_i)$ was calculated using (equation (5))

$$L(\theta_i|Q) = \frac{1}{F_i} \cdot \frac{1}{C}$$
(5)

where *Q* represents the observed runoff series and *C* is a scaling constant such that the sum of  $L(\theta_i|Q)$  over the accepted simulations equals unity; here  $F_i$  is the RMSE<sub>sqrt</sub> for  $\theta_i$  divided by the minima of the likelihood measure returned for the retained set. These Rescaled Likelihoods (*RL*) were used to assign a weight to the behavioral simulations. The prediction quantiles at each time step were empirically derived according to (equation (6))

$$P[\hat{Z}_t < z] = \sum_{i=1}^{N} RL[f(\theta_i)|\hat{Z}_{t,i}, z]$$
(6)

where *P* is the selected quantile,  $\theta_i$  is the *i*th parameter set, and *N* is the number of behavioral parameters. The value of the discharge series at time *t* by model  $f(\theta_i)$  is represented by  $\hat{Z}$ . The median was taken as the most likely estimate and used as input for model averaging.

#### 2.5. Model Averaging

Numerous averaging techniques have been proposed. These range from simple averaging—where all outcomes are considered equally probable—to more sophisticated weight-based methods which may be static or dynamically tuned to system behavior [*See and Openshaw*, 2000; *Hu et al.*, 2001]. Here four averaging techniques were considered, namely: Bayesian Model Averaging (BMA), Akaike information criterion averaging (AICA), a variant of the Granger-Ramanathan Averaging (GRA) method, and simple arithmetic mean (SAM). Methods were selected on the basis that they have achieved good results in previous intercomparison studies [*Diks and Vrugt*, 2010; *Arsenault et al.*, 2015], differ in complexity, and are representative of contrasting methodological approaches. In cases where weights were applied, their values were estimated over the training period (Figure 2), with transferability of the ensemble average to each opposing testing period being assessed. SAM is the least sophisticated method considered, and assigns equal weight to each ensemble member irrespective of past performance. While simplistic, previous studies have demonstrated that SAM can improve performance over individual model structures [*Seiller et al.*, 2012, 2015]. Additionally, SAM provides a benchmark against which to compare more complex averaging methods. The median prediction from the GLUE method as applied above to each model and DSST scenario was taken as the input for averaging.

### 2.5.1. Bayesian Model Averaging (BMA)

BMA is a statistical framework for combining output from competing members of an ensemble to give a more realistic description of predictive uncertainty [*Hoeting et al.*, 1999; *Raftery et al.*, 2005; *Rojas et al.*, 2008]. A comprehensive description of the technique is provided by *Hoeting et al.* [1999] and *Bastola et al.* [2011]. BMA weights simulations from individual model members based on their relative skill estimated over a training period. According to BMA the full predictive distribution for the quantity of interest ( $\Delta$ ) is described by (equation (7))

$$p(\Delta|M_1, \ldots, M_K, D) = \sum_{k=1}^{K} p(\Delta|M_k, D) p(M_k|D)$$
(7)

The above is estimated as the mean of the posterior predictive distribution for  $\Delta$  predicted by each individual model  $p(\Delta|M_k, D)$  weighted by the associated posterior model probability  $p(M_k|D)$ . The posterior probability of model  $M_k$  is given by (equation (8))

$$p(M_k|D) \propto p(D|M_k)p(M_k)$$
 (8)

where  $p(D|M_k)$  is the integrated likelihood of model  $(M_k)$ . A distribution for the prior probability of each model  $p(M_k)$  must be specified. In this case, as no prior assumptions regarding the likely performance or suitability of individual model structures were made, a uniform (noninformative) distribution was selected. This ensured model weights (likelihoods) were estimated conditional only on observed data used for training. The mean and variance of the predictive distribution for  $\Delta$  were estimated using (equations (9) and (10))

$$E[\Delta|M_1, \ldots, M_k, D] = \sum_{k=1}^{K} w_k \hat{\Delta}_k$$
(9)

$$Var[\Delta|M_1, \ldots, M_k, D] = \sum_{k=1}^{K} \left( Var(\Delta|D, M_k) + \hat{\Delta}_k \right) w_k - E(\Delta|D)^2$$
(10)

where  $\hat{\Delta}_k = E(\Delta|D, M_k)$ . The weighting for models in the ensemble  $(w_k)$  varies between zero and one with the cumulative sum equal to unity. The total variance or predictive uncertainty is estimated as a combination of intermodel and intramodel variance. Streamflow is nonzero, strictly positive and highly skewed meaning it does not conform to a Gaussian distribution. Thus, the probability density function of the model output at time step *t* was modeled using a gamma distribution (equation (11)) with heteroscedastic variance (equation (12)).

$$p(\Delta|M_k) = \Delta^{\alpha_k - 1} e^{\binom{\Delta}{\beta_k}} / (\Gamma(\alpha_k) \theta^{\alpha_k})$$
(11)

$$\alpha = \mu_k^2 / \sigma_k^2; \ \beta_k = \sigma_k^2 / \mu_k; \ \mu_k = M_k; \ \sigma_k^2 = b \cdot M_k + c$$
(12)

$$I(w_1,\ldots,w_k|\sigma_1^2\ldots\sigma_k^2, \ \Delta) = \sum_{t=1}^n \log\left(w_1p(\Delta|M_1) + \cdots + w_kp(\Delta|M_k)\right)$$
(13)

Here *b* and *c* are the coefficients which relate the model simulated series with the respective variances. Over each training period the BMA weights and variances were estimated from observed streamflow data through Markov Chain Monte Carlo (MCMC) sampling. This was undertaken using the Differential Evolution Adaptive Metropolis (DREAM) algorithm [*Vrugt et al.*, 2008]. The maximum a posteriori probability estimates of the weights—as determined over the training period—were used to average model simulations. Performance of the model average when temporally transferred to each testing period was then assessed using the adopted set of performance criteria.

#### 2.5.2. Akaike Information Criteria Averaging (AICA)

AICA [*Akaike*, 1974] is a method for combining ensemble members based on both performance and model parsimony. Weights represent a trade-off between reducing the overall prediction bias while tending toward less complex models. Such a measure is important when considering model transferability, where increasing the number of parameters could increase the likelihood of overfitting, thus limiting a model's ability to generalize to unseen conditions. As specified by *Buckland et al.* [1997] and *Burnham and Anderson* [2003] the weights are calculated by (equation (14))

$$\beta_{AICA,k} = \frac{\exp\left(-\frac{1}{2}I_k\right)}{\sum_{k=1}^{K}\exp\left(-\frac{1}{2}I_k\right)}$$
(14)

where  $I_k$  (equation (15)) is an information criterion estimated based on the mean of the logarithm of the model variances.

$$I_k = -2\log(L_k) + q(p_k) \tag{15}$$

In the above,  $L_k$  is the maximum likelihood of model k and  $q(p_k)$  is its associated penalty term which, in this case, is taken for each ensemble member as double the number of calibration parameters or  $q(p_k)=2p$ . **2.5.3. Granger-Ramanathan Averaging (GRA)** 

GRA simulations are combined using Ordinary Least Squares (OLS) optimized by minimizing the root-meansquared difference between simulated and observed series. Previous studies have employed different variants of the method including applying a bias correction and using (non)constrained linear coefficients [*Diks and Vrugt*, 2010; *Arsenault et al.*, 2015]. In this study, the OLS algorithm is constrained so that weights are positive and sum to unity—a prior bias correction was not applied. The model weighting vector ( $\beta_{GRA}$ ) was estimated according to (equation (16))

$$\beta_{GRA} = (X^T X)^{-1} X^T Y \tag{16}$$

where Y it a vector representing the observed discharge series for the training period and X is an  $n \times m$  matrix whose columns (*m*) correspond to the daily (*n* rows) simulated flow series from each model member.

