

Politician preferences, law-abiding lobbyists and caps on political contributions

Ivan Pastine · Tuvana Pastine

Received: 20 March 2009 / Accepted: 29 September 2009
© Springer Science+Business Media, LLC 2009

Abstract The effect of a contribution cap is analyzed in a political lobbying game where the politician has a policy preference. In contrast to the previous literature without politician policy preferences, more restrictive binding caps always reduce expected aggregate contributions. However the initial imposition of a cap increases contributions if the politician mildly favors the low-valuation lobbyist's policy. The introduction of policy preferences permits analysis of monied interests' policy influence. A more restrictive cap makes it more likely that the politician enacts the policy he would have enacted in the absence of lobbying, even in cases where expected aggregate contributions increase.

Keywords All-pay auction · Campaign finance reform · Explicit ceiling

JEL Classification D72 · C72

"Because it costs so much to run for office, interests with big money to contribute to candidates or spend on ad campaigns are able to get special access in Congress." Senator Russ Feingold (D-WI)

"Americans believe that political representation is measured on a sliding scale. The more you give the more effectively you can petition your government." Senator John McCain (R-AZ)¹

1 Introduction

The concept of representative democracy is founded on the proposition that the actions of elected representatives in some sense reflect the will of the people. Either the public votes

¹Quoted on the senators' web sites, March 2008.

I. Pastine
School of Economics, University College Dublin, Belfield, Dublin 4, Ireland

T. Pastine (✉)
Department of Economics, Finance and Accounting, National University of Ireland Maynooth,
Maynooth, County Kildare, Ireland
e-mail: Tuvana.Pastine@nuim.ie

for people whose views reflect their own, or the desire to be reelected leads politicians to try to act as though their views reflected the public's. In either case it is likely that an elected politician has preferences over policy alternatives.

There is concern that the need to raise money to finance election campaigns is diluting this fundamental premise of representative democracy. In 2008 the average cost of a successful campaign for the House of Representatives was \$1.3 million, which represents a real increase of 53% in a decade. Over the same period the average cost of a winning Senate campaign increased by 21% in real terms to \$6.5 million.² The need to raise funds may take time away from other duties and raises the concern that legislative outcomes may be driven by money.³

In the United States there have been numerous attempts to regulate campaign financing by imposing caps on political contributions.⁴ The current Federal regulation on campaign financing is the Bipartisan Campaign Reform Act of 2002, also known as the McCain-Feingold Bill. The act limits an individual's contributions to a candidate to a maximum of \$2,300 per election and to a political action committee to a maximum of \$5,000 with built-in increases for inflation. However it is a complicated piece of legislation which provides various avenues for contributors to direct funds in support of a candidate. The current effective legal limit on an individual's total contributions is \$70,100 in any two-year period.⁵

Caps on political contributions are put in place with the desire to reduce the influence of special interest groups by lowering the total special interest group money in politics. Natural intuition suggests that contribution caps would result in decreased aggregate contributions. However Che and Gale (1998), henceforth CG, challenge this intuition in an all-pay auction setting where lobbyists have different valuations of a political prize. CG show that a more restrictive cap can level the playing field, inducing greater competition and higher aggregate contributions from lobbyists.⁶ In CG the politician has no preference over the policy alternatives supported by the lobbyists. This paper extends CG by allowing the politician to have a preference for the policy position of one of the lobbyists contesting for the political prize.⁷

²For summary statistics see the web sites of the Campaign Finance Institute and the Center for Responsive Politics, www.cfinst.org and www.opensecrets.org respectively.

³It is well documented that larger contributors are more likely to gain access to legislators and that they lobby members with positions of power in congressional committees more heavily (Hall and Wayman 1990; Langbein 1986; Ansolabehere et al. 2002 and Wright 1990). There is extensive literature documenting that institutional contributors appear to be acting as rational investors; see Ansolabehere and Snyder (1999), Grier and Munger (1991), Grier et al. (1994), Hart (2001), Kroszner and Stratmann (1998, 2000), Lott (2000), Milyo (1997), Pittman (1998), Romer and Snyder (1994), Snyder (1990, 1992, 1993), and Zardkoohi (1998).

⁴A number of other countries also have contribution limits. Examples include France, India, Israel, Italy, Japan, Mexico, Russia, Spain, Taiwan and Turkey. See www.aceproject.org.

⁵For the contributions limit chart see <http://www.fec.gov/pages/brochures/contriblimits.shtml>. See the Federal Election Commission's website www.fec.com for details. For state-level offices individual states are in charge of their own campaign finance regulations. All states except for Illinois, New Mexico, Oregon, Utah and Virginia have contribution limits. Details on various state level contribution limits are provided by the National Conference of State Legislatures, www.ncsl.org.

⁶Drazen et al. (2007) find a related result in a very different framework. In an incomplete information environment Gavious et al. (2002) find that expected spending can go up when the cap is more restrictive. Amegashie (2003) analyzes caps in all-pay auctions when a committee awards the prize. Austen-Smith (1998) shows that caps can reduce the incentive to grant access for fund-raising purposes and result in legislators spending more time gathering information.

⁷There is extensive empirical evidence that the policy position of the politician is an important determinant of politician behavior. Of the 36 empirical papers which study ideology or party affiliation surveyed in Ansolabehere et al. (2003), all but one find policy position significant for predicting congressional roll-call votes.

Modeling politicians with policy preferences is standard in many workhorse models in the vast political lobbying literature. For instance, in Grossman and Helpman (1996) politicians have preferences derived from the preferences of their constituents and in equilibrium lobbyists have a stronger electoral motive to contribute if the lobbyists would fare very differently depending on the policy platform alternatives politicians adopt. In the access fee model of Austen-Smith (1995), contributions are a means of signaling the degree to which the lobbyist's preferences are aligned with those of the politician. In Denzau and Munger (1986), lobbyists offer legislators campaign resources to buy political favors and *ceteris paribus* they tend to contribute to legislators who do not have strong policy preferences as those legislators are easier to sway.⁸ In this paper we extend the literature by incorporating politician preferences into the CG framework to analyze the effect of contribution caps where lobbyists contribute to buy policy favors.

In frameworks without politician policy preferences, Kaplan and Wettstein (2006) and Gale and Che (2006) analyze caps when lobbyists may be willing to break the law and possibly contribute more than the legal limit. Here we continue to maintain the CG assumption that lobbyists are law-abiding and do not attempt to circumvent the law as written. Hence we analyze the effect of a contribution cap in the baseline case where the law operates as intended.⁹

In contrast to CG, we find that making a binding cap more restrictive always decreases expected aggregate contributions. This is true no matter how mild the politician's policy preference may be. The lobbyist with the preferred policy position does not need to match his rival's contribution in order to win. This implies that the effect of the cap is qualitatively different from the effect of the cap when the politician is indifferent between policy alternatives. In CG both lobbyists are constrained by the cap: Given their rival's strategy they would each like to exceed the limit if it were possible to do so. However, when the politician has a policy preference the cap effectively constrains the less-preferred lobbyist, but not the preferred lobbyist. The favored lobbyist never needs to contribute by the full amount allowed by the cap in order to guarantee victory since the unfavored lobbyist cannot contribute more than the cap. Hence the cap always helps the preferred lobbyist. Making a binding cap more restrictive tilts the playing field in favor of the preferred lobbyist, reducing the aggressiveness of his rival. This leads to decreased expected contributions overall.

If the politician mildly prefers the policy position of the low-valuation lobbyist, the main message of CG that a contribution limit may increase expected total contributions survives at the point where the cap just becomes binding. In this case the preference of the politician is not too strong, so without a binding cap the lobbyist with the higher valuation of the political prize is in an advantageous position. The introduction of a binding cap switches the advantage to the favored lobbyist (the low-valuation lobbyist). This fosters more aggressive bidding by the low-valuation lobbyist and results in higher expected aggregate contributions. Hence a politician who is concerned with raising money may support a barely binding cap over no cap.

⁸In order to disentangle the electoral motive from the buying policy favors motive of contributions and to establish clear causality between money and voting behavior, Stratmann (2002) examines repeated votes on the same piece of legislation: the repeal of provisions of the 1933 Glass-Steagall Act. The act prohibited bank holding companies from owning other financial services companies. The repeal was rejected by the House in 1991, and it then passed in 1998. It was strongly favored by banking interests but also strongly opposed by insurance and securities interests. Stratmann finds that an extra \$10,000 in contributions was associated with an 8% increase in the probability of a House member voting to repeal the prohibition.

⁹See Pastine and Pastine (2008) for the case where the politician has policy preferences and lobbyists circumvent the cap.

The introduction of policy preferences permits the analysis of the effect of a cap on the influence of monied interests on policy. The literature often cites the level of total political contributions as a measure of the degree of influence of money on policy. We suggest a different measure that captures the concern that money may be driving policy choices: The equilibrium probability that the politician does not enact a policy that he would have enacted in the absence of lobbying. The choice of measure matters. With policy preferences the imposition of a cap may lead to increased aggregate contributions while at the same time making it more likely that the politician enacts his preferred policy, reducing the influence of lobbying effort. We find that a more restrictive contributions cap always makes it more likely that the politician enacts his favored policy. Furthermore lobbying activity will be observed on fewer policy issues.

