# Geographically Weighted Visualization: Interactive Graphics for Scale-Varying Exploratory Analysis 

Jason Dykes and Chris Brunsdon


#### Abstract

We introduce a series of geographically weighted (GW) interactive graphics, or geowigs, and use them to explore spatial relationships at a range of scales. We visually encode information about geographic and statistical proximity and variation in novel ways through gw-choropleth maps, multivariate gw-boxplots, gw-shading and scalograms. The new graphic types reveal information about GW statistics at several scales concurrently. We impement these views in prototype software containing dynamic links and GW interactions that encourage exploration and refine them to consider directional geographies. An informal evaluation uses interactive GW techniques to consider Guerry's dataset of 'moral statistics', casting doubt on correlations originally proposed through visual analysis, revealing new local anomalies and suggesting multivariate geographic relationships. Few attempts at visually synthesising geography with multivariate statistical values at multiple scales have been reported. The geowigs proposed here provide informative representations of multivariate local variation, particularly when combined with interactions that coordinate views and result in gw-shading. We argue that they are widely applicable to area and point-based geographic data and provide a set of methods to support visual analysis using GW statistics through which the effects of geography can be explored at multiple scales.


Index terms - Geographical weighting, exploratory data analysis, scale, multivariate, directional, interaction, coordinated views

## 1 INTRODUCTION

Definitions of geovisualization and information visualization suggest mutual exclusivity - yet in practice much geovisualization is dependent on and informed by aspatial graphics and many views that combine elements of geography and statistical spaces provide useful insights. The value added in combining these elements to help insights. The value added in combining these elements to help
explain geographical processes is that exploring relationships between measured phenomena that are 'near' in statistical space and geographical space may provide insights that cannot be achieved with maps or statistical graphics alone. The definition of 'nearness' is fundamental to such approaches: How near do two houses have to be before the selling price of one influences the selling price of the other? How near does an area with a high crime rate have to be from a house to influence its selling price? Is the relationship a simple monotone or might there be more than one 'critical distance' at which interactions occur? And do these relationships vary across space and with direction? These kinds of questions consider geographical interaction between variables but also imply that an investigation of scale must be considered.

A popular approach to the investigation of geographical patterns is the concept of local statistics [11,18] perhaps arising from Openshaw's stated dissatisfaction with 'whole map statistics' [15]. A point location $\mathbf{u}$ in a study area is selected, and some statistical technique applied to the data weighted by proximity to $\mathbf{u}$. Applying this procedure to a number of locations spanning the study area gives an indication of the spatial variability in the distribution of the data values. Such approaches have incorporated not only formal inferential methods, such as the $g$-statistic [11], or geographically
weighting reduces with distance is controlled by a parameter $h$ : typically $h$ is either a fixed distance for all $\mathbf{u}$, or chosen to equal the distance from each $\mathbf{u}$ to its $k$ th nearest neighbour [1]. In the former case the scale of localisation is fixed for all $\mathbf{u}$ in physical space, and in the latter it is fixed for all $\mathbf{u}$ in areas of a given density. Mapping the results for each location for some given $h$ or $k$ is an effective way of showing local changes in the distribution of some measured attribute, or changes in the relationships between several of these However, a number of spatial processes operate at several scales simultaneously. Consider for example house prices which may exhibit patterns within streets, between parts of a town and between national regions, or topographic features whereby a local peak may be part of a larger valley when measured at a wider scale [20].

It can be helpful to consider the effect of varying either $k$ or $h$ in order to identify all scales at which patterns operate, particularly when spatial data are analysed in an exploratory situation Fotheringham et al.[8] describe the process of so doing as involving a 'spatial microscope' whose focal length may be varied to allow the identification of patterns at different scales. For example, Foody [7] uses GWR to explore the relationship between species richness and three explanatory environmental variables in sub-Saharan Africa, and considers how spatial patterns in the geographically varying regression parameters change in association with $h$ in order to investigate the underlying geographical scale of the relationships between these variables. Scale-space analysis [13] provides a multiscale framework for analysing data recorded in a regular rectangula array in this manner and is used for feature recognition. It may, along
measured using irregular zones. They are suitable for investigating the properties of spatial data at a range of scales. They include standard choropleth maps, maps of geographic weightings for any $h$ (weighting maps) maps of geographically weighted means (gw-mean maps) and local variations from the mean (gw-residual maps), a localised (GW) version of the box-and-whisker plot that we term a gw-boxplot and a scalogram - a plot showing the variation of localised summary statistics as the value of $h$ changes. Our prototype software contains interactions and visual encodings that are both geographic and geographically weighted. In combination these views and coordinated interactions are designed to help analysts gain insight into spatial patterns through which geographic processes may be characterised and understood.