### 3. Results

This section presents results from the DSST undertaken to assess the performance of a six member CRR model ensemble under contrasting climate conditions. For each of the 37 catchments DSST was conducted using the wettest/driest 3 year noncontinuous periods on record. Similarly, performance when models were transferred between contrasting wet/dry seasonal scenarios was examined. Note that while DSST analysis is conducted using noncontinuous periods, all model simulations are run continuously using the entire period for which input data (rainfall and PET) are available ( $\sim$ 1970–2010). DSST was conducted for individual model structures and for the ensemble collectively, using the four different model averaging techniques.

### 3.1. Individual Model Performance: Wettest/Driest Years

Figure 5 shows individual model structures ranked according to performance when tested for each wet/dry scenario (W/D, D/W), catchment and evaluation criterion. Performance is examined using median GLUE simulations. According to the NSE criterion, HBV and GR4J generally perform best. HBV is typically ranked



**Figure 5.** Individual model structures ranked (*x* axis; best (1) to worst (6)) according to performance when tested under transference between "wet"/"dry" annual regimes. Catchments (*y* axis) are sorted according to their BFI in ascending order. Models are ranked according to the absolute (Abs) PBIAS value.

higher for catchments with a low BFI; GR4J performs better on catchments with a higher BFI. While both models perform well for NSE<sub>cubrt</sub>, NAM is also ranked among the best models for this criterion, most notably for the W/D scenario. Tank and AWBM typically return the lowest NSE and NSE<sub>cubrt</sub> values across catchments. Much less consistency is evident among the results for PBIAS: in some instances, Tank is ranked among the best performing models with GR4J among the worst. The favorable results for GR4J—particularly under NSE for high BFI catchments corroborate the findings of previous model intercomparison studies [Pushpalatha et al., 2011; van Esse et al., 2013]. Given the lack of convergence in results across catchments, testing criteria, and DSST scenarios, there is considerable uncertainty when identifying a preferred model structure (albeit that a combination of GR4J and HBV appears a good compromise, with either model ranked first for 118 out of the 148 tests according to the NSE criterion).

Figure 6 plots scores for the evaluation criteria by comparing performance for the same 3 year control period when trained using (dis)similar wet/dry annual regimes (Figure 2). Differences are examined using median GLUE simulations. Distances from the diagonal (x = y) indicate differences in performance under transference. Based on results for both DSST scenarios, NSE values vary between 0.51 (GR4J; D/W; Gauge ID 26029) and 0.97 (GR4J; D/W; Gauge ID 27002). Gauge 26029 (27002) has a BFI of 0.23 (0.70), a mean elevation of 217 (73) m, and an area of 117 (511) km<sup>2</sup>. While runoff is approximately twice as much for 26029 (1308 mm  $yr^{-1}$ ) as 27002 (651 mm  $yr^{-1}$ ), annual precipitation is relatively similar (1569-1319 mm yr<sup>-1</sup>). In other words, skill is least for small, higher elevation, hydrologically responsive catchments.

PBIAS values range from 29% (AWBM;

W/D; Gauge ID 7009; BFI 0.70) to -36.0% (NAM; W/D; Gauge ID 18003; BFI 0.54). With respect to the BFI, catchment elevation, runoff (mm yr<sup>-1</sup>) and precipitation receipts (mm yr<sup>-1</sup>) are generally of (lesser) importance in differentiating model performance. Each is also negatively correlated with the BFI (Pearson's

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Figure 6. Testing (y axis) and control (x axis; shown in bold) results for two ("wet"/"dry") annual precipitation regimes. Models producing similar results for each DSST fall closer to the 45° line. Marker type corresponds to an individual model structure; markers are also coded using graduated shading for Base Flow Index (BFI).

coefficient of -0.76, -0.72, and -0.70, respectively), indicating some redundancy in using the full suite of catchment characteristics to differentiate performance. Catchment area is more poorly correlated both with model performance and BFI across catchments (Pearson's coefficient = 0.54). Broadly speaking, groundwater-dominated catchments tend to have lower precipitation receipts, yield less runoff and are located in lower lying areas; the converse generally holds for catchments dominated by surface runoff.

Given that the NSE criterion is based on the sum of squared errors, irrespective of the model structure catchments with a high BFI also return higher NSE and  $NSE_{cubrt}$  values. This is due to catchments with greater storage capacity (higher BFI) tending to be less responsive to storm events, and thus producing a less variable flow series. For example, using HBV Gauge ID 21002 with BFI of 0.21 returns a NSE value of 0.55 for the D/W testing scenario. In contrast Gauge ID 26021 (BFI 0.82) returns a NSE of 0.77 for the same model and testing scenario.

As shown by Figure 6, in some cases models experience a slight improvement in performance under transference. Overall, however, the greatest deviations from the diagonals are due to declining performance. Based on the greater variability and spread of the NSE<sub>cubrt</sub> values, models tend to experience the largest reductions in performance when trained on a wet period and transferred to a dry (i.e., W/D versus D/D) [*Seiller et al.*, 2012, 2015]. Figure 6 is supplemented by Table 3 which lists for each catchment the DSST scenario and model associated with the greatest singular decline in performance. Deceases under transference are estimated in relative (NSE and NSE<sub>cubrt</sub>) and absolute (PBIAS) terms using performance for the control (Figure 2) as a benchmark, and represents a "worst-case" scenario for each catchment. Greater relative decreases are associated with NSE<sub>cubrt</sub> as opposed to the NSE measure; in some cases, up to a 21% decrease in this criterion is observed.