However our theoretical findings imply that empirical evaluation of the effect of a cap is a nontrivial challenge. We find that even when the cap severely restricts donations, in equilibrium very few contributions will be at the limit. Hence the standard practice of looking at the proportion of donations at the maximum permitted amount, as for example in Ansolabehere et al. (2003), may fail to identify binding caps. We also show that contribution caps may redistribute political contributions from senators and politicians from large or urban districts to representatives and politicians from smaller or rural districts.

To the best of our knowledge this is the first paper to characterize the equilibrium of a preferential treatment all-pay auction with a cap. We first analyze the equilibrium of the lobbying game without a cap. We adapt Konrad's (2002) all-pay auction with additive preferential treatment to allow bidders to have different valuations of the prize. We then examine the effect of a cap on contributions. We conclude with a short discussion of the limitations of the model and a possible extension to help study campaign finance regulations in the European context where the cap is on expenditures rather than on contributions.

2 The model

Two risk-neutral lobbyists compete for a political prize. The prize arises due to a policy choice of a politician who holds a political post. The prize may be a vote on impending legislation but may also be more subtle; such as attaching a rider to an upcoming bill creating a regulatory loophole, or pushing a particular wording in a committee. The value of the political prize to lobbyist 1 is denoted by v_1 , and the value of the prize to lobbyist 2 is v_2 , $v_1 > v_2 > 0$. The lobbyists make simultaneous contributions (bids), b_1 and b_2 , to the politician in power. The contributions are not returned to the lobbyist whose efforts fail. Since the contributions are sunk both for the winner and the loser, this political lobbying game is an all-pay auction.¹⁰ If bidder 1 (lobbyist 1) wins the prize, his payoff is $v_1 - b_1$; if his rival wins bidder 1's payoff is $-b_1$. Bidder 2's payoffs are constructed in the same manner.

In this paper we allow the politician to have a preference over the policy alternatives supported by the two lobbyists. The politician's preference may be ideologically based or it may be induced from the preferences of constituents who will be voting in the future. The interest groups lobby the politician and the politician awards the political prize based on

¹⁰The complete information all-pay auction without a cap has been analyzed by Hillman and Riley (1989), Baye et al. (1993, 1996) and Siegel (2009). See Yildirim (2005) for a contest where players have the option of adding to their previous efforts and see Kaplan et al. (2002) for a model where the size of the reward is a function of the bid.

the contributions and his preference. The lobbyist with the preferred policy position has an advantage since he can win the prize with a smaller contribution than his rival's. The degree of the advantage depends on the intensity of the preference of the politician.

The intensity of the preference for the policy position of lobbyist 2 is put into monetary terms, denoted $\gamma \in (-\infty, \infty)$. For example $|\gamma|$ could represent the expected future campaign costs required to offset the effect of taking a policy position that is unpopular in the politician's district. If the politician favors lobbyist 2's position $\gamma > 0$. If the politician favors lobbyist 1's position $\gamma < 0$. It will be possible to write the proofs much more concisely if we define f as the bidder whose policy is favored by the politician and u as the bidder with the unfavored policy. If $\gamma \geq 0$ then $f = 2$ and $u = 1$, while if $\gamma < 0$ then $f = 1$ and $u = 2$. It will be assumed that the politician awards the prize to lobbyist 1 if $b_1 > b_2 + \gamma$, and to lobbyist 2 if $b_1 < b_2 + \gamma$. In case of a tie, $b_1 = b_2 + \gamma$, each contestant has an even chance of winning the prize. CG is a special case of our framework where the politician does not have a policy preference, $\gamma = 0$. The rules of the game, the valuations of the lobbyists and the preference of the politician are common knowledge.

Simple backward induction in the one-shot game that will be analyzed here would have the politician taking his preferred action regardless of bids since all contributions are sunk. Hence there would be no contributions. Thus implicitly we assume that this one-shot game is embedded in a repeated setting so that the politician has an incentive to reward high contributions in order to keep them coming in the future. However, as long as contributions, preferences and actions are common knowledge among lobbyists, the same lobbyists do not necessarily need to be involved in repeated contests.

3 Equilibrium without a cap

If the politician's preference is too strong, either $\gamma \geq v_1$ or $\gamma \leq -v_2$, the unique equilibrium is in pure strategies where neither lobbyist contributes. The preferred lobbyist can bid zero and still win the prize since it would never be optimal for his rival to contribute more than his valuation. We study all nontrivial cases where the politician has a policy preference $\gamma \in (-v_2, v_1)$. Equilibrium of this contribution game does not exist in pure strategies. The best response to a bid b' of the favored bidder is either to outbid him by $|\gamma|$ or to drop out of the race. In either case the favored bidder's choice would not be optimal.

Lemma 1 below describes the equilibrium. This lemma extends Konrad (2002) to allow the value of the prize to differ between bidders. In Konrad (2002) the bidder with the head-start advantage (the lobbyist with the favored policy in our framework) always has a positive expected value from the contest and the bidder without the head-start advantage has an expected value of zero. However in our framework where bidders have different valuations of the prize this is not always the case. When the politician mildly prefers the policy position of the low-valuation lobbyist the preferential treatment is not strong enough to overwhelm the advantage lobbyist 1 has due to his high valuation. This implies that we need to study the equilibrium in two separate cases.

Lemma 1 *Without a contribution cap, there is no equilibrium in pure strategies if $\gamma \in (-v_2, v_1)$. The equilibrium in mixed strategies is characterized by unique cumulative density functions $F_f(b)$ and $F_u(b)$ for the favored lobbyist's and the unfavored lobbyist's contributions, respectively.*

- (i) If the politician favors the policy position of the high-valuation lobbyist $\gamma \in (-v_2, 0)$ or if the politician “strongly favors” the policy position of the low-valuation lobbyist $\gamma \in (v_1 - v_2, v_1)$, the unique equilibrium cumulative density functions are given by

$$F_f(b) = \begin{cases} \frac{b+|\gamma|}{v_u} & \text{for } b \in [0, v_u - |\gamma|] \\ 1 & \text{for } b > v_u - |\gamma| \end{cases}$$

and

$$F_u(b) = \begin{cases} \frac{v_f - v_u + |\gamma|}{v_f} & \text{for } b \in [0, |\gamma|] \\ \frac{v_f - v_u + b}{v_f} & \text{for } b \in (|\gamma|, v_u) \\ 1 & \text{for } b > v_u \end{cases}$$

- (ii) If the politician “mildly favors” the policy position of the low-valuation lobbyist $\gamma \in (0, v_1 - v_2]$, the unique equilibrium cumulative density functions are given by

$$F_f(b) = \begin{cases} \frac{v_u - v_f + b}{v_u} & \text{for } b \in [0, v_f] \\ 1 & \text{for } b > v_f \end{cases}$$

and

$$F_u(b) = \begin{cases} 0 & \text{for } b \in [0, |\gamma|] \\ \frac{b-|\gamma|}{v_f} & \text{for } b \in (|\gamma|, v_f + |\gamma|) \\ 1 & \text{for } b > v_f + |\gamma| \end{cases}$$

Proof Appendix A. □

From Lemma 1 it is straightforward to derive the expected contributions of individual bidders and the probabilities of winning from the equilibrium distribution functions.

(i) $\gamma \in (-v_2, 0) \cup \gamma \in (v_1 - v_2, v_1)$. On $b \in (|\gamma|, v_u)$ the p.d.f. of the bids of bidder u is $f_u(b) = 1/v_f$. The expected contribution of bidder u is given by

$$E(b_u) = \int_{b_u=|\gamma|^+}^{v_u} x f_u(x) dx = \frac{v_u^2 - \gamma^2}{2v_f}$$

On $b \in (0, v_u - |\gamma|]$ the p.d.f. of the bids of bidder f is $f_f(b) = 1/v_u$. The expected contribution of bidder f is given by

$$E(b_f) = \int_{b_f=0}^{v_u-|\gamma|} x f_f(x) dx = \frac{(v_u - |\gamma|)^2}{2v_u}$$

When bidder u contributes an amount b , he wins the contest if and only if bidder f contributes less than $b - |\gamma|$. Hence the probability that bidder u wins the contest is given by

$$\text{prob}_u = \int_{b=|\gamma|^+}^{v_u} F_f(x - |\gamma|) f_u(x) dx = \int_{b=|\gamma|^+}^{v_u} \frac{x}{v_u v_f} dx = (v_u^2 - \gamma^2) / 2v_u v_f$$

(ii) $\gamma \in (0, v_1 - v_2]$. $f = 2$ and $u = 1$. On $b \in (|\gamma|, v_f + |\gamma|]$ the p.d.f. of the bids of bidder u is $f_u(b) = 1/v_f$. The expected contribution of bidder u is given by

$$E(b_u) = \int_{b=\gamma^+}^{v_f+\gamma} x f_u(x) dx = \frac{v_f + 2\gamma}{2}$$

On $b \in (0, v_f]$ the p.d.f. of the bids of bidder f is $f_f(b) = 1/v_u$. The expected contribution of bidder f is given by

$$E(b_f) = \int_{b_f=0}^{v_f} x f_f(x) dx = \frac{v_f^2}{2v_u}$$

The probability that bidder u wins the contest is given by

$$prob_u = \int_{b=\gamma^+}^{v_f+\gamma} F_f(x - |\gamma|) f_u(x) dx = 1 - v_f/2v_u$$