## 2 Context : Challenges for Multivariable Spatial <br> Analysis - Guerry's Moral Statistics of France

By way of example we focus on a particular multivariate geographic data set - that collated and graphically represented by André-Michel Guerry in his 'Essai sur la statistique morale de la France' [19]. Guerry meticulously collected and importantly related data on a number of themes for the departments of France to analyse social issues in the early $19^{\text {th }}$ century. He considered geography predominantly by visually inspecting his univariate choropleth maps and identified geographic outliers and some regional trends. Visual inspections were used to hypothesize about relationships between variables. Friendly [9] uses statistical and graphical methods to revisit Guerry's data set. Regression analysis shows that some of Guerry's postulated associations do not hold and that others omitted by Guerry exist. Geography is considered in a hierarchical manner by comparing data for departments in each of the five regions of France and suggestions are made about relationships between these regional aggregations [10]. Multivariate graphics and conditioned choropleths [4] are used to augment Guerry's univariate maps.

## 3 Geographically Weighted Graphics

The geographically weighted interactive graphics, or 'geowigs', developed here are graphical representations of geographically weighted summary statistics.

### 3.1 Summary Statistics

A number of geographically weighted summary statistics can be calculated at locations in a spatial data set [2]. The most fundamental of these is the geographically weighted mean. This is simply a moving spatial window mean smoother. If we have a number of observations with values $x_{i}$ at points $\mathbf{u}_{i}$, then the geographically weighted mean at any point $\mathbf{u}$ is

$$
\begin{equation*}
M(\mathbf{u}, h)=\frac{\sum x_{i} w_{i}(\mathbf{u})}{\sum w_{i}(\mathbf{u})} \tag{1}
\end{equation*}
$$

where $w_{i}(\mathbf{u})$ is the weight applied to the observation at location $\mathbf{u}$ when computing the geographically weighted mean at location $\mathbf{u}$. This weight is typically a monotone decreasing function of the

$x 1$ : population per 'crime against persons'
$x 2$ : population per 'crime against property'


Fig. 1. Unclassified choropleth maps of Guerry's six key variables.
This last expression demonstrates that a geographically weighted mean is the mean of a mass-point distribution with a discrete set of (value, probability) pairs $L=\left\{\left(x_{i}, W_{i}\right)\right\}$. The other locally weighted summary statistics of importance here are the distributional quantiles associated with the construction of boxplots. They are computed in terms of the quantiles of the mass-point distribution $L$. If the ( $x_{i}, W_{i}$ ) pairs are ordered in increasing values of $x_{i}$ then the cumulative distribution of $L$ makes a series of discrete 'jumps' at each value of $x_{i}$
using unclassified choropleths (Figure 1). The colour schemes used throughout are continuous and based upon Brewer's sequential and diverging schemes [12]. Guerry regarded high values are being indicative of moral character and so in accordance with Guerry and Friendly's maps low data values are represented by darker shades to reveal 'la France obscure and la France éclairée'. We use the YlOrBr scheme [12] for maps of original statistical values and GW means. Spatial variation in any single variable can be depicted at a range of scales by displaying GW means. Choropleth maps for variable 1 are shown in Figure 2 with five values of $h$ increasing from left to right. $M(\mathbf{u}, h)$ is precomputed for selected values of $h$ in our implementation. The weighting maps (top) show the relative contributions of local departments $w_{i j}$ in the calculation of $M(\mathbf{u}, h)$ for a single unit using the YlGn scheme [12] - in which zones making no contribution to the statistic are light shaded yellow. Symbolism that is consistent across the resultant gw-mean maps (middle) shows the absolute effects of increasing $h$ on the local weighted value of a single statistic. Symbolism that varies between gw-mean maps (bottom) shows the relative effects of varying $h$. Each map shows the local statistic for 'population per crime against persons' with 'nearness' being considered more widely successively from left to right. The value computed for any location $\mathbf{u}_{i}$ is dependent upon the geography considered in calculating the statistic. In this case the values are calculated for the 86 department centroids.