Figure 7 shows NSE, NSE<sub>cubrt</sub> and PBIAS estimates for individual model structures across all catchments when transferability between the wettest/driest years is examined. Boxplots are calculated using behavioral parameter sets identified over the training period; performance under control and testing conditions is examined. Parameter sets generally perform well across all catchments, with median NSE and NSE<sub>cubrt</sub>

Table 3. The DSST Scenario and Model Associated With the Greatest Singular Decrease in Performance Under Transference Between "Wet"/"Drv" Annual Regimes<sup>a</sup>

		5	NSE NSE <sub>cubrt</sub>				PBIAS			
ID	BFI	Scenario	Model	%Δ	Scenario	Model	%Δ	Scenario	Model	Δ
6013	0.60	D/W	HyMod	-2.8	W/D	AWBM	-1.5	W/D	AWBM	-4.4
6014	0.61	D/W	HBV	-5.0	W/D	AWBM	-4.8	W/D	AWBM	- <b>4.8</b>
7009	0.70	D/W	Tank	-3.8	W/D	AWBM	-6.6	W/D	AWBM	- <b>4.6</b>
7012	0.68	D/W	HBV	-14.0	W/D	AWBM	-21.6	W/D	GR4J	-11.3
12001	0.69	D/W	NAM	-3.8	W/D	AWBM	-6.1	W/D	HBV	- <b>7.9</b>
14007	0.62	W/D	Tank	-5.0	D/W	Tank	-5.6	D/W	GR4J	-10.1
14019	0.65	D/W	Tank	-1.0	D/W	Tank	-0.9	D/W	GR4J	-4.1
15001	0.52	D/W	HyMod	-3.6	W/D	AWBM	-5.2	W/D	GR4J	-7.3
15003	0.38	W/D	GR4J	-5.3	W/D	AWBM	-7.5	D/W	AWBM	-10.5
15006	0.62	W/D	GR4J	-3.6	W/D	AWBM	-9.4	W/D	GR4J	-9.9
16008	0.63	D/W	HyMod	-8.7	W/D	HyMod	-7.0	D/W	GR4J	-10.7
16009	0.64	D/W	HyMod	-6.6	D/W	HyMod	-4.1	W/D	GR4J	-9.5
18002	0.62	D/W	HBV	-1.6	D/W	HyMod	-1.2	D/W	GR4J	<b>-4.6</b>
18003	0.54	W/D	Tank	-2.8	W/D	AWBM	-7.6	D/W	GR4J	- <b>9.6</b>
18005	0.71	D/W	NAM	-4.1	W/D	HyMod	-6.9	W/D	GR4J	-8.4
18006	0.50	W/D	GR4J	-14.6	W/D	AWBM	-20.6	W/D	AWBM	-18.4
18050	0.38	D/W	HBV	-4.3	W/D	AWBM	-6.3	W/D	HyMod	-3.9
19001	0.59	D/W	HyMod	-2.4	W/D	AWBM	-5.4	W/D	HBV	-5.9
21002	0.21	W/D	GR4J	-13.3	D/W	HyMod	-5.3	D/W	HyMod	-5.8
23002	0.28	W/D	GR4J	-6.1	D/W	NAM	-6.1	W/D	NAM	-12.0
25001	0.53	D/W	HyMod	-5.8	W/D	Tank	-10.3	D/W	GR4J	-10.8
25002	0.48	D/W	GR4J	-6.4	W/D	GR4J	-5.6	D/W	GR4J	-13.3
25006	0.69	D/W	NAM	-3.8	W/D	HyMod	-5.0	D/W	AWBM	-5.3
25030	0.54	D/W	HBV	-9.4	W/D	HyMod	-5.1	D/W	GR4J	-7.6
26009	0.43	W/D	GR4J	-5.5	W/D	AWBM	-6.8	W/D	GR4J	- <b>8.6</b>
26021	0.82	D/W	NAM	-4.0	W/D	AWBM	-5.3	D/W	GR4J	-11.2
26029	0.23	D/W	HyMod	-3.2	W/D	NAM	-2.7	W/D	Tank	-3.5
27002	0.70	D/W	NAM	-5.1	W/D	AWBM	-10.1	D/W	GR4J	-11.9
32012	0.56	W/D	AWBM	-5.4	W/D	HyMod	-18.0	W/D	HBV	-10.2
34001	0.77	W/D	Tank	-14.9	W/D	Tank	-5.5	D/W	GR4J	-16.2
35002	0.40	D/W	HyMod	-2.5	W/D	HyMod	-17.7	W/D	HBV	- <b>9.3</b>
35005	0.63	D/W	NAM	-7.1	W/D	HyMod	-12.5	W/D	HBV	-4.2
36010	0.60	D/W	Tank	-3.0	W/D	Tank	-2.5	W/D	HyMod	-4.3
38001	0.26	D/W	HyMod	-4.1	W/D	AWBM	-2.4	D/W	GR4J	-5.6
39006	0.46	D/W	NAM	-2.7	W/D	HBV	-7.3	D/W	GR4J	-5.3
201005	0.47	D/W	HBV	-1.5	W/D	HyMod	-1.4	D/W	GR4J	-4.1
201008	0.32	W/D	HBV	-10.9	D/W	AWBM	-7.4	W/D	HBV	-12.2

<sup>a</sup>Differences are estimated using performance under control conditions as a benchmark (i.e., control versus testing). Percent ( $\%\Delta$ ; NSE, NSE, NSE<sub>cubrt</sub>) and absolute ( $\Delta$ ; PBIAS) differences are given. PBIAS values in bold denote an underestimation of the total observed flow under transference (e.g., W/D). Values underlined indicate that models trained under dissimilar conditions both (under/over)estimate the total volume.

values  $\geq$ 0.7. Only HBV, GR4J, and NAM have a median NSE value greater than 0.75 for both control periods (D/D and W/W); AWBM returns the lowest median NSE and NSE<sub>cubrt</sub> values, respectively. Despite GR4J and HBV performing well across catchments, they exhibit a relatively large range under temporal transference. This suggests that the weighting applied through the GLUE procedure offsets the poor performance of some parameters within the behavioral set.

### 3.2. Individual Model Performance: Seasonal Assessment

In addition to examining transferability between the wettest and driest hydrological years, assessment was also undertaken between years with contrasting seasonal regimes. Testing was performed based on sample sizes of 2 years using the median GLUE simulation. Figure 8 shows highest to lowest ranked model structures according to performance over each testing scenario for the NSE, NSE<sub>cubrt</sub>, and PBIAS criterion, respectively. AWBM, along with HyMod and Tank (to a lesser extent) are the lowest ranked models for the NSE measure. HBV is generally ranked highest for catchments with lower base flow contributions; GR4J tends to be ranked higher for catchments with a larger BFI. Either HBV (52.2% of cases) or GR4J (27.2% of cases) are ranked first for 354 of 444 transference tests according to the NSE criterion. For NSE<sub>cubrt</sub> both models are similarly dominant, with GR4J (50.2% of cases) or HBV (29.0% of cases) being ranked first for 344 testing scenarios. Lowest NSE and NSE<sub>cubrt</sub> values are generally given by AWBM which is ranked first/last for 10/503



**Figure 7.** The combined performance of behavioral parameter sets for all catchments and rainfall-runoff models. DSST results are for two ("dry"/"wet") annual precipitation regimes are shown. The red line represents the median estimate; box edges denote the 25th and 75th percentiles. Whiskers are located at Q3 + 1.5 × (Q3 - Q1) and Q1 - 1.5 × (Q3 - Q1), where Q1 and Q3 are the 25th and 75th percentiles, respectively. Values beyond this are identified with red dots. Control scenarios are highlighted in bold. NSE/NSE<sub>cubrt</sub> values <0.3 are not shown.

cases of the same 888 transference tests. In contrast to the NSE criteria, there is much greater uncertainty in results for PBIAS. AWBM tends to be highest ranked for catchments with a low BFI, however this is reversed as the BFI increases. Additional weaker patterns in results emerge, including the poor ranking for Tank (NSE and Abs PBIAS) and NAM (NSE<sub>cubrt</sub>) under transference to a Dry-Dry (DD) seasonal regime. Similarly AWBM performs poorly for transference to a Wet-Wet (WW) and Dry-Wet (DW) scenario according to all criteria. However, the degree of inconsistency highlights the complexity of model transference, with performance being related to the individual model structure, catchment, and climate regime type.