When the politician mildly favors the policy of the low-valuation bidder, an increase in the intensity of the preference parameter has no effect on the equilibrium probabilities of winning. In this range, the preference of the politician is simply offset by the greater effort of lobbyist 1 (bidder u) while the expected effort from lobbyist 2 (bidder f) remains unchanged.¹¹

Note that the ability to raise funds depends on the intensity of the politician's preference. Politicians with extreme policy preferences generate less competition between lobbyists and hence garner fewer donations. This result is common in models of contributions for policy favors; see for example Denzau and Munger (1986) or Grossman and Helpman (1996).¹² However here a politician with no preference over policy alternatives is not the top fundraiser. It is the politician with mild preference for the low-valuation lobbyist who receives the highest expected aggregate contributions. At $\gamma = v_1 - v_2$, the preference for lobbyist 2's policy position just offsets his disadvantage in the game arising from his low valuation of the prize. In this situation the playing field is leveled (the expected value of the contest to both of the lobbyists is equal to zero) and the expected aggregate contributions are maximized.¹³

¹¹This result is different from the affirmative action paper of Fu (2006) where preferential treatment is modeled as a multiplicative weight. A multiplicative preferential treatment rule augments the bid of the favored bidder by a fixed percentage which gives that bidder an additional incentive to increase his effort. Pastine and Pastine (2009) explore the implications of this difference for affirmative action policy.

¹²In Grossman and Helpman (1996) the party that needs to cater more to constituent preferences, due to lack of existing popularity or party-loyal voter base, receives less contributions from special interest groups.

¹³Note that the politician has an incentive to misrepresent his preference in order to induce greater competition between donors. Denote Γ as the true policy preference of the politician (either ideologically driven or motivated by reelection concerns) and let him choose the allocation rule γ . He would like to enact legislation in line with his policy preference but also cares about total contributions. $|\Gamma|prob_f$ is the expected value from the policy decision and let $U(\text{total contributions})$ be the utility from contributions. If $U'(\cdot)$ is zero the politician does not care about contributions and it would be optimal for him to simply go with his preference, setting an allocation rule $|\gamma| \geq v_u$ even if his true preference is not as strong. If $U'(\cdot) > 0$ the politician would never set an allocation rule $\gamma \in [0, v_1 - v_2]$, since in this range $prob_f$ is constant with respect to γ and expected contributions are increasing. Hence when $\Gamma \in [0, v_1 - v_2]$, it would be optimal for the politician to set $\gamma = v_1 - v_2$. For Γ outside this range there would be an incentive to distort the allocation rule downward from the true policy preference (towards a less extreme allocation rule) in order to increase expected contributions. For sufficiently concave utility there will be a non-degenerate mapping between preferences

Empirically Magee (2002) finds that lobbyists give less to politicians who do not share their policy values. This observation is consistent with the implications of the model. However, the model also predicts that lobbyists give less to politicians who strongly share their policy values. There is no empirical evidence supporting this prediction. Note, however, that in this paper we only study contributions for political favors. Interest groups may also contribute to promote a politician's electoral prospects if the politician's policy preferences are aligned with their own.¹⁴ Often these two motives may be intertwined. Hence while a politician with a strong preference attracts lower contributions from both the unfavored and the favored lobbyist for policy favors, contributions from the favored lobbyist may be high due to the electoral motive.

4 Equilibrium with a cap

Denote m as the level of the contribution cap. The lobbyists are assumed to be law-abiding. Hence neither bidder contributes more than m . A cap restricting contributions to $|\gamma|$ or less would result in the unfavored lobbyist being unable to compete at all. Hence if the cap is too restrictive it completely suppresses all contributions. What follows discusses the nontrivial case where the cap permits contributions greater than the preference parameter, $m > |\gamma|$.

First define some terminology. A “binding cap” is a cap which is lower than the maximum of the upper bounds of the no-cap equilibrium bid supports established in Lemma 1. (i) If the politician favors the high-valuation lobbyist or if the politician strongly favors the low-valuation lobbyist, in the absence of a cap the favored lobbyist mixes in the range $[0, v_u - |\gamma|]$ and the unfavored lobbyist mixes in the range $\{0\} \cup (|\gamma|, v_u]$. Hence a cap $m < v_u$ is binding. (ii) If the politician mildly favors the low-valuation lobbyist, a cap $m < v_f + |\gamma|$ is binding. A cap that is ε less than the maximum of the upper bounds of the supports of the no-cap equilibrium bids is a “barely binding” cap. A “more restrictive cap” refers to a smaller m when the cap is binding.

Lemma 2 below describes the equilibrium with a cap when the politician has a policy preference. As long as the cap does not suppress all contributions, $m > |\gamma|$, there is no pure-strategy Nash equilibrium. This result is in contrast to CG. When the politician does not have a policy preference ($\gamma = 0$) the nature of the equilibrium changes from a mixed-strategy equilibrium to a pure-strategy equilibrium when a very restrictive cap is introduced ($m < v_2/2$) and both bidders contribute the amount of the cap. When the politician has a policy preference, the favored bidder's optimal response to a bid b' is either to bid slightly higher than $b' - |\gamma|$ or to drop out of the contest altogether, so b' would not be optimal for the unfavored lobbyist. The unique equilibrium is in mixed strategies.

Lemma 2 *With a binding contribution cap and $m > |\gamma|$, there is no pure-strategy equilibrium if $\gamma \in (-v_2, 0) \cup (0, v_1)$. The equilibrium is characterized by unique cumulative density functions $F_f(b)$ and $F_u(b)$ for the favored lobbyist's and the unfavored lobbyist's*

and allocation rules. The results of Sect. 4 imply that a similar non-degenerate mapping will also exist with a contribution cap but over the whole range of $\Gamma \in (-v_2, 0) \cup (0, v_1)$, as with a binding cap $prob_f$ is never constant w.r.t. γ .

¹⁴See Ansolabehere et al. (2003) for a survey of these two motives. See Bronars and Lott (1997) for an empirical study testing the vote-buying and electoral motive hypotheses using data on politicians' voting in their final term. They find the latter to be more dominant.

contributions, respectively.

$$F_f(b) = \begin{cases} \frac{b+|\gamma|}{v_u} & \text{for } b \in [0, m - |\gamma|] \\ 1 & \text{for } b > m - |\gamma| \end{cases}$$

and

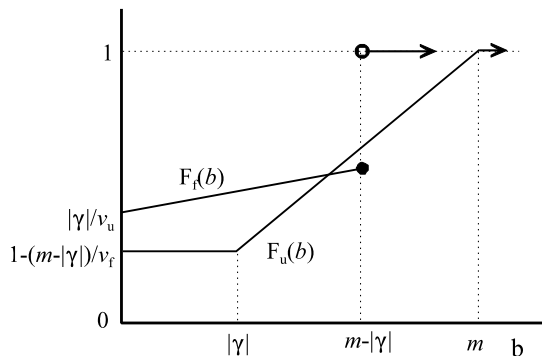
$$F_u(b) = \begin{cases} \frac{v_f - m + |\gamma|}{v_f} & \text{for } b \in [0, |\gamma|] \\ \frac{v_f - m + b}{v_f} & \text{for } b \in (|\gamma|, m] \\ 1 & \text{for } b > m \end{cases}$$

Proof Appendix A. The equilibrium distribution functions of bidder u and bidder f are graphed in Fig. 1. □

A significant feature of the equilibrium is that the favored lobbyist never bids up to the cap. Since the unfavored lobbyist cannot contribute more than the cap, the favored lobbyist always has the option of winning for sure with a contribution just above $m - |\gamma|$. Also note that in equilibrium the unfavored lobbyist has a negligible probability of contributing the maximum amount. This implies that it will be difficult to establish empirically whether an existing contribution cap is binding or not. Natural intuition would suggest that if the cap were binding there would be a large number of lobbyists who contribute the maximum permissible amount. Ansolabehere et al. (2003) argue that the constraint on political contributions is not binding since only 4% of PAC contributions to House and Senate candidates are at or near the legal limit. However, Lemma 2 shows that in equilibrium neither lobbyist has a probability mass at the contribution cap. The favored lobbyist does have a probability mass at the maximum permissible amount less the politician’s policy preference. However one would not expect to see this mass point in actual data since in practice different policy issues are likely to induce different intensities of preferences. Instead one would expect to see the distribution of contributions peaking below the cap, reflecting the underlying distribution of the preference parameter over different policy issues.