The univariate gw-mean maps reveal some regional trends at particular scales, but it can be useful to compare local variation at a range of scales. We achieve this by generating $g w$-boxplots at a range of scales from GW percentiles, as discussed in section 3.1. In Figure 3 the light grey boxplots represent the national figures (not weighted and consistent across all values of $h$ ). The green gw-boxplots show local variation for any combination of $\mathbf{u}$ and $h$, which tend towards the national values as $h$ increases (from left to right). The smaller grey circles represents the local value $\mathrm{x}(\mathbf{u})$, the larger green circle represents the GW mean - $\mathrm{M}(\mathbf{u}, h)$.

The geographically weighted box and whisker plots visually encode the GW median and GW percentiles. A series of these allows multivariate GW relationships to be considered at a variety of scales. The gw-boxplots contrast with the maps in that they are projected in a statistical space with the $y$-axis representing statistical values and the x -axis ordering a series of alternative gw-boxplots by variable ( x ) or scale (h).



Fig. 3. gw-boxplots for a single department - variable 1 'population per crime against persons' at five different scales ( $h=25$ to $h=200$ ).

Figure 3 shows $g w$-boxplots for $i=23$, Creuse, at five scales. The department is evidently a local maximum at $h=25$, as suggested clearly by the light zone on the map and as identified by Guerry, though it is not considered a statistical outlier in the boxplot. This maximum is not persistent across scale however. Locations to the north have higher GW mean values at a scale of $h=50$ and several departments to the east have higher GW means at $h=100$ as shown in the gw-mean maps of Figure 2. Not unrelated is that fact that 'local' variability in 'crime against persons' around Creuse at scale $h=50$ is greater than that observed in the national data set. These trends and findings are more subtle and more spatial than those detected in previous analyses, including Guerry's identification of a local high, the regional analysis of Friendly and the national 'obscure / éclairée' trend. The way that local maxima depend upon the definition of 'nearness' and that a process operating at a local scale (between $h=25$ and $h=50$ ) focused on Creuse is resulting in more variation than is evident in the wider national data set may be of some interest and is indicative of the kind of knowledge that might be elicited from geowigs.

The scalogram is designed to help explore such variations and the scales at which they occur. Whilst the gw-mean maps are projected in geographical space, the scalogram fills an abstract space with orthogonal geographic and statistical dimensions. The x-axis is used to represent $h$ and the y -axis for $\mathrm{M}(\mathbf{u}, h)$. Lines linking $\mathrm{M}(\mathbf{u}, h)$ for all $h$ for every $\mathbf{u}_{\mathbf{i}}$ enable us to consider variation in multiple zones at a range of scales for any variable. The three views in Figure 4 show the original data mapped as a choropleth (left), the scalogram for $i=23$ - Creuse, which is the maximum value in the original data (center), and the complete scalogram for all 86 departments (right). The vertical lines in the scalograms show values of $h$ for which $\mathrm{M}(\mathbf{u}, h)$ has been computed. The path of the single line in the central scalogram of Figure 4 corresponds with the GW means in Figure 3 (the green circles). Flatter sections of the lines in the full scalogram (right) denote departments where varying scale or the definition nearness has little effect on the GW value.

5. Map views - choropleth map of original values, gw-mean map, gwresidual map and weighting map.

The way in which the GW mean centred on Creuse decreases as our definition of 'nearness' increases in scale is shown by the falling profile in Figure 4 (centre). The reducing dominance of the location as a 'high' as we expand our definition of 'nearness' is reflected in the profile dipping beneath those of other departments in Figure 4 (right). The bottom line in Figure 4 (right) is Corsica, and the lack of any local effect until $h=100$ relates to the geographic isolation of the island. Steeper line sections within a scalogram draw attention to local variability at a particular scale and show the scale at which this occurs. These are characteristic of a number of departments. Some departmental scalogram profiles contain local maxima or minima identifying a scale at which local variation is particularly atypical.