Figure 9 (NSE), Figure 10 (NSE<sub>cubrt</sub>), and Figure 11 (PBIAS) present results of the DSST scenarios, while Table 4 lists for each catchment the scenario of seasonal transference and associated model structure that yields the greatest decrease in performance relative to the control for each evaluation criterion. For 29 of the 37 catchments, transference to a DW (Dry-Wet; 14 cases) or DD (Dry-Dry; 15) seasonal regime returns the largest reductions in the NSE criterion. Within this, the DD/DW (11 cases) and DW/DD (8 cases) scenarios are notable for returning the greatest number of poor performances. These range from a decrease in NSE of -46.4% (WD/DD; Gauge ID 25006; Tank) to -3.2% (DD/ DW; Gauge ID 18003; HBV). In contrast, the decline in performance when transferred to a WW or WD scenario is much less, while the DW/WW or WW/DW tests do not lead to the greatest singular decrease for any catchment.

A similar and more pronounced pattern is evident in the results for  $NSE_{cubrt}$  and PBIAS. For the  $NSE_{cubrt}$  criterion, transference to a DW or DD

regime is found for 33 catchments, with seven registering reductions of 20–30% relative to the control. Poor transference to a DD and WD is similarly evident for the PBIAS criterion. As shown in Table 4, deficiencies in performance across catchments are generally associated with a more pronounced underestimation of flow volumes (WD/DD; Gauge ID 18005; GR4J). Although there is a degree of variation between models, GR4J (NSE; PBIAS), HyMod, and AWBM (NSE<sub>cubrt</sub>) yield greatest reductions relative to the control.





UW/WD WW/WD WU/WD WU/WD WU/WD WU/UD WU/UD UU/WW UU/WU WW/WD WW/WD

NSE cubrt: Worst ranked model



UWC/WD WWC/WD WWC/WD WWC/UW WWC/UW WWC/WW WWC/WW WW/WW WW/WQ



Figure 8. Best and worst ranked hydrological model according to DSST results for four (DD, WW, DW, and WD) seasonal precipitation regimes (x axis). Catchments (y axis) are sorted according to their BFI in ascending order.

Figure 12 shows the results of DSST applied to all behavioral parameter sets identified across the catchment sample. In terms of absolute model performance the highest NSE<sub>cubrt</sub> control/ testing values are generally returned for the WD/WD scenario. Based on the median estimate, GR4J performs well across the catchment sample, whereas AWBM generally returns the lowest scores. Difficulties in transference to a DW or DD regime are also highlighted by Figure 12. In contrast, parameters generally maintain performance when transferred to a WW regime irrespective of the training scenario.

### 3.3. Multimodel Performance

Attention is now given to how use of the four different averaging methods over our multimodel ensembles may improve transferability. Figure 13 plots NSE values for individual models against corresponding values returned when model averaging is applied. Plots are based on the results of DSST conducted using contrasting wet/dry annual regimes for each catchment. Table 5 lists the frequency with which each method outperforms the individual ensemble members. In the majority of cases, model averaging surpasses performance of any single structure, even for SAM where the application of equal weights returns  $\mathsf{NSE}_{\mathsf{cubrt}}$  values better than individual models in more than 79% of cases. Model averaging performs better for the NSE criteria than for PBIAS. With respect to volumetric error, SAM returns similar values to the more complex averaging methods employing objective weighting criteria. Both BMA and GRA perform similarly across DSST scenarios, exhibiting only a slight difference in performance under transference to each testing period(s).

Despite the ensemble average clearly being better than individual model members (Figure 13 and Table 5), differences are evident not just in how well each averaging method performs but also in the evaluation measure used. For both Nash-Sutcliffe measures,

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Figure 9. NSE testing (y axis) and control (x axis; shown in bold) results for four (DD, WW, DW, and WD) seasonal precipitation regimes. Models producing similar results for each DSST fall closer to the 45° line. Marker type corresponds to an individual model structure; markers are also coded using graduated shading for Base Flow Index (BFI).

GRA and BMA are most consistent in exceeding the best ensemble member and perform considerably better than simple averaging. AICA fails under all DSSTs to provide encouraging results. Considering all DSST scenarios, AICA assigns the largest weight to HBV and GR4J in 50% and 31% of cases, respectively. In contrast, AWBM is never assigned a weight above zero. As would be expected, the objective methods perform well over the period used for estimation of model weights, highlighting an inherent bias to the training data. This is particularly evident for GRA according to the NSE and NSE<sub>cubrt</sub> criterion. In both cases, this method achieves almost perfect results (Table 5).

Table 6 lists the frequency with which each model averaging technique outperforms the best performing individual model from the ensemble. In the majority of cases, GRA and BMA are better under transference (and for the control) than the best performing model member according to both the NSE and NSE<sub>cubrt</sub> measures. In general, GRA performs better than BMA for the NSE criterion, particularly with respect to the best performing model member. However, the opposite applies for NSE<sub>cubrt</sub>—albeit that returned differences are of a lesser magnitude. As is demonstrated by differences between the control and testing periods, neither GRA nor BMA experience a significant drop in performance under transference. Generally, the averaging methods perform similarly across each opposing DSST period. Overall, GRA emerges as the most consistent technique, returning high NSE and NSE<sub>cubrt</sub> values across all DSST scenarios.

For PBIAS, all averaging methods generally return a considerably lower proportion (<20%) of better performing estimates when benchmarked against the best model member. The results shown in Table 6 are reflected in Figure 14 which displays the best/worst ranked model averaging method for each catchment **Table 4.** The DSST Scenario and Model Associated With the Greatest Singular Decrease in Performance Under Transference Between Seasonal (DD, WW, DW, and WD) Precipitation Regimes<sup>a</sup>