In equilibrium it is possible that the unfavored lobbyist contributes more than the favored lobbyist but not by enough to overcome the politician’s preference. Consequently, in an empirical study the evidence of the effect of money on legislative action may appear to be weak. Indeed in their survey Ansolabehere et al. (2003) find that empirical evidence on

Fig. 1 Equilibrium bids with a binding contribution cap. Bidder f ’s policy is favored by the politician



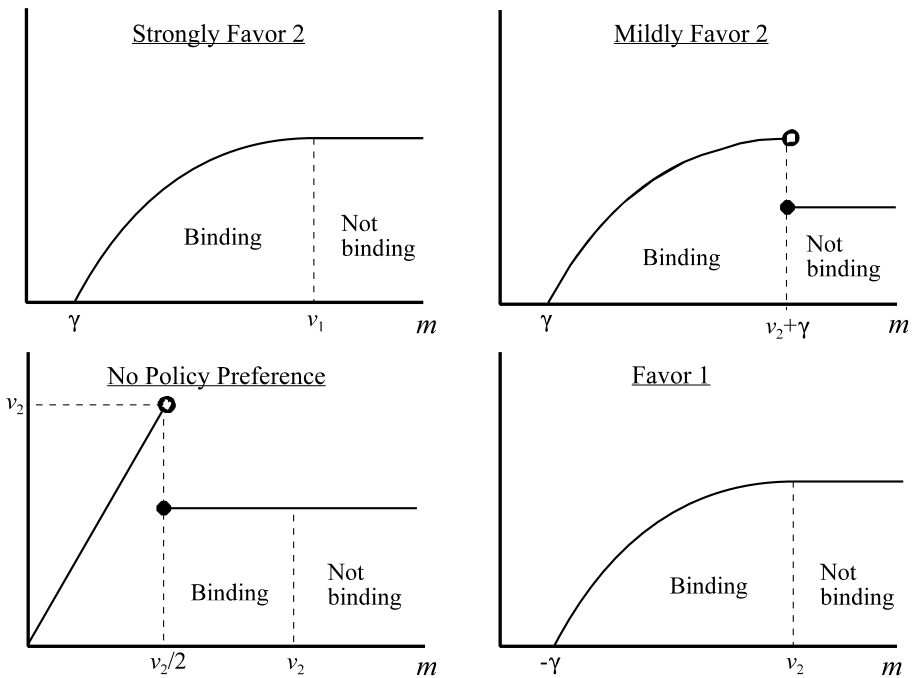


Fig. 2 Expected Aggregate Contributions with a Cap

the effect of PAC contributions on roll-call votes is mixed.¹⁵ Furthermore given that the preference of the politician would vary over policy issues, the model is consistent with the fact that the evidence appears to be strong in some policy areas but not in others.

When the politician has a preference over policy alternatives, however mild the preference may be, the equilibrium predictions are different from the case where $\gamma = 0$. In that case lobbyist 1 has an advantage in the contest due to his higher valuation of the political prize. CG show that with $\gamma = 0$ a very restrictive cap levels the playing field. This induces the low-valuation lobbyist to become more aggressive, both lobbyists contribute the maximum legal limit, and expected aggregate contributions go up. However, when the politician has a policy preference a more restrictive binding cap always tilts the playing field in favor of the preferred lobbyist irrespective of the identity of the low-valuation lobbyist and expected aggregate contributions go down.

Proposition 1 *For all $\gamma \neq 0$, making a binding cap more restrictive always reduces expected aggregate contributions.*

Proof Appendix B. □

Figure 2 gives the expected aggregate contribution as a function of m for the possible ranges of γ defined in Lemma 1. The lobbyist for the unfavored policy is constrained by the

¹⁵They survey 34 empirical papers and find that evidence on the effect of PAC contributions on roll-call votes is strong in some policy areas but not in others. For instance, on issues relating to trade there is weak evidence of the effect of PAC contributions on votes, but on issues relating to labor the evidence is very strong.

contribution cap. But the favored lobbyist is not effectively constrained since he never needs to contribute above $m - |\gamma|$ to guarantee victory. This advantage allows the favored bidder to capture a strictly positive expected value from the contest equal to $v_f - m + |\gamma|$. Hence if the cap becomes more restrictive the unfavored lobbyist becomes more constrained which is to the advantage of the favored lobbyist. As the cap gets more restrictive, the playing field is tilted more in favor of the preferred lobbyist. This decreases the overall aggressiveness of the unfavored lobbyist, which in turn induces less aggressive bidding from the preferred lobbyist, leading to decreased expected aggregate contributions. So the natural intuition put forward by proponents of campaign finance reform is indeed correct when the politician has a preference over policy alternatives. Further tightening an existing binding contribution cap always reduces expected aggregate contributions in equilibrium.

There is some empirical evidence suggesting that restrictions on campaign contributions tend to reduce campaign spending.¹⁶ Stratmann (2006) computes an index of limits of contributions to parties, PACs, corporations, unions and individuals and finds that incumbent and challenger spending both are significantly lower for state legislators from 1996 to 2000 when states have restrictions on all five sources of contributions. Stratmann and Aparicio-Castillo (2006) also exploit contribution limit variations across states with 1998 state contribution restrictions. The findings indicate that stricter limits tend to be associated with lower campaign spending. Hogan (2000) confirms the same for incumbent spending in a study with 3,253 state legislative candidates running in 27 states in the mid 1990s. In gubernatorial elections however Gross et al. (2002) find no significant effect of contribution limits on total campaign spending.

Proposition 2 *Imposition of a cap will lead to an increase in expected aggregate contributions if and only if the politician mildly favors the policy position of the low-valuation lobbyist, $\gamma \in (0, v_1 - v_2]$.*

Proof Appendix B. □

As depicted in Fig. 2, when the politician has a mild preference for the policy of the low-valuation lobbyist expected aggregate contributions jump up with the imposition of a binding cap. A similar jump in the probability that the low-valuation lobbyist wins can also be observed in Fig. 3. The case of mild-preference for the low-valuation lobbyist's policy position is different from the other cases because the imposition of a cap changes the identity of the player who has the advantage in equilibrium. When the cap is not binding and $\gamma \in (0, v_1 - v_2]$, the high-valuation bidder has the advantage in the competition. He can bid slightly higher than $v_2 + |\gamma|$ and win for sure. In equilibrium he is able to use this advantage to secure himself a positive expected payoff, competing away all of the low-valuation bidder's surplus. However, the roles are reversed when the contribution cap becomes binding (m falls below $v_2 + |\gamma|$). Now the high-valuation bidder is effectively constrained. Hence the low-valuation bidder has the option of bidding just above $m - |\gamma|$ guaranteeing victory and a positive payoff. This advantage induces the low-valuation lobbyist to bid more aggressively in equilibrium. This results in a discrete increase in expected aggregate contributions¹⁷ (see Fig. 2) and in the probability that the policy of the low-valuation lobbyist gets enacted

¹⁶Campaign expenditures closely track campaign contributions since only one percent of total expenditure is self-financed; see Herrnson (2000).

¹⁷The size of the jump is inversely related to the intensity of the preference. With a non-binding cap the low-valuation lobbyist is at a disadvantage due to his low valuation of the prize. The milder is the preference for

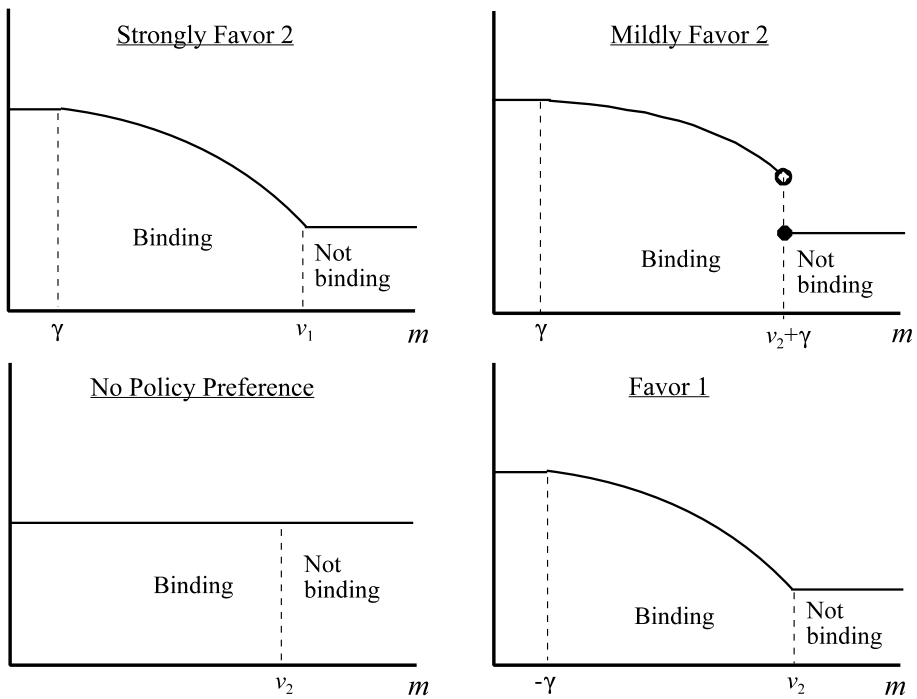


Fig. 3 The probability that the politician's favored policy is enacted

(see Fig. 3). The contribution cap does not change the basic nature of the competition—equilibrium is still in mixed strategies—but it swings the advantage from the high-valuation bidder to his rival whose policy is favored by the politician. Such a reversal does not arise in cases where the politician favors the high-valuation bidder, nor where the low-valuation bidder is strongly favored, and hence expected aggregate contributions are continuous in those cases.¹⁸

Proposition 3 *For all $\gamma \neq 0$, a more restrictive cap (decreasing m) always reduces the influence of monied interests in policy making; a more restrictive cap increases the probability*

his position the greater is his disadvantage. Introducing a binding cap tilts the playing field in his favor. Hence when the preference for his position is very mild the introduction of a binding cap makes a big difference. From a playing field tilted very much in favor of the high-valuation lobbyist, the low-valuation lobbyist now enjoys a playing field where he has the advantage. So the milder the politician's preference for his policy the greater the change in the aggressiveness of the low-valuation lobbyist, leading to a greater jump in aggregate contributions when the cap becomes binding.