### 3.3 Interactions - Software Implementation

Our demonstrator software contains three linked views: a map, $g w$ -
local high and blue is negative, denoting a local low ; the weighting map - a sequential scheme shows the relative weightings of all departments in localities based upon a particular source department the visual emphasis relates directly to the contribution of each department to $\mathrm{M}(\mathbf{u}, h)$ (see Figure 2).

All of the views are coordinated so that any interaction that changes $x$ (the mapped variable) or $h$ (the scale used in weightings) results in appropriate updates to all views. Links between the scalogram and map are dynamically updated as the map is clicked; selecting a location on the map updates the gw-boxplots and weighting map so that they are centred on the relevant zone (Figure 6). gw-boxplots for five departments are shown in Figure 6 to highlight the spatial differences in scale effects for a single variable. The departments selected are the 'outliers' identified by Friendly.

original values $x I$ - - oulbiber departments hightighted


Fig. 6. Choropleth and gw-boxplots for one variable at a single scale five different departments, those selected identified as 'outliers' [10].

Our software shows gw-boxplots for all variables in the data set simultaneously and so the interactions described occur for multiple variables concurrently. Figure 7 shows the effects of interactively changing the mapped variable $(x)$, the scale $(h)$ and the zone of interest $(i)$ whilst undertaking exploratory analysis.


Shading used in the map is reflected in the scalogram and so when weighting maps are displayed, colour encodings in the scalogram emphasize items according to their weighted contribution to the locality [6]. Figure 8 illustrates with maps and scalograms at $h=50$ for two variables: $x 1$ (top set) and $x 2$ (bottom set). In each case the first scalogram is shaded according to the original statistical values of the selected variable ( $x$ ) recorded for each department (i). The second scalogram uses gw-shading - GW highlighting in which the colour of each line is varied such that departments closest to that selected on the map are visually emphasized. The currently selected values of $h$ and $i$ are shown by emboldening the appropriate vertical line in the scalogram and through a weighting map focused on the brushed spatial unit. In Figure 9, the graphics use the format shown in Figure 8 and focus on $i=69$, Rhône. The peak in the darkest curve ( $i=69$ ) indicates a scale effect that may be of interest.

These visual encodings constitute new graphic types for geographic enquiry. When combined, the dynamic features of these geographically weighted interactive graphics or 'geowigs' provide the basis for exploring local variations in the effects of scale on a series of geographic variables. This configuration supports rapid comparison and exploration. Computing the geographically weighted statistics and subsequent use of visual mappings provides a spatial perspective on the analysis of geographic data. In terms of visual information seeking we are filtering by geography in two ways - by location (u) and nearness ( $h$ ) and provide graphical details on demand (gw-boxplots and scalograms). The geographic nature of our enquiry requires the Gestalt of the graphical overview and so maps are provided concurrently. Dynamic brushing helps relate graphical overview with graphical detail as data are filtered.

## 4 Geographically Weighted Analysis

The graphic types introduced here show that the identification of maxima, minima and notable 'outliers' is scale dependent when considering geographic data and draw attention to these dependencies. Our preliminary analysis allows us to suggest patterns at a range of scales. Individual departments identified as 'outliers' in Guerry's data set may not be atypical for all variables at all scales (Figure 7). The shapes of the scalograms help us relate local and national variations in single variables. For example, when comparing the full scalograms in Figure 8, the wider range of values of $\mathrm{M}(\mathbf{u}, h)$ at $h=200$ for $x 1$ than $x 2$ suggest that trends measured at a national scale are more dominant in case of the former variable ('crime against persons') than the latter ('crime against property').