	,	,,	NSE			NSE <sub>cubrt</sub>		PBIAS			
ID	BFI	Scenario	Model	%Δ	Scenario	Model	%Δ	Scenario	Model	Δ	
21002	0.21	DD/DW	GR4J	-5.19	WW/DW	AWBM	-2.42	DD/DW	GR4J	-5.6	
26029	0.23	DD/WW	HBV	-6.91	WW/WD	AWBM	-5.58	WD/DD	HBV	- <b>7.0</b>	
38001	0.26	WD/WW	GR4J	-8.26	WW/DW	AWBM	-13.37	DW/WW	GR4J	-7.4	
23002	0.28	DD/DW	HyMod	-25.33	WW/DD	AWBM	-28.24	DD/DW	HBV	-11.8	
201008	0.32	DW/DD	GR4J	-16.31	DW/DD	AWBM	-13.40	DW/DD	GR4J	-16.0	
15003	0.38	DW/DD	Tank	-14.03	DD/DW	Tank	-14.50	DD/DW	GR4J	-7.5	
18050	0.38	DW/WD	NAM	-5.45	DW/WD	NAM	-11.39	WD/DW	GR4J	-11.1	
35002	0.4	DD/DW	HyMod	-6.04	DW/DD	HyMod	-5.24	WW/WD	GR4J	-7.6	
26009	0.43	DD/DW	HyMod	-13.51	DW/DD	HyMod	-11.81	DD/DW	AWBM	-6.9	
39006	0.46	WW/DD	GR4J	-4.72	WW/DD	AWBM	-12.59	WW/DD	GR4J	-9.3	
201005	0.47	DD/DW	HyMod	-10.43	WD/DD	Tank	-13.39	DD/DW	GR4J	-8.8	
25002	0.48	DD/WW	HyMod	-8.96	DD/WW	Tank	-6.89	DW/DD	GR4J	-10.3	
18006	0.5	DD/WW	HBV	-5.07	DD/DW	GR4J	-7.08	DW/DD	GR4J	-13.4	
15001	0.52	DW/DD	Tank	-19.84	DW/DD	HyMod	-16.03	DW/DD	HyMod	-24.2	
25001	0.53	DW/WD	NAM	-6.98	DD/DW	Tank	-10.51	WW/DD	GR4J	-7.3	
25030	0.54	WD/DD	GR4J	-27.62	WW/DD	AWBM	-22.82	WW/DD	GR4J	-18.5	
18003	0.54	DD/DW	HBV	-3.23	DW/DD	AWBM	-10.49	WW/WD	GR4J	-4.2	
32012	0.56	WD/DD	GR4J	-5.35	DW/DD	AWBM	-4.82	DW/DD	GR4J	-7.1	
19001	0.59	DW/DD	HBV	-18.49	DD/DW	HBV	-16.03	DD/DW	GR4J	-11.9	
6013	0.6	WW/DW	GR4J	-15.55	WD/DW	NAM	-14.64	WW/DD	HBV	- 18.9	
36010	0.6	DD/DW	GR4J	-14.22	DW/DD	HyMod	-17.89	DD/DW	GR4J	-11.6	
6014	0.61	DD/DW	GR4J	-10.52	WW/DW	HyMod	-11.92	DD/DW	GR4J	-14.4	
14007	0.62	DD/DW	HBV	-16.75	WW/DD	AWBM	-9.72	WD/DD	HyMod	-14.7	
15006	0.62	DW/DD	Tank	-14.36	WD/DW	Tank	-13.29	DW/DD	HyMod	-10.8	
18002	0.62	WW/DD	GR4J	-4.58	DW/DD	AWBM	-6.61	WW/WD	GR4J	-7.2	
16008	0.63	DD/DW	GR4J	-13.74	WD/DW	NAM	-18.62	DD/DW	GR4J	-18.5	
35005	0.63	DD/WD	NAM	-2.57	WD/WW	NAM	-3.56	DD/DW	GR4J	-3.1	
16009	0.64	DD/WD	NAM	-8.03	DW/DD	AWBM	-20.08	DD/WW	GR4J	-5.4	
14019	0.65	WD/DD	GR4J	-14.37	WW/DD	HyMod	-20.51	DW/WD	HyMod	-18.8	
7012	0.68	DW/DD	Tank	-45.25	DW/DD	HyMod	-16.23	DW/DD	HyMod	-15.5	
25006	0.69	DW/DD	Tank	-46.42	DW/DD	HyMod	-33.43	DW/WD	HyMod	-12.0	
12001	0.69	DD/DW	GR4J	-30.05	DD/DW	GR4J	-31.64	DW/DD	GR4J	-33.3	
27002	0.7	WD/DW	AWBM	-15.88	WD/DD	GR4J	-5.44	WD/DW	GR4J	-4.6	
7009	0.7	WW/DW	GR4J	-11.35	DW/DD	HyMod	-6.05	WW/DD	HBV	-7.2	
18005	0.71	WD/DD	GR4J	-36.39	WD/DD	GR4J	-29.16	WD/DD	GR4J	-36.0	
34001	0.77	WD/DD	AWBM	-6.04	WD/DW	AWBM	-5.66	DD/WD	GR4J	-5.9	
26021	0.82	DW/DD	GR4J	-27.16	DD/DW	HBV	-19.19	WD/DD	HBV	-11.7	

<sup>a</sup>Differences are estimated using performance under control conditions as a benchmark (i.e., control versus testing). Percent ( $\Delta$ ; NSE, NSE, NSE<sub>cubrt</sub>) and absolute ( $\Delta$ ; PBIAS) differences are given. PBIAS values in bold denote an underestimation of the total observed flow under transference (e.g., WD/DD). Values underlined indicate that models trained under dissimilar conditions both (under/over)estimate the total volume.

and seasonal DSST scenario; also considered is the best/worst performing model structure. Evident are the more favorable results for BMA/GRA according to the NSE/NSE<sub>cubrt</sub> criterion. The ranking of methods is also largely consistent across individual catchments and for each DSST scenario. Figure 14 further highlights disparities in performance between the NSE and PBIAS measures. In the latter case, it is shown that the best individual model structure for each scenario typically performs better than the respective model averaging techniques. Figure 14 also highlights that the worst performing model is most often ranked lower than the worst performing averaging method.

### 4. Discussion

While in some cases model performance was shown to improve relative to the control when trained under a contrasting set of conditions, in general there was a degradation in performance. The extent of this degradation depends on model structure, catchment, DSST scenario, performance criterion, and averaging technique. For all catchments, no clear relationship could be identified between decline in performance under transference and relative differences in precipitation between DSST periods. This may be due to variations in training/control and testing conditions being broadly similar across the catchment sample (Figure 4a). In

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Figure 10. NSE<sub>cubrt</sub> testing (y axis) and control (x axis; shown in bold) results for four (DD, WW, DW, and WD) seasonal precipitation regimes. Models producing similar results for each DSST fall closer to the 45° line. Marker type corresponds to an individual model structure; markers are also coded using graduated shading for Base Flow Index (BFI).

addition, despite using a 2/3 year period to maximize interannual/seasonal differences, the dissimilarity between training/testing conditions varies only within a limited range. Furthermore, when considering results for the catchment sample collectively, there are a number of interacting factors external to the driving climate regime. These include differences in the catchment properties and model/data uncertainties which may preclude or complicate a simple quantitative (linear or otherwise) relationship between differences in performance and differences in the associated annual/seasonal precipitation regime. As a result, no generally applicable quantitative threshold for transferability—indicating when models may become inaccurate or nonfunctional—can be identified. This underlines the necessity of conducting DSST on a catchment-by-catchment and model-specific basis.

Generally, models were challenged when transferring between wetter and drier periods. Overall, the greatest performance declines were associated with transference from wet to dry conditions. This is evident both in terms of transference between wetter/drier years and between contrasting seasonal precipitation regimes. For the latter, models struggled when simulating years with a dry winter followed by dry summer, particularly with respect to the (low flow) NSE<sub>cubrt</sub> criterion. In contrast, models were less affected by transference to a wet-dry or wet-wet seasonal regime. This finding applies both to the median estimate derived using GLUE and behavioral parameter sets across the catchment sample. Hence, if climate change tends toward drier conditions, then we would expect models calibrated on a wetter present to be less accurate under future forcing. Conversely, for a more pronounced seasonal regime (wetter winters and drier summers) models may maintain performance. Difficulties in transference to a "drier" regime may be related to nonlinearities in the hydrological processes being more pronounced and poorly conditioned under a

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**Figure 11.** PBIAS testing (*y* axis) and control (*x* axis; shown in bold) results for four (DD, WW, DW, and WD) seasonal precipitation regimes. Models producing similar results for each DSST fall closer to the 45° line. Marker type corresponds to an individual model structure; markers are also coded using graduated shading for Base Flow Index (BFI).