¹⁸While it seems natural to model the politician's allocation rule as an additive preferential treatment, alternative specifications exist, such as the multiplicative preferential treatment in Fu (2006). However, as long as the lobbyist with the preferred policy can win the prize with a lower contribution than his rival's, a binding cap will effectively constrain only the lobbyist with the less preferred policy. Hence the favored lobbyist will have the advantage due to the cap. Whenever the politician mildly prefers the policy of the low valuation lobbyist, the introduction of a cap will switch the identity of the lobbyist with the advantage. Hence the results in Propositions 1 through 3 are likely to hold for any reasonable specification of politician preferences. Nevertheless, in this context an additive specification has the desirable property that the politician's preference for a policy does not depend on the contributions he receives.

of winning for the lobbyist whose policy position is preferred by the politician no matter whether it is the high-valuation or the low-valuation lobbyist.

Proof Appendix B. □

Figure 3 graphs the probability that the favored lobbyist wins. Since a more restrictive binding cap tilts the playing field in favor of the lobbyist with the preferred policy alternative, it always makes it more likely that the policy preferred by the politician is enacted. If the politician mildly favors the low-valuation lobbyist's position there is a jump in the probability of the low-valuation policy being enacted at the point where the cap just becomes binding. The intuition of this jump was discussed earlier in the context of Proposition 2.

Contribution caps can be expected to lower special interest group influence, as well as the amount of money contributed in order to buy political favors. A more restrictive cap makes it more likely that the politician enacts the policy alternative he would have enacted if there were no contributions (see Fig. 3). Note that this measure of the degree of influence of monied interests has an advantage over using expected aggregate contributions because it captures the concern that policy may be driven by money. The imposition of a binding cap can lead to an increase in expected aggregate contributions (Fig. 2, mild preference for the low-valuation lobbyist's policy) while at the same time leading to an increase in the probability that the politician enacts his preferred policy (Fig. 3).

Also note that in equilibrium both lobbyists have a probability mass at zero (see Fig. 1). The more restrictive the cap, the more likely it is that the politician does not receive any funds from either lobbyist. In that case the politician simply enacts his preferred policy. A more restrictive cap fosters an environment where it is less likely that special interest group money exerts influence on policy decisions.

Furthermore the politician is likely to have different intensities of policy preference across issues. For all policy issues where the preference is too strong, $|\gamma| \geq m$, lobbyists do not contribute and the politician simply goes with his conscience. A more restrictive cap implies a lower critical threshold of politician preference where there will be no influence of special interest groups on policy making. Hence politician decisions will be swayed by monied interests on a smaller number of questions. A more restrictive binding cap implies decreased expected aggregate contributions on issues where lobbying matters and it implies that there will be fewer of these policy issues. This suggests that contribution limits can help alleviate Senator Feingold's concern that "only interests with big money to contribute" will be able to effectively petition the legislature.

Propositions 1 and 2 show that a contribution cap always reduces expected aggregate contributions when $|\gamma|$ is sufficiently large. However, when the politician has a mild preference for the policy of the low-valuation lobbyist (small but positive γ), the imposition of a cap can have the unintended consequence of increasing contributions. One interpretation of $|\gamma|$ is the politician's expected future campaign costs required to offset the effect of taking a policy position that is unpopular in his district. Under this interpretation, the effect of a contribution cap on aggregate contributions can be quite different for House members versus senators, as well as for members from cities versus members from rural areas. Between congressional districts there are vast differences in the cost of communicating with constituents even though they represent the same number of voters. Stratmann (2009) finds that the cost of reaching 1% of constituents with TV advertising during prime time in the 2000 election cycle ranged from \$18 in Idaho's 2nd district to \$1875 in New York City.

Since a politician from a larger or a more urban district is likely to face a higher cost of communicating with constituents, with the same underlying policy preference the $|\gamma|$ for

this politician is likely to be higher. So the cap on contributions may change the distribution of contributions between politicians. It may result in reduced contributions to senators from larger states but increased contributions to representatives from districts contained within minor media markets. When states consider contribution caps for state level offices, the experience with national level contribution caps may not apply directly to state politicians who generally have much lower costs of communicating with constituents.

5 Discussion

The effect of a contribution cap is analyzed in a political lobbying game where the donors compete to purchase political favors and the politician has a preference for the policy position of one of the lobbyists. In contrast to the previous literature where the politician has no preference over policy alternatives, a more restrictive binding cap always reduces expected aggregate contributions. However the initial imposition of a cap increases contributions if and only if the politician mildly favors the policy of the low-valuation lobbyist. The introduction of policy preferences permits the analysis of the effect of a cap on the monied interests' influence on policy. In equilibrium a more restrictive cap makes it more likely that the politician enacts the policy alternative he would have enacted in the absence of lobbying, even in cases where expected aggregate contributions increase.

5.1 Expenditure limits

While there are caps on political lobbying in the United States, there are no limits on campaign expenditures. Expenditure limits were struck down by the 1976 Supreme Court ruling on *Buckley v. Valeo* as unconstitutional limitations on free speech. There are, however, many countries with expenditure limits in place such as the United Kingdom, Canada, France and Israel. One of the arguments in support of expenditure limits is that without such limits larger parties would have an unfair advantage over smaller parties. While our model is not tailored for expenditure limits, one may suggest some possible interpretations of the variables that might help shed light on this discussion.

Assume that there are two types of voters: party-loyal voters and swing voters. The swing voters are swayed by campaign spending while the party-loyal voters are not.¹⁹ The party with fewer loyal voters has to spend more in order to win 50% of the total votes. If the larger party tends to have more party loyal supporters, then it is subject to "preferential" treatment in the all-pay auction election game. Proposition 3 shows that a cap always increases the probability that the favored bidder wins. Thus the model may suggest that a cap on campaign expenditure (the bids of the political parties to win the election) may in fact benefit the larger party rather than the smaller party, contrary to one of its intended consequences.

5.2 Transparency of the allocation rule

This paper assumes complete information of the allocation rule the politician implements. However, in reality uncertainty about the allocation rule is common in preferential treatment contests. Students may be uncertain about affirmative action in college admissions. Job candidates may have incomplete information about the degree of preferential treatment for

¹⁹An alternative representation of swing voters is in Kovenock and Roberson (2008) where they are swayed by promises of redistributive policy.

in-house versus outsider candidates, and so on. There is a literature examining all-pay auctions where bidders have incomplete information about their rivals' valuations, for instance Amann and Leininger (1996). However the problem of uncertainty about the allocation rule is different since it does not involve asymmetric information between the bidders. To our knowledge there is no literature examining this issue. The question is of particular interest since the designer of the contest can choose the nature and degree of uncertainty. This also raises the issue of the extent of learning in repeated interactions. Empirically politicians seem to prefer to avoid ambiguity about their policy preferences; see Kroszner and Stratmann (2005). Nevertheless theoretical work needs to be done to understand why this is the case.

5.3 The effect of caps on electoral competition

This paper focuses solely on the effect of contribution caps on competition for political favors. Austen-Smith (1998) analyzes the effect of caps on the incentives incumbent politicians face when deciding whether to grant access to lobbyists. While the results of both papers are encouraging for the efficacy of contribution caps, in a broader context the effect of contribution caps on electoral outcomes may be perverse. Caps may be imposed by incumbents as entry barriers to challengers in guise of promoting clean government. Caps may make it harder to overcome the incumbent's advantage of being already well-known.²⁰

On the other hand, the ability to raise funds is much greater for incumbents than for challengers. In the 2006 elections the average incumbent senator raised \$11.3 million, while the average challenger raised \$1.8 million.²¹ A contribution to buy policy favors or access is of potential value only if the politician is in office to pay back. Over the past five election cycles from 1996 to 2004, 96.8% of House incumbents and 88% of the Senate incumbents were returned to office.²² Hence restricting the ability to raise funds may hurt the incumbent at least as much as it hurts his challenger. However the evidence is mixed on the question of who enjoys the benefit of a cap. Hamm and Hogan (2008) find that restrictions make the prospects of running against an incumbent more attractive to potential candidates. La Raja (2008) however reports that the financial gap widened in congressional races since the Bipartisan Campaign Reform Act. Incumbent fund-raising increased 20% between 2002 and 2006. But that of challengers did not. Using data on contribution limits at the state level Stratmann and Aparicio-Castillo (2006) report that limits lead to closer elections but the effect is smaller on incumbents who were in office when the law was passed.

Appendix A: Proof of Lemmas 1 and 2

The case where $\gamma = 0$ has been extensively studied (see Hillman and Riley 1989 and Baye et al. 1993, 1996 without a cap and Che and Gale 1998 with a cap) and so it will be omitted

²⁰Lohmann (1995) points out that caps on political contributions may be counterproductive because when contributions serve as an access fee they may signal the credibility of the message.