Equally, we can identify particular scales at which local effects occur. For example, in Figure 9, Rhône $(i=69)$ has a low value for $x 2$ at low values of $h$, but is part of a wider locality with values of 'crime against property' above the national average where $h=50$ and $h=75$. The peak in the curve suggests that, relative to other departments, Rhône is a local high for 'crime against property', but only when considered at certain scales. These scales do not correspond to either the highest resolution available (the departments for which the data were originally collected) or a formal regional scale (the regions into which departments are aggregated in the administrative hierarchy $\lceil 10\rceil$ ). The peak suggests that there is more



Fig. 9. scalograms with statistical and geographically weighted shading $\left(x_{i}\right.$ and $\left.w_{i j}\right) . i=69, x 2$. The graphics use the format shown in Figure 8 and focus on $i=69$, Rhône. The peak in the darkest curve of the scalograms $(i=69)$ indicate a scale effect that may be of interest.

Another feature of the interactive nature of the geowigs presented here is the ability to 'strum' the set of scalogram curves - here 'strumming' means running the cursor quickly up or down the curves while brushing. Highlighting each curve in quick succession gives an indication of how unusual the shape of the scalogram curve is. Not only has this approach highlighted an effect at an unexpected scale, in the case of Rhône, it has also demonstrated that this is localised to one particular area. Processes may work at different scales in different places.

Other geographic patterns are detectable in the GW views. LoireInferiure is notable as being unlike its immediate locality (which has nationally high values) in variable 5 (illegitimate births) despite having an individual value close the national statistical average; Lozere and Rhône are local highs and local lows in variables 6 ('suicide') and 2 ('crime against property') respectively and Loiret is spatially invariant when variable 3 ('literacy') is considered. These

## 5 Directed Geographic Weighting

Weighting has been applied isotropically thus far, with weighting functions depending only on the distance between a pair of points, and not on their angular separation. However direction, as well as distance, plays a key role in the study of many geographical phenomena. In the domain of physical geography there are many examples, such as wind speed, direction of water flows and orientation of faultlines. Examples in human geography include population migration flows and the direction of commuting patterns When such phenomena and processes are considered, similarity between a pair of places may not just depend on their distance apart, but also on the direction from one place to the other. For example, if this direction were coincident with population flow, one might expect two places to have more social characteristics in common than otherwise.

We extend the idea of geographical weighting to incorporate direction as well as distance by pre-multiplying the expression for $w_{i}$ by the expression

$$
\begin{equation*}
\exp \left(-\lambda \cos \left(\theta_{i}-\varphi\right)\right) \tag{4}
\end{equation*}
$$

Here, $\theta_{i}$ is the angle of the path between locations $\mathbf{u}$ and $\mathbf{u}_{i}$ and $\varphi$ is the principal direction of the weighting (angles are measured counter-clockwise from the east). For a fixed distance, $\mathbf{u}_{i}$ values along this direction from $\mathbf{u}$ will gain the highest weighting. Those in the opposite direction will receive the lowest weighting. The parameter $\lambda$ controls the relative sharpness of the directional effect Setting $\lambda$ to zero removes any directional bias in the weighting, while increasing it results in an expansion of the ratio between the highest and lowest weight values.



scalogram - $x 1, i=82$ anisotropic
$\lambda=2, \varphi=90$ (north)



For example, department 82, Tarn et Garonne, shows interesting variation when the directionless GW mean is compared with directed GW means at $90^{\circ}$ (north) and $180^{\circ}$ (west) at multiple scales. Whilst Tarn et Garonne has a low value of variable xl ('crime against persons') when compared to the national distribution at a scale of $h=50$, the directionless GW mean indicates a value close to the local median and the department is thus locally typical (Figure 10). If we consider the directed statistics however, more spatial structure is revealed. With $=2$ and $=90$ (directed GW mean with bias towards the north) Tarn et Garonne is identified as a local directional low due to the high value of the northern neighbour - department 46, Lot. With $=2$ and $=180$ (directed GW mean with bias towards the west) Tarn et Garonne is identified as a local directional high due to the lower values of neighbours to the west, particularly the immediate neighbours - Lot et Garonne ( $i=47$ ) and Gers ( $i=32$ ). There is evidently directional structure in the local statistics associated with Tarn et Garonne, which exhibits variously typical, low and high values of 'population per crime against person' depending upon the uniform, northern and western directional biases used in calculating the local statistic. This explains the colour profile of outlined department 82, Tarn et Garonne, in the residual maps of Figure 10.