"wetter" regime [*Atkinson et al.*, 2002, *van Esse et al.*, 2013]. Sensitivity to training using wet or dry periods is highlighted by *Li et al.* [2012], who indicate that models intended to simulate a wet/dry climate scenario should be trained using a similar period from the observed record.

While our findings support previous research [*Li et al.*, 2012; *Seiller et al.*, 2012, 2015], they contradict *Wilby and Harris* [2006] who found greater transferability from wet to dry conditions in the Thames basin (SE England). Here it is highlighted that data information content, in terms of threshold parameter activation, is higher during wet periods, thereby improving transference to dry (as opposed to wet) conditions. However, as applies to all previous studies a direct comparison is complicated by differences in the hydroclimatological regime and the degree of dissimilarity between DSST conditions [*Brigode et al.*, 2013]. For example differences between "wet" and "dry" are more pronounced in SE England than the lol.

Typically, the structures that performed well under control conditions also performed well under transference, with the model rankings generally unchanged. Overall declines in performance were not sufficient to conclude that the models may be inaccurate or nonfunctional under altered climate conditions. However, it is acknowledged that the historical record may only provide limited analogues to represent plausible ranges of future changes. For instance, there is no 3 year period that is >20% wetter or drier than the climatology mean (1976–2005) to stress test operational limitations under the full range of possible future climates [*Matthews et al.*, 2016]. Consequently, we emphasize that caution be exercised in assuming model reliability under input forcing that differs markedly from the data available for model development. This concurs with



**Figure 12.** NSE<sub>cubrt</sub> boxplots developed using the combined behavioral parameter sets of all six rainfall-runoff models for 37 catchments and four (DD, WW, DW, and WD) seasonal precipitation regimes. The red line represents the median estimate; box edges denote the 25th and 75th percentiles. Whiskers are located at Q3 + 1.5  $\times$  (Q3 - Q1) and Q1 - 1.5  $\times$  (Q3 - Q1), where Q1 and Q3 are the 25th and 75th percentiles, respectively. Values beyond this are identified with red dots. Control scenarios are highlighted in bold. NSE/NSE<sub>cubrt</sub> values <0.2 are not shown.

Bastola et al., [2011] who found substantial divergence between individual CRR model structures when driven using the same downscaled climate change projections, even though the models performed similarly under observed conditions. Difficulties encountered in temporal transferability mirror those of spatial transferability, whereby rainfall-runoff models are developed for ungauged catchments using parameters calibrated at suitable donor sites identified based on physical similarity and/or spatial proximity [Oudin et al., 2008; Parajka et al., 2013]. The DSST method used here would provide a suitable approach for interrogating the performance of different regionalization techniques under contrasted conditions.

Our results confirm that it is impossible to identify a single optimum model structure across all catchments and all DSST scenarios. In addition, performance was found to vary considerably depending on the evaluation criteria used, with differences being most apparent when comparing the NSE and PBIAS. However, under transference for the NSE criteria, a number of models can be identified that are likely to be more/less robust for climate assessment. Overall, HBV, GR4J and to a lesser extent NAM were consistently the best performing models, with HBV (GR4J) generally ranked the highest for catchments with a lower (higher) groundwater contribution. For climate impact studies the case for GR4J is further strengthened by its relatively parsimonious structure. In contrast, AWBM generally performed poorly across DSST periods for the majority of catchments. This may be due to its relatively large number of parameters (i.e., low parsimony) or the fact that, despite its plausible structure it was conceived for a different (Australian) hydroclimate regime. It is noted that, contrary to other models AWBM requires that surface stores are satisfied before excess moisture required to sustain base flow and surface runoff is generated.

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**Figure 13.** NSE scores for "wet"/"dry" DSST period obtained from four different model averaging techniques plotted against the corresponding NSE value from each model structure (grey dots). NSE values showing transference between the wettest/driest years for each catchment is plotted; red dots denote the best performing individual ensemble member. Model averaging improves relative to a single structure where points are plotted below the  $45^{\circ}$  continuous green line (i.e., x = y).

The favorable results for HBV and GR4J are consistent with previous studies [*Perrin et al.*, 2001; *Seiller et al.*, 2012, 2015]. The good performance of GR4J may, in part, be attributed to its inclusion of a water exchange function alongside two independent parallel routing paths, which *van Esse et al.*, [2013] cite as important both for ground water-dominated catchments and successful transference between contrasting wet/dry periods. Conversely high BFI catchments with less dynamic flow behavior may be better represented using linear models. In our case, the higher performance of HBV for responsive catchments may be due to its use of two linear outflows from the upper reservoir (one of which is threshold activated) allowing better representation of lateral and direct flow dynamics during storm events. This is supported by the better performance of HBV (GR4J) for the NSE (NSE<sub>cubrt</sub>) criterion which is more representative of high (low) flow dynamics. *Fenicia et al.*, [2014] note the importance of storage elements connected in series (versus a parallel configuration) for catchments with impermeable bedrock dominated by lateral flows. Such catchments may also favor nonlinear models where threshold exceedance activates more direct flow paths. As shown by others, improvements in HBV simulation of groundwater catchments may be gained (particularly for recession dynamics) if reservoir discharges were modeled using a power function [*Samuel et al.* 2012; *van Esse et al.*, 2013].

The number of model parameters is an important factor that can directly affect model performance. In base flow dominated catchments, parsimonious models with less complexity (e.g., GR4J) may be sufficient. However, in catchments with a low BFI and thus higher variability in runoff a more complex model (more parameters; e.g., HBV) may be required. When comparing HBV and HyMod—which share similar soil moisture accounting routines—our results suggest that the greater parametric complexity of HBV and use of a parallel rather than serial routing/storage structure is more successful. Based on the differing number of free parameters (Table 3), the performance of AWBM and Tank indicates that a greater degree of freedom in terms of fitting does not necessarily lead to superior performance. In fact, this may increase the risk of overfitting during training, and hence a lesser ability to generalize across diverse conditions.