²¹These of course include races with just a token challenger. Candidates for open seats, which generally include serious challengers, raised an average of \$2.8 million, substantially below the amount the average incumbent was able to raise. The figures for House races are similar, although the amounts are lower. The average incumbent raised \$1.2 million, while the average challenger raised \$283,000. Candidates for open seats raised an average of \$584,000.

²²For comparison, if these percentages stayed constant and equal for all members and there were no voluntary retirements or deaths, the expected time in office would be roughly 43 years for senators and 50 years for representatives.

here. Claims 1 through 7 are employed in the proof of Lemmas 1 and 2. Throughout consider just the nontrivial cases where $\gamma \in (-v_2, 0) \cup (0, v_1)$ and $m > |\gamma|$. Define $z = \min(v_u, m)$. If there is no contribution cap $z = v_u$.

Claim 1 Bidder u will not put a probability mass on any level of contribution greater than zero. Without a contribution cap, bidder f will not put a probability mass on any level of contribution greater than zero. With a binding contribution cap, bidder f will not put a probability mass on any bid $b_f \in (0, m - |\gamma|)$. With or without a contribution cap, there is no equilibrium in pure strategies.

Proof Bidder u will never bid more than z . Suppose the lowest mass point of bidder u in the range $B_u = (0, z]$ is given by $b'_u \in B_u$. Then bidder f would not put any probability at $b'_f = b'_u - |\gamma|$, as a slight increase in his bid would result in a discrete increase in the probability of winning. As there is no probability of b'_f exactly, bidder u could lower his bid slightly without changing his probability of winning. Since bidder u will never bid more than z and since he has no probability mass at z by the above argument, bidder f can win for sure with a bid of $z - |\gamma|$ so he will never bid more than that. Define a range B_f as $B_f = (0, z - |\gamma|]$ if $z = v_u$ and as $B_f = (0, z - |\gamma|)$ if $z < v_u$. Suppose the lowest mass point of bidder f in B_f is given by $b'_f \in B_f$. Bidder u would not put any probability at $b''_u = b'_f + |\gamma|$ since bidding $b''_u = b'_f + |\gamma| + \varepsilon$ would yield a discrete increase in probability. So bidder f would prefer a slightly lower bid than b'_f . Both players' bidding zero cannot be sustained as a pure-strategy equilibrium either, since the best response to $b_f = 0$ would be to bid slightly higher than $|\gamma|$. \square

Claim 2 With or without a contribution cap, bidder u will put zero probability on $b_u \in (0, |\gamma|]$.

Proof If bidder u contemplates $b_u \in (0, |\gamma|)$ a bid of zero will win with the same probability as he must exceed his rival's bid by at least $|\gamma|$ in order to win. If $b_u = |\gamma|$ then he can win only if $b_f = 0$, in which case there is an even chance of winning. If $b_u = |\gamma|$ gives bidder u nonnegative payoff he could double his chances of winning by a slight increase in his bid. And if $b_u = |\gamma|$ gives him a negative payoff he could get a zero payoff by dropping his bid to zero. \square

Claim 3 If there is a binding contribution cap, or if $\gamma \in (-v_2, 0) \cup (v_1 - v_2, v_1)$ without a contribution cap, bidder u has an infimum bid of zero, and $EV_u = 0$.

Proof Bidder u would never bid higher than z . Bidder u 's infimum bid must be less than z since there can be no probability mass at z by Claim 1. Suppose that bidder u has an infimum bid of $b'_u \in (|\gamma|, z)$. Then bidder f would never choose $0 < b_f \leq b'_u - |\gamma|$. If he did he would be paying a positive amount and would lose for sure, since the probability of bidder u choosing exactly b'_u is zero by Claim 1. Therefore bidder u could lower his bid without changing the probability of winning. Suppose that bidder u 's infimum bid is $b'_u = |\gamma|$ where bidder u is mixing in the open interval above $|\gamma|$ but not at $|\gamma|$, by Claim 2. Then bidder f would never bid zero as this would give a zero payoff and he can win for sure with a bid of $z - |\gamma| + \varepsilon$ yielding a positive payoff. Take a bid of $b_u = |\gamma| + \varepsilon$, the probability that bidder u wins with this bid is $\int_{|\gamma|}^{|\gamma|+\varepsilon} f_f(x - |\gamma|) dx$. Since bidder f has no mass point on $(0, \varepsilon]$ by Claim 1, this probability is close to zero for small ε , yielding a negative expected payoff

for bidder u . Hence bidder u 's infimum bid cannot be $|\gamma|$. $b_u^{\text{inf}} \in (0, |\gamma|)$ is not possible by Claim 2. Therefore $b_u^{\text{inf}} = 0$. At this bid he loses for sure, so $EV_u = 0$. \square

Claim 4 *If there is a binding contribution cap, or if $\gamma \in (-v_2, 0) \cup (v_1 - v_2, v_1)$ without a contribution cap, bidder u has a supremum bid of z . Bidder f has a supremum bid of $z - |\gamma|$ and $EV_f = v_f + |\gamma| - z > 0$.*

Proof Suppose that bidder u has a supremum bid of $b'_u < z$. Then bidder f would never set $b_f > \max[0, b'_u - |\gamma|]$ as he can win for sure with $b_f = \max[0, b'_u - |\gamma|]$ since the probability of bidder u choosing exactly b'_u is zero by Claim 1. Therefore bidder u could win for sure with $b_u = b'_u + \varepsilon$ yielding a payoff greater than zero for small enough ε , a contradiction of Claim 3. Hence the supremum bid of u , $b_u^{\text{sup}} = z$. Suppose that bidder f had a supremum bid of $b'_f < z - |\gamma|$. Then bidder u could win for sure with $b_u = b'_f + |\gamma| + \varepsilon$ yielding a payoff greater than zero for small enough ε , a contradiction of Claim 3. Bidder f can win for sure with a bid in the open interval above $z - |\gamma|$ hence $b_f^{\text{sup}} = z - |\gamma|$. Since $z - |\gamma|$ is in the support of f 's mixed strategy and he wins for sure with that bid, $EV_f = v_f + |\gamma| - z$. \square

Claim 5 *Without a contribution cap, if $\gamma \in (0, v_1 - v_2]$, $u = 1$ and $f = 2$, bidder u has an infimum bid of γ . Bidder f has an infimum bid of zero and $EV_f = 0$.*

Proof Bidder u can win for sure with a bid of $v_f + \gamma$ yielding a payoff of $v_u - v_f - \gamma > 0$. He would never bid zero since he would lose for sure. $b_u^{\text{inf}} \in (0, \gamma)$ is not possible by Claim 2. $b_u^{\text{inf}} = v_f + \gamma$ would be a pure strategy, but Claim 1 establishes that there is no pure-strategy Nash equilibrium. Suppose that bidder u has an infimum bid of $b'_u \in (\gamma, v_f + \gamma)$. Then bidder f would never choose $0 < b_f \leq b'_u - \gamma$. If he did he would be paying a positive amount and would lose for sure, since by Claim 1, the probability of bidder u choosing exactly b'_u is zero. Therefore, bidder u could lower his bid without changing the probability of winning. Hence $b_u^{\text{inf}} = \gamma$. Suppose bidder f had an infimum bid of $b'_f \in (0, v_f]$, then bidder u would never choose $b_u \leq b'_f + \gamma$. If he did, bidder u would lose for sure yielding a negative payoff. Since by Claim 1 the probability of bidder f choosing exactly b'_f is zero and bidder u can always guarantee a positive payoff of $v_u - v_f - \gamma > 0$. But then bidder f would prefer a bid of zero to b'_f . Therefore $b_f^{\text{inf}} = 0$. At this bid he loses for sure, so $EV_f = 0$. \square

Claim 6 *Without a contribution cap, if $\gamma \in (0, v_1 - v_2]$, $u = 1$ and $f = 2$ and bidder u has a supremum bid of $v_f + |\gamma|$ and $EV_u = v_u - v_f - \gamma > 0$. Bidder f has a supremum bid of v_f .*

Proof Given that f would never bid higher than his valuation of the prize, u would never bid higher than $v_f + |\gamma|$. Suppose that bidder u had a supremum bid of $b'_u < v_f + |\gamma|$. Then bidder f would never set $b_f > \max[0, b'_u - |\gamma|]$ as he can win for sure with $b_f = \max[0, b'_u - |\gamma|]$ since the probability of bidder u choosing exactly b'_u is zero by Claim 1. Therefore bidder f could win for sure with $b_f = b'_u - |\gamma| + \varepsilon$ yielding a payoff greater than zero for small enough ε , a contradiction of Claim 5. So $b_u^{\text{sup}} = v_f + |\gamma|$. By Claim 1, bidder u wins for sure with a bid of $v_2 + |\gamma|$, so $EV_u = v_u - v_f - |\gamma| > 0$. Suppose that bidder f has a supremum bid of $b'_f \in (0, v_f)$. Then bidder u would never set $b_u > b'_f + |\gamma|$ since he could win for sure with $b_u = b'_f + |\gamma|$ given that probability that bidder f chooses b'_f exactly is equal to zero by Claim 1. Therefore bidder f could win for sure with $b_f = b'_f + \varepsilon$ yielding a payoff greater than zero for small enough ε , a contradiction of Claim 5. So $b_f^{\text{sub}} = v_f$. \square