These differences are not consistent across scales. The local statistics for Tarn et Garonne are relatively independent of scale from $h=50$ upwards when the directionless local statistic is considered, but when a northern bias is applied to the statistics ( $=2$ and $=90$ ) the considerable variation in values to the north results in a profile showing that Tarn et Garonne varies from local low, to local average to local high through scales from $h=50$ to $h=100$. There is less scale dependency in the western biased GW means ( $=2$ and $=180$ ) as there is less variation in values with scale to the west of the department. Here, Tarn et Garonne is regarded as a local high across scales from $h=50$ upwards (at $h=25$ neighbouring zones make little contribution to the local statistic). These relationships are depicted in the $g w$-shaded scalograms and multi-scale gw-boxplots shown in Figure 11.

A single measured value in space can thus be considered low, high and typical in relation to its neighbours and these characteristics can be variously scale dependent and scale invariant when direction is considered. These differences are important because as we have seen, geographic phenomena are often directional. This directional analysis uses geowigs to demonstrate some of the complexity associated with geographic relationships - spatial processes are neither scale invariant nor isotropic. When we consider a value recorded in space its relationships with 'near' neighbours depend upon definitions of locality and directional emphases. Such differences are difficult to detect in standard choropleth maps and the GW statistics can help with our exploratory spatial data analysis. Interactive visualization of the type described here in our geowigs allows us to explore various scale-based definitions of locality and nearness and to investigate the effects of directional bias upon relationships between attributes recorded in geographic spaces.
focus is predominantly on the six key quantitative variables used in Friendly's work $[9,10]$ the techniques are extensible to higher numbers of variables.

There is considerable potential for extending and exploring the techniques outlined here and using them further. For example, it may be helpful to benchmark geowigs, by considering their performance when applied to a test bed of geographical data sets - investigating the change in outcome when different sizes and shapes of geographical regions are used. Doing so may help explore the dependence of the GW mean on the geometry of nearby regions at low values of $h$ and relate this effect to those associated with the aggregation of continuous geographic phenomena into discrete irregular units for enumeration. The locally weighted statistics are computed on centroids associated with irregular units in our implementation. The statistics could, however be centred on any points, such as those comprising a regular grid. This might be useful for speeding up certain visualisation routines, particularly when large numbers of spatial units are involved, and in such situations it would not be necessary to compute a local statistic for each unit. Comparing geowigs generated from discrete units with those produced from more regular continuous representations of phenomena in geographic space (perhaps using centroids re-allocation techniques [14]) would enable us to explore a number of issues relating to the scale effects associated with alternative models of geographic information. Additionally, our focus here has been predominantly on highlighting multi-scale effects for individual variables, however, one could extend the ideas of Brunsdon et. al. [2] by measuring local multivariate patterns and mapping a GW correlation coefficient. This would enable the effect of local bivariate association to be explored at different scales, using a scalogram based upon GW correlation instead of the GW mean. Each of these techniques could be used with non-Euclidian distances, such as estimated travel time - perhaps a more realistic indicator of potential human interaction.

In commenting on Guerry's original maps, Friendly [10] states that "at the very least, this work testified to the importance of detailed data, sensibly presented, to inform the debate on the relations of crime and education." The techniques presented here are intended, at the very least, to draw attention to geographically weighted graphics and interactions in visualization and to inform debate on the possibilities for using interactive graphics to explore and reveal spatial structure at multiple scales in multivariate and anisotropic geographic data. By adapting ideas from scale-space analysis to irregular, multivariate data we have developed techniques for geographers and policy analysts to explore regional variability in relationships between social variables. These techniques provide instruments for helping uncover processes operating in specific localities and at particular scales and can draw attention to some of the subtleties of spatial information as it encodes geography - such as the effects of using zones of irregular shape and of dealing with scale using an aggregated hierarchical approach. We hope that they may improve understanding of our models and our geography and support informed decision-making.

## AcKnowledgments

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