With respect to the BFI, it is worth noting how differences in the storage and routing configuration relate to infiltration processes and performance for groundwater/runoff dominated catchments. The influence of

Table 5. Frequency (%) With Which Each Model Averaging Technique Outperforms Individual Members of the Model Ensemble Calculated for Each DSST and Training Period<sup>a</sup>

		N	SE		NSE <sub>cubrt</sub>				Absolute PBIAS			
DSST	BMA	AICA	GRA	SAM	BMA	AICA	GRA	SAM	BMA	AICA	GRA	SAM
D (training)	80	80	100	72	99	70	99	85	75	50	66	60
D/D	87	82	94	78	98	71	95	87	57	56	60	57
W/D	89	74	94	81	97	63	92	89	60	54	66	55
W (training)	85	72	100	85	100	75	99	91	58	51	77	60
W/W	89	76	96	82	99	70	97	90	55	54	67	64
D/W	86	77	95	76	97	68	95	86	58	58	70	60
DD (training)	80	68	100	82	99	70	98	85	68	52	65	55
DD/DD	82	70	90	81	90	65	90	82	64	87	68	52
WD/DD	86	69	89	83	95	63	89	91	60	55	60	58
DW/DD	86	67	87	77	91	61	85	86	57	50	63	53
WW/DD	91	68	93	84	95	65	90	92	54	52	64	55
WD (training)	84	82	100	80	99	69	97	79	57	49	75	65
WD/WD	89	86	95	77	80	71	95	80	55	50	69	61
DD/WD	77	71	91	77	91	67	92	88	50	51	64	60
DW/WD	86	76	91	74	96	74	92	85	58	50	63	58
WW/WD	88	77	92	76	96	71	92	89	57	46	61	64
WD (training)	85	80	100	78	100	75	98	85	57	52	80	62
WD/WD	87	82	90	79	98	75	97	86	66	58	76	69
WD/DW	88	77	95	85	96	72	95	90	60	54	66	64
DD/DW	82	71	91	82	92	64	91	88	55	51	64	62
WW/WD	89	73	94	86	96	71	95	91	51	44	59	64
WW (training)	90	81	100	75	100	80	99	82	65	55	78	59
WW/WW	92	84	91	77	92	75	99	86	69	57	76	62
DW/WW	89	79	92	76	95	72	92	85	64	55	69	60
WD/WW	89	76	95	80	96	73	95	89	63	52	68	59
DD/WW	84	73	95	77	93	67	91	86	61	55	66	62

<sup>a</sup>Results for the training and control periods are listed in bold.

vertical soil heterogeneity and slope has on runoff generation is well documented [*Smith and Hebbert*, 1983; *Jackson*, 1992]. Typically for catchments with permeable homogeneous soils and a low anisotropy ratio (vertical conductivity/horizontal conductivity), movement through upper layers tends to occur vertically, with vertical increases in the saturated zone depth having a greater effect on runoff than lateral movements. Here catchments are likely to have a high BFI owing to better infiltration and delayed routing. In contrast,

Table 6. Frequency (%) With Which Each Model Averaging Technique Outperforms the Best Individual Model Member of the Ensemble for Each DSST<sup>a</sup>

DSST		N	SE		NSE <sub>cubrt</sub>				Absolute PBIAS			
	BMA	AICA	GRA	SAM	BMA	AICA	GRA	SAM	BMA	AICA	GRA	SAM
D/D	41	5	65	14	86	0	70	49	20	0	15	8
W/D	49	0	68	16	86	5	70	51	17	0	16	14
W/W	46	0	81	27	95	3	86	51	15	0	18	16
D/W	32	3	70	16	84	0	81	32	14	0	16	3
DD/DD	44	3	60	16	75	3	72	43	15	0	19	5
WD/DD	41	0	57	22	70	11	53	57	18	0	18	5
DW/DD	41	0	51	16	62	3	51	41	15	0	14	3
WW/DD	51	3	62	24	76	3	54	62	17	0	13	5
WD/WD	46	10	70	16	72	8	73	43	12	0	15	15
DD/WD	30	0	54	16	57	5	62	41	13	0	15	5
DW/WD	35	5	52	14	78	3	59	35	18	0	16	11
WW/WD	41	5	68	16	84	3	68	43	16	0	12	11
WD/WD	46	8	71	19	89	5	84	27	11	0	12	12
WD/DW	41	5	73	27	81	8	78	46	12	0	15	14
DD/DW	32	0	68	27	68	3	65	46	13	0	11	5
WW/WD	51	0	76	27	86	3	76	51	14	0	10	8
ww/ww	54	5	68	8	80	3	81	30	19	0	17	11
DW/WW	43	3	57	11	78	0	65	35	17	0	15	5
WD/WW	46	8	73	16	78	5	76	46	20	0	18	8
DD/WW	30	3	70	14	73	3	68	32	21	0	11	11

<sup>a</sup>Results for the control are listed in bold.

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Figure 14. Best and worst ranked model averaging technique according to DSST results for four (DD, WW, DW, and WD) seasonal precipitation regimes (*x* axis). Also considered is the best and worst performing conceptual rainfall-runoff (CRR) model for each scenario. Catchments (*y* axis) are sorted according to their BFI in ascending order.

for catchments with a high anisotropy ratio where hillslope processes dominate, lateral flows are likely to be more significant. Hence, models like HBV, which can better capture vertical variability in soil processes by using multiple vertical stores and a dedicated soil moisture routine, and which explicitly account for direct/lateral flows, may be more applicable to low BFI catchments. Furthermore the hillslope can be conceptualized as consisting of two soil layers, with the lower layer capable of retarding vertical flow at the boundary allowing development of subsurface stormflow. This corresponds well with the inclusion of an upper soil box in HBV from which two lateral outflows (one threshold based) are represented [*Smith and Hebbert*, 1983]. While GR4J also accounts for vertical variability, only two stores (production and routing) are included, and lateral flows are less well represented. In addition, the model has fewer free parameters to adjust in order to better capture horizontal/direct flows (e.g., the set 90:10 split between delayed and direct routing channels).

Relative to other criteria, model performance for PBIAS was more varied: notably, in some cases, AWBM was returned as the best performing model. Performance in simulating the long-term water balance is related to how precipitation is partitioned between evaporation and streamflow. Hence, performance hinges on those model parameters relating to evaporation influence on the water balance [*Herman et al.*, 2013]. The more favorable performance of AWBM may be due to it being the only model that incorporates an adjustment factor for PET. However, determining which parameters influence the overall water balance would require an in-depth and systematic sensitivity assessment that is beyond the scope of this study. In addition, as noted by *Herman et al.* [2013], selecting behavioral parameter sets using RMSE alone (as in this study) is no guarantee of achieving an accurate water balance. Thus, differences between the NSE and PBIAS criteria may also reflect the choice of likelihood function.

Differences in the performance criteria suggest that model selection should give due consideration to those components of the flow regime that are most relevant to the study objectives. For example, AWBM may be more appropriate for assessing climate driven changes in the long-term water balance, as opposed to assessing changes in dynamic behavior (e.g., timing and magnitude of flood peaks). However, given that it only provides a measure of systematic error, and is thus a less comprehensive indicator of overall performance, selecting a model on the basis of mean bias alone lacks rigor. Hence, to inform robust model selection for climate studies, modelers should examine temporal transferability giving weight to multiple performance criteria. Here each criterion can be treated equally, or based on the study objective weights can be used to place greater emphasis on performance for particular parts of the hydrological regime.

When benchmarked against a single model structure, the ensemble average provides a better overall estimator. The performance of averaging techniques was shown to remain relatively consistent under transference. Additionally, methods based on objective weighting are recommended over simple averaging. The results confirm findings from previous studies which stress the value of a multimodel strategy [e.g., *Shamseldin et al.*, 1997; *Velázquez et al.*, 2010, 2011, *Seiller et al.*, 2012, 2015; *Arsenault et al.*, 2015]. When benchmarked against the best individual model structure, greater variation in the averaging methods emerged. These differences are related primarily to the choice of evaluation criteria rather than the DSST scenario or catchment selected. All methods performed considerably better for the NSE as opposed to PBIAS measure. This suggests that any potential bias toward certain error types should be considered when selecting an averaging technique.