Claim 7 For bidder u bids almost everywhere on $b_u \in (b'_u, b''_u)$ and for bidder f , bids almost everywhere on $b_f \in (b'_f, b''_f)$ must have positive probability, where

if there is no contribution cap:

$$\forall \gamma \in (v_1 - v_2, v_1) \cup (-v_2, 0) \quad b'_u = |\gamma|, b''_u = v_u \quad \text{and} \quad b'_f = 0, b''_f = v_u - |\gamma|$$

$$\forall \gamma \in (0, v_1 - v_2] \quad b'_u = |\gamma|, b''_u = v_f + |\gamma| \quad \text{and} \quad b'_f = 0, b''_f = v_f$$

if there is a contribution cap:

$$b'_u = |\gamma|, b''_u = m \quad \text{and} \quad b'_f = 0, b''_f = m - |\gamma|$$

Proof Suppose there were an interval (t, s) in (b'_u, b''_u) where bidder u had zero probability of bidding. Then bidder f would have zero probability of bidding in $(t - |\gamma|, s - |\gamma|)$ since he could lower his bid to $t - |\gamma|$ and have the same chance of winning. But in this case bidder u would never bid $s + \varepsilon$ as he could lower his bid to t , saving $s + \varepsilon - t$ in bidding costs and losing only $F_f(s + \varepsilon - \gamma) - F_f(t - \gamma)$ in probability. By Claim 1 the loss in probability is negligible for small ε . So if there were an interval of zero probability it must go up to b''_u , which depending parameter values contradicts either Claim 4 or Claim 6. A symmetric argument rules out ranges of zero probability for bidder f on $b_f \in (b'_f, b''_f)$. \square

Proof of Lemma 1 (Characterization of the equilibrium without cap)

(i) $\gamma \in (-v_2, 0) \cup \gamma \in (v_1 - v_2, v_1)$. Claims 1, 2, 3, 4 and 7 show that bidder u must be indifferent among all bids almost everywhere in $\{0\} \cup (|\gamma|, v_u]$ and bidder f is indifferent among all bids almost everywhere in $[0, v_u - |\gamma|]$. $EV_u = 0$ by Claim 3. Bidder u wins the prize v_u when he bids $b \in (|\gamma|, v_u]$ only with the probability that bidder f contributes less than $b - |\gamma|$. Hence, $v_u F_f(b - |\gamma|) - b = 0$. So, $F_f(b) = (b + |\gamma|)/v_u \forall b \in [0, v_u - |\gamma|]$. Bidder f has a probability mass equal to $|\gamma|/v_u$ at zero. $EV_f = v_f + |\gamma| - v_u$ by Claim 4. Bidder f wins the prize v_f when he bids $b \in [0, v_u - |\gamma|]$ only with the probability that bidder u does not exceed bidder f 's bid by more than $|\gamma|$: So the indifference implies $v_f F_u(b + |\gamma|) - b = v_f - v_u + |\gamma|$. Hence $F_u(b) = (v_f - v_u + b)/v_f \forall b \in (|\gamma|, v_u]$. Bidder u has a probability mass equal to $(v_f - v_u + |\gamma|)/v_f$ at zero. And he puts zero probability on $(0, |\gamma|]$ by Claim 2.

(ii) $\gamma \in (0, v_1 - v_2]$. In this case $f = 2$ and $u = 1$. Claims 1, 2, 5, 6, and 7 show that bidder u is indifferent between bids almost everywhere in $(\gamma, v_f + \gamma]$ and bidder f is indifferent between bids almost everywhere in $[0, v_f]$. $EV_u = v_u - v_f - \gamma$, by Claim 6. Bidder u wins the prize v_u when he bids $b \in (\gamma, v_f + \gamma]$ only if bidder f bids less than $b - \gamma$. Therefore $v_u F_f(b - \gamma) - b = v_u - v_f - \gamma$. So, $F_f(b) = (v_u - v_f + b)/v_1 \forall b \in [0, v_f]$. Bidder f has a probability mass of $(v_u - v_f)/v_u$ at zero. $EV_f = 0$ by Claim 5. Bidder f wins the prize v_f when he bids $b \in [0, v_f]$, only if bidder u bids less than $b + \gamma$. So, $v_f F_u(b + \gamma) - b = 0$. Therefore $F_u(b) = (b - \gamma)/v_f \forall b \in (\gamma, v_f + \gamma]$. Bidder u puts zero probability on $(0, \gamma]$ by Claim 2. \square

Proof of Lemma 2 (Characterization of the equilibrium with a cap)

Claims 1, 2, 3, 4 and 7 demonstrate that in equilibrium bidder u is indifferent among all bids almost everywhere in $\{0\} \cup (|\gamma|, m]$ and bidder f is indifferent among all bids almost everywhere in $[0, m - |\gamma|]$. $EV_u = 0$ by Claim 3. Bidder u wins the prize v_u when he bids $b \in (|\gamma|, m]$ only if the bidder whose policy is favored bids less than $b - |\gamma|$. Hence, $v_u F_f(b - |\gamma|) - b = 0$. So, $F_f(b) = (b + |\gamma|)/v_u \forall b \in [0, m - |\gamma|]$. Bidder f has a probability mass equal to $|\gamma|/v_u$ at zero. The equilibrium distribution function is discontinuous. There is a probability mass equal to $1 - F_f(m - |\gamma|) = 1 - m/v_u$ in the open interval above $m - |\gamma|$.

$EV_f = v_f + |\gamma| - m$ by Claim 4. Bidder f wins the prize v_f when he bids $b \in [0, m - |\gamma|]$ only with the probability that bidder u does not exceed bidder f 's bid by more than $|\gamma|$: $v_f F_u(b + |\gamma|) - b = v_f + |\gamma| - m$. So, $F_u(b) = (v_f - m + b)/v_f \forall b \in (|\gamma|, m]$. Bidder u has a probability mass equal to $(v_f - m + |\gamma|)/v_f$ at zero. There is a gap in the support of equilibrium bids. By Claim 2 bidder u puts zero probability on $(0, |\gamma|]$. \square

Appendix B: Proof of Propositions

Proof of Proposition 1 (Change in expected aggregate contributions w.r.t. binding cap)

On $b \in (|\gamma|, m]$ the p.d.f. of the bids of bidder u is $f_u(b) = 1/v_f$. The expected contribution of bidder u is

$$\int_{b_u=|\gamma|^+}^m x f_u(x) dx = \frac{m^2 - \gamma^2}{2v_f}$$

On $b \in (0, m - |\gamma|]$ the p.d.f. of bidder f 's bids is $f_f(b) = 1/v_u$. The expected contribution of bidder f is

$$\int_{b_f=0}^{(m-|\gamma|)} x f_f(x) dx + (m - |\gamma|)(1 - m/v_u) = \frac{(m - |\gamma|)}{2v_u} (2v_u - m - |\gamma|)$$

The derivative of expected aggregate contributions with respect to m is equal to $[(m/v_f) + (v_u - m)/v_u]$. This term is positive since when $\gamma \in (-v_2, 0) \cup \gamma \in (v_1 - v_2, v_1)$ a binding cap is $m < v_u$ and when $\gamma \in (0, v_1 - v_2]$ $u = 1$ and $f = 2$ so $v_u > v_f$. \square

Proof of Proposition 2 (Change in expected aggregate contributions due to imposition of a binding cap)

See Sect. 3 in the main text for the derivation of expected contributions when there is no cap. See the proof of Proposition 2 above for expected aggregate contributions when there is a binding cap. Evaluate expected aggregate contributions with a binding cap where the cap just becomes binding. When $\gamma \in (-v_2, 0) \cup (v_1 - v_2, v_1)$ expected aggregate contributions is continuous at the point where the cap becomes just binding ($m = v_2 - \epsilon$) and it equal to $[(v_2^2 - |\gamma|^2)/2v_1 + (v_2 - |\gamma|)^2/2v_2]$ as $\epsilon \rightarrow 0$. However when $\gamma \in (0, v_1 - v_2]$, expected aggregate contributions is discontinuous. The expected aggregate contributions with no cap are equal to $[(v_2 + 2\gamma)/2 + v_2^2/2v_1]$. The expected aggregate contributions with a binding cap where the cap just becomes binding ($m = v_2 + |\gamma| - \epsilon$) is equal to $[(v_2 + 2|\gamma|)/2 + v_2(2v_1 - v_2 - 2|\gamma|)/2v_1]$ as $\epsilon \rightarrow 0$. Hence the imposition of a barely binding cap leads to a discrete jump up in expected aggregate contributions. The size of the jump is equal to $[(v_1 - (v_2 + |\gamma|)v_2/v_1) > 0$. \square

Proof of Proposition 3 (Change in $prob_f$ w.r.t. cap)

Bidder u wins the prize with a bid b only with the probability that bidder f does not exceed $b - |\gamma|$. By Lemmas 1 and 2 if there is a binding contribution cap, or if $\gamma \in (-v_2, 0) \cup (v_1 - v_2, v_1)$ without a contribution cap then

$$Prob_u = \int_{b=|\gamma|^+}^z F_f(x - |\gamma|) f_u(x) dx = \int_{b=|\gamma|^+}^z \frac{x}{v_u v_f} dx = (z^2 - \gamma^2)/2v_u v_f$$