As reported by previous studies, the AICA method was found to perform relatively poorly [*Diks and Vrugt*, 2010; *Arsenault et al.*, 2015] due to a tendency to heavily weight a single member, thereby discounting additional information provided by the ensemble. As implemented here, AICA is strictly a model averaging technique. This is generally not the case with conventional information criterion methods which seek to identify the single "best" model based on parsimony and performance. This suggests that, although it can be used as a model averaging technique, there are better alternatives. But the method does have value if there are any concerns about overfitting models with a large number of parameters.

Overall, GRA produced the most consistent results across catchments and DSST periods. While BMA was found to perform comparably, this method is computational demanding and requires considerable run time to achieve convergence. However, it is acknowledged that the deterministic nature of this study ignores the importance of uncertainty in model averaging. For this purpose, BMA provides a coherent framework which allows explicit quantification of both within and between model uncertainties. Given its importance for robust decision making, the benefit of selecting an averaging method like BMA which provides a comprehensive and statistically robust framework for uncertainty assessment should receive due consideration.

It could be argued that a more carefully selected model may provide a better tool for impact assessment. While this may be appealing, particularly given the additional resources required to develop a multimodel ensemble, it ignores the fact that structural uncertainties make this a particularly risky strategy. This will always be the case because of our inability to fully explore model behavior under (unknowable) future climate forcing using historical data. It is also noted that the process of parameter selection (whether using an optimization routine or a method such as GLUE), and the training data used, limit model ability to produce accurate simulations when extrapolated beyond this context.

Our results demonstrate that the best model varies depending on the DSST scenario, performance measure and catchment considered, thus making optimal model identification unlikely. Such an approach would also require tuning the selection for each catchment, which an adequate averaging technique should achieve without necessitating prior screening. An alternative strategy might be to select an optimum model subset. However, this process is subject to the same uncertainties outlined above, and is complicated by the optimal subset not always being comprised of the best individual models [*Velázquez et al.*, 2011; *Seiller et al.*, 2012, 2015]. This approach further runs the risk of pooling insufficient information to provide a good measure of structural uncertainty, with too few members resulting in diminished predictive power and the added benefit of the ensemble ultimately being lost.

Future work will examine why the individual CRR models performed differently across the catchment sample used in this study. Exploring parameter sensitivity to time-varying hydroclimatic conditions would help link physical processes with model formulation and provide insight to the relative skill of ensemble members under different forcing scenarios (e.g., wet/dry and seasonal transitions). This would also help to establish the influence which information content in the training data and the associated activation frequency of key parameters have on transferability between contrasting regimes.

While the current study considers six dissimilar CRR models, each has a fixed structure which, it is assumed, will generalize across a variety of catchment types. However, there is scope for exploring temporal transferability using a flexible modeling framework such as SUPERFLEX [*Fenicia et al.*, 2011] or FUSE [*Clark et al.*, 2008]. Previous studies have highlighted the benefits of moving away from the "one-size-fits-all" approach to one based on developing a structure commensurate with the hydrological complexity of the study catchment [*Staudinger et al.*, 2011; *Euser et al.*, 2013]. Although potentially allowing for more appropriate structure selection this would still require DSST to evaluate capabilities beyond the training set(s). Similarly using a flexible framework, whereby the effect of individual components can be isolated allows a more tenable link between physical catchment properties/processes and the model structure. Parametric uncertainty notwithstanding, it facilitates attributing differences in performance to specific structural configurations.

### 5. Conclusion

This study employed Differential Split Sample Testing (DSST) to scrutinize the temporal transferability of six conceptual rainfall-runoff models based on contrasting 2/3 year noncontinuous periods. Using 37 Irish catchments with diverse hydrological regimes, model performance was assessed when transferred between the wettest/driest years on record and between contrasting wet/dry seasonal combinations. The study also considered the benefits of employing combined model estimates derived from four different ensemble averaging techniques.

Overall, HBV, GR4J, and to a lesser extent NAM were consistently the best performing models, with HBV (GR4J) generally ranking highest for catchments with a lower (higher) groundwater contribution. Transferability of individual structures was found to vary depending on the DSST scenario, catchment and testing criteria used. The greatest declines in performance were associated with transference to drier conditions, with the extent of decline dependent on the performance criterion used.

The results confirm that it is impossible to identify a single structure that performs optimally across all catchments, DSST scenarios and performance criteria. Moreover, the collective ensemble was shown to outperform the majority of individual ensemble members. However, averaging methods were found to differ considerably with respect to the frequency with which they surpass the best individual member, particularly for volumetric errors. Bayesian Model Averaging (BMA) and the Granger-Ramanathan Averaging (GRA) method were found to perform better under transference than using the simple arithmetic mean (SAM) and Akaike Information Criteria Averaging (AICA). Further work could be done on the potential added value of using different variants of GRA including nonconstrained weights and a bias correction step, as well as the transferability of averaging techniques that implement dynamic weighting [*See and Openshaw*, 2000; *Hu et al.*, 2001; *Wagener et al.*, 2003].

Given that the historical record may not provide sufficient analogues to represent the plausible range of projected climate changes, it is likely that the predictive errors from DSST will be underestimated and the demand for models to offer functional simulations under increasingly different conditions will almost

certainly be greater than can be captured here. It is noted that we only examined performance based on mean seasonal/annual conditions. Other objective functions could be used to test model performance under extreme high or low flows (which may be of greater interest to decision-makers than average flow conditions).

Moreover, there is scope to develop an expanded DSST methodology that incorporates an assessment of extremes, particularly as transferability at seasonal/annual timescales may mask performance with respect to exact nonstationarities in the intensity and occurrence of extreme events. Similarly, while we focus on precipitation, it may be helpful to consider using other climate variables (e.g., temperature, evaporation, wind speed, and cloud cover) when selecting contrasting periods of record for model training and transference testing [e.g., *Seiller et al.*, 2012, 2015]. This may be particularly pertinent in regions where evapotranspiration and/or snowmelt presently play a greater role, or where climate scenarios suggest that such drivers are likely to become more/less significant in the future.

In closing, we emphasize that the predictive skill of hydrological models under different climate conditions should be considered routinely, particularly when results are used to inform adaptation decision making. Thus, it is important that codes of good practice are established to ensure models are applied in consistent and appropriate ways. On the basis of our findings, we offer the following five recommendations:

- Clearly articulate the objectives of the climate assessment; these will define the options in the next four choices (below).
- Set up the DSST to select the best available analogues of expected annual mean, seasonal mean, or subseasonal (extreme) climate conditions for model training and evaluation, depending on the study objectives.
- Apply multiple performance criteria that are pertinent to the study objectives when assessing the transferability of model parameters between contrasting climate conditions; do not rely on a single performance metric.
- 4. Test parameter transferability using a range of catchment types to better appreciate the form(s) of hydroclimatic regime that are simulated with more or less reliability by a given model, and for the specified objective function(s).
- 5. Use a multimodel ensemble in conjunction with an objectively based averaging technique—ideally BMA or GRA—to obtain the most reliable estimate of future river flow under a changing climate.

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