Since $z = \min(v_u, m)$, if $\gamma \in (-v_2, 0) \cup (v_1 - v_2, v_1)$ the probability that the unfavored lobbyist wins is continuous and increasing in m , hence the probability that the favored lobbyist wins is continuous and decreasing in m . Likewise if $\gamma \in (0, v_1 - v_2]$ whenever the cap is binding the probability that the favored lobbyist wins is continuous and decreasing in m . In Sect. 3 it is shown that when $\gamma \in (0, v_1 - v_2]$ and there is no cap the probability that bidder u wins the contest is equal to $(1 - v_f/2v_u)$. When a barely binding cap is introduced ($m = v_2 + |\gamma| - \varepsilon$) the probability that bidder u wins the contest jumps down to $[(v_f + 2|\gamma|)/2v_u]$ where $u = 1$ and $f = 2$. Hence the discrete increase in the probability that the favored policy position enacted is given by $[(v_u - (v_f + |\gamma|))/v_u] > 0$. \square

References

- Amann, E., & Leininger, W. (1996). Asymmetric all-pay auctions with incomplete information: the two-player case. *Games and Economic Behavior*, 14, 1–18.
- Amegashie, A. (2003). The all-pay auction when a committee awards the prize. *Public Choice*, 116(1–2), 79–90.
- Ansolabehere, S., de Figueiredo, J., & Snyder, J. (2003). Why is there so little money in US politics? *Journal of Economic Perspectives*, 17(1), 105–130.
- Ansolabehere, S., & Snyder, J. (1999). Money and institutional power. *Texas Law Review*, 77, 1673–1704.
- Ansolabehere, S., Snyder, J., & Tripathi, M. (2002). Are PAC contributions and lobbying linked? New evidence from the 1995 lobby disclosure act. *Business and Politics*, 4(2), 131–155.
- Austen-Smith, D. (1995). Campaign contributions and access. *American Political Science Review*, 89(3), 566–581.
- Austen-Smith, D. (1998). Allocating access for information and contributions. *Journal of Law, Economics and Organization*, 14, 277–303.
- Baye, M., Kovenock, D., & de Vries, C. (1993). Rigging the lobbying process: an application of all-pay auctions. *American Economic Review*, 83(1), 289–294.
- Baye, M., Kovenock, D., & de Vries, C. (1996). The all-pay auction with complete information. *Economic Theory*, 8(2), 291–305.
- Bronars, S., & Lott, J. (1997). Do campaign donations alter how a politician votes? Or do donors support candidates who value the same thing that they do? *Journal of Law and Economics*, 40(October), 317–350.
- Che, Y., & Gale, I. (1998). Caps on political lobbying. *American Economic Review*, 88(3), 643–651.
- Drazen, A., Limão, N., & Stratmann, T. (2007). Political contribution caps and lobby formation: theory and evidence. *Journal of Public Economics*, 91(3–4), 723–754.
- Denzau, A., & Munger, M. (1986). Legislators and interest groups: how unorganized interests get represented. *American Political Science Review March*, 80(1), 89–106.
- Fu, Q. (2006). A theory of affirmative action in college admissions. *Economic Inquiry*, 44, 420–428.
- Gale, I., & Che, Y. (2006). Caps on political lobbying: reply. *American Economic Review*, 96(4), 1355–1360.
- Gavious, A., Moldovanu, B., & Sela, A. (2002). Bid costs and endogenous bid caps. *Rand Journal of Economics*, 33(4), 709–722.
- Grier, K., & Munger, M. (1991). Committee assignments, constituent preferences, and campaign contributions. *Economic Inquiry*, 29(January), 24–43.
- Grier, K., Munger, M., & Roberts, B. (1994). The determinants of industrial political activity, 1978–1986. *American Political Science Review*, 88(4), 911–926.
- Gross, D., Goidel, R., & Shields, T. (2002). State campaign finance regulations and electoral competition. *American Politics Research*, 30(2), 143–165.
- Grossman, G., & Helpman, E. (1996). Electoral competition and special interest politics. *Review of Economic Studies*, 63, 265–286.
- Hall, R., & Wayman, F. (1990). Buying time: moneyed interests and the mobilization of bias in congressional committees. *American Political Science Review*, 3(September), 797–820.
- Hamm, K., & Hogan, R. (2008). Campaign finance laws and candidacy decisions in state legislative elections. *Political Research Quarterly*, March, 1–10.
- Hart, D. (2001). Why do some firms give? Why do some firms give a lot? High-tech PACs, 1977–1996. *Journal of Politics*, 63(4), 1230–1249.
- Hernson, P. (2000). *Congressional elections: campaigning at home and in washington* (3rd ed.). Washington: CQ Press.

- Hillman, A., & Riley, J. (1989). Politically contestable rents and transfers. *Economics and Politics*, 1(1), 17–39.
- Hogan, R. (2000). The costs of representation in state legislatures: explaining variations in campaign spending. *Social Science Quarterly*, 81(4), 941–956.
- Kaplan, T., & Wettstein, D. (2006). Caps on political lobbying: comment. *American Economic Review*, 96(4), 1351–1354.
- Kaplan, T., Luski, I., Sela, A., & Wettstein, D. (2002). All-pay auctions with variable rewards. *Journal of Industrial Economics*, 50(4), 417–430.
- Konrad, K. (2002). Investment in the absence of property rights; the role of incumbency advantages. *European Economic Review*, 46, 1521–1537.
- Kovenock, D., & Roberson, B. (2008). Electoral poaching and party identification. *Journal of Theoretical Politics*, 20(3), 275–302.
- Kroszner, R., & Stratmann, T. (1998). Interest group competition and the organization of congress: theory and evidence from financial services political action committees. *American Economic Review*, 88(5), 1163–1187.
- Kroszner, R., & Stratmann, T. (2000). Congressional committees as reputation-building mechanisms: repeat PAC giving and seniority on the house banking committee. *Business and Politics*, 2, 35–52.
- Kroszner, R., & Stratmann, T. (2005). Corporate campaign contributions, repeat giving, and the rewards to legislator reputation. *Journal of Law and Economics*, April, 41–71.
- Langbein, L. (1986). Money and access: some empirical evidence. *Journal of Politics*, 48(November), 1052–1062.
- La Raja, R. (2008). From bad to worse: the unraveling of the campaign finance system. *The Forum*, 6(1), Article 2.
- Lohmann, S. (1995). Information, access, and contributions: a signaling model of lobbying. *Public Choice*, 85(3–4), 267–284.
- Lott, J. (2000). A simple explanation for why campaign expenditures are increasing: the government is getting bigger. *Journal of Law and Economics*, 43(2), 359–393.
- Magee, C. (2002). Do political action committees give money to candidates for electoral or influence motives? *Public Choice*, 112(3–4), 373–399.
- Milyo, J. (1997). Electoral and financial effects of changes in committee power: the Gramm-Rudman-Hollings budget reform, the Tax Reform Act of 1986, and the money committees in the House. *Journal of Law and Economics*, 40(April), 93–112.
- Pastine, I., & Pastine, T. (2008). *Soft money and caps on political contributions*. Mimeo.
- Pastine, I., & Pastine, T. (2009). *Student incentives and diversity in college admissions*. Mimeo.
- Pittman, R. (1998). Rent-seeking and market structure: comment. *Public Choice*, 58(2), 173–185.
- Romer, T., & Snyder, J. (1994). An empirical investigation of the dynamics of PAC contributions. *American Journal of Political Science*, 38(August), 745–769.
- Siegel, R. (2009). All-pay contests. *Econometrica*, 77(1), 71–92.
- Snyder, J. (1990). Campaign contributions as investments: the House of Representatives, 1980–1986. *Journal of Political Economy*, 98(6), 1195–1227.
- Snyder, J. (1992). Long-term investing in politicians, or give early, give often. *Journal of Law and Economics*, 35(1), 15–44.
- Snyder, J. (1993). The market for campaign contributions: evidence for the US Senate, 1980–1986. *Economics and Politics*, 5(3), 219–40.
- Stratmann, T. (2002). Can special interests buy congressional votes? Evidence from financial services legislation. *Journal of Law and Economics*, 45(2), 345–374.
- Stratmann, T. (2006). Contribution limits and the effectiveness of campaign spending. *Public Choice*, 129, 461–474.
- Stratmann, T. (2009). How prices matter in politics: the returns to campaign advertising. *Public Choice*, 127(3–4), 177–206.
- Stratmann, T., & Aparicio-Castillo, F. (2006). Competition policy for elections: do campaign contribution limits matter? *Public Choice*, 127, 177–206.
- Wright, J. (1990). Contributions, lobbying and committee voting in the US House of Representatives. *American Political Science Review*, 84(June), 417–438.
- Yildirim, H. (2005). Contests with multiple rounds. *Games and Economic Behavior*, 51, 213–227.
- Zardkoohi, A. (1998). Market structure and campaign contributions: does concentration matter? A reply. *Public Choice*, 58(2), 187–